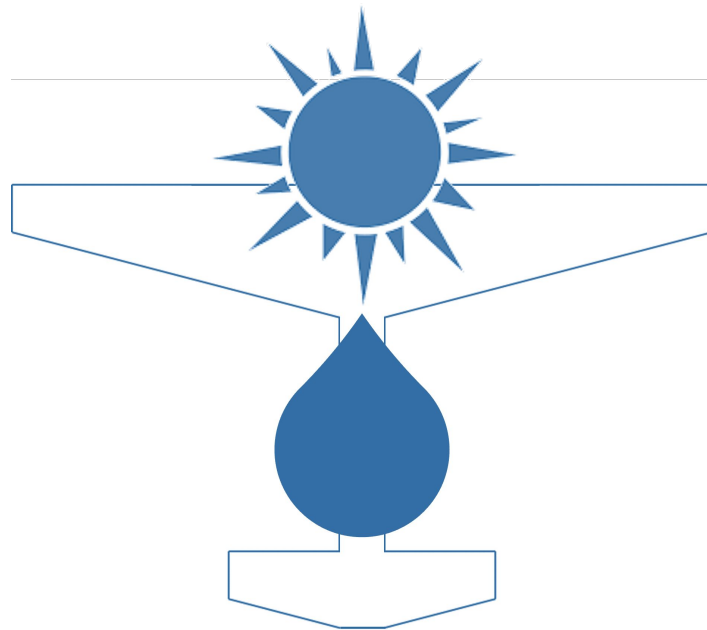



Aide Mill  
Alberto Berra  
Ethan Jones  
Lance Lee  
Summer Hoss  
Dhranyal  
~~Johann Hieber~~  
Andrew C. Nagy



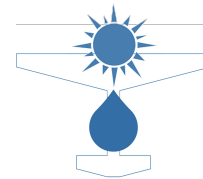
Team Water

Matthew J. McLittick   
Moto  
Blake Stephens  
Austin  
Zachary Brown  
Chris  
Paul B...  
Wm...  
N...  
V...

# Team Water

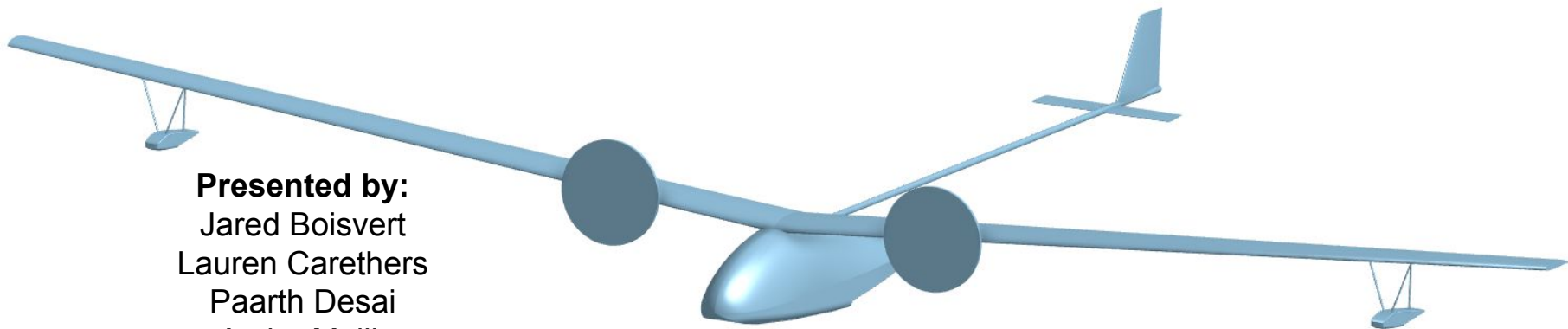
Presents:

# SEAWAY



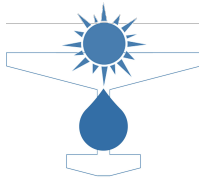
*Solar Electric Aquatic Winged Air Yacht*

*"The new way to see new sights"*



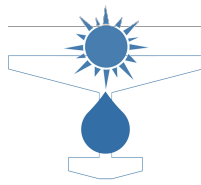
**Presented by:**

Jared Boisvert  
Lauren Carethers  
Paarth Desai  
Amira Malik  
Josh Malone  
Joey Merkel  
Jax Rivers  
David von Wrangel



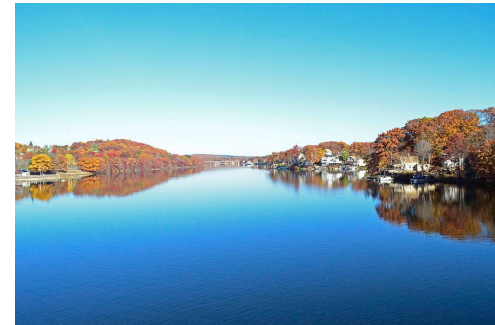
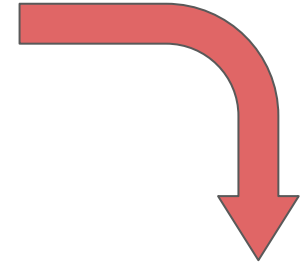
# Outline

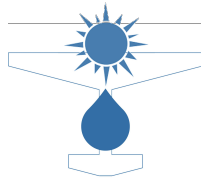
1. **Motivation**
2. General Overview
3. Subsystem Design
4. Risk
5. Conclusion



# The Road to Seaway

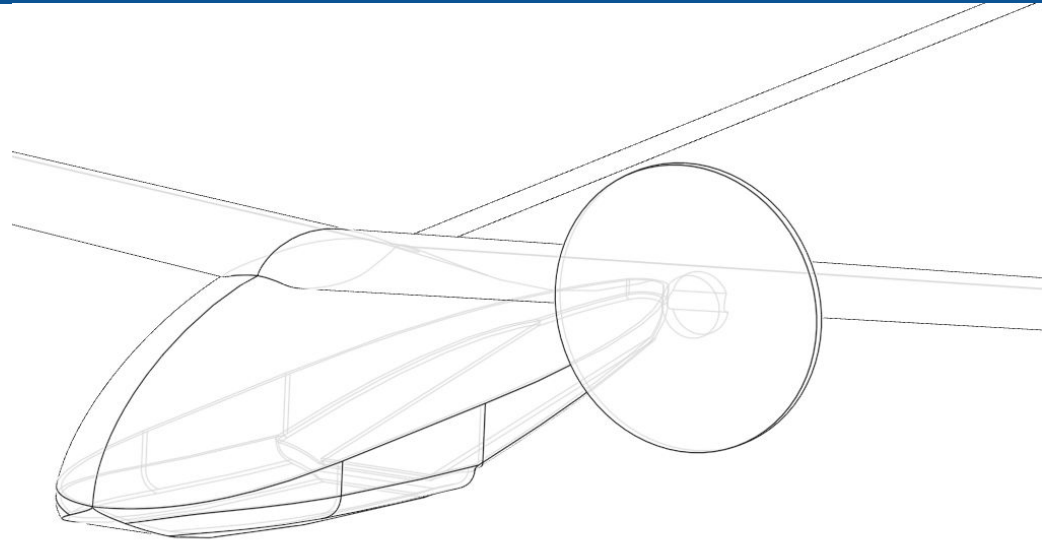
- Allow people easy entry to the world of aviation
- Go see the great outdoors and be fully immersed in nature
- Do so in an environmentally friendly way

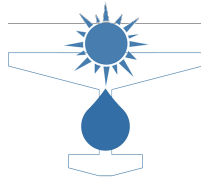




# SEAWAY is born

- **Ultralight!**
  - Cheaper to operate and maintain, no pilot's license required
- **Seaplane!**
  - Can land in remote areas w/o a runway
- **Solar Powered!**
  - Completely off the grid for zero emissions

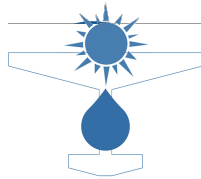




# Targeted Audience

- Backpackers
- Wilderness Fishermen
- Aviation Enthusiasts
- Adventurous Professionals





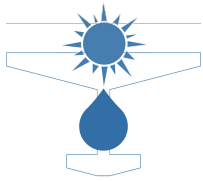
# Requirements

Specification	Requirement
Stall Speed (power off)	<24 kts CAS
Empty Weight	304 lbs (254 regular + 50 as seaplane w/ 2 pylons)
Max Speed	<55 kts. CAS (full power in level flight)
In-Flight Emissions	Zero
Range	>100 mi
Max Payload	260 lbs: 1 Passenger (230 lbs.) + cargo (30 lbs)
Takeoff Distance	<1000 ft
Runway Terrain	Water (Seaplane)

FAA  
Part 103

16.82

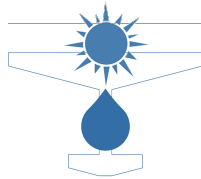
Self-  
Imposed



# Outline

1. Motivation
2. **General Overview**
  - a. Vehicle Configuration
  - b. Mass Breakdown
3. Subsystem Design
4. Risk
5. Conclusion





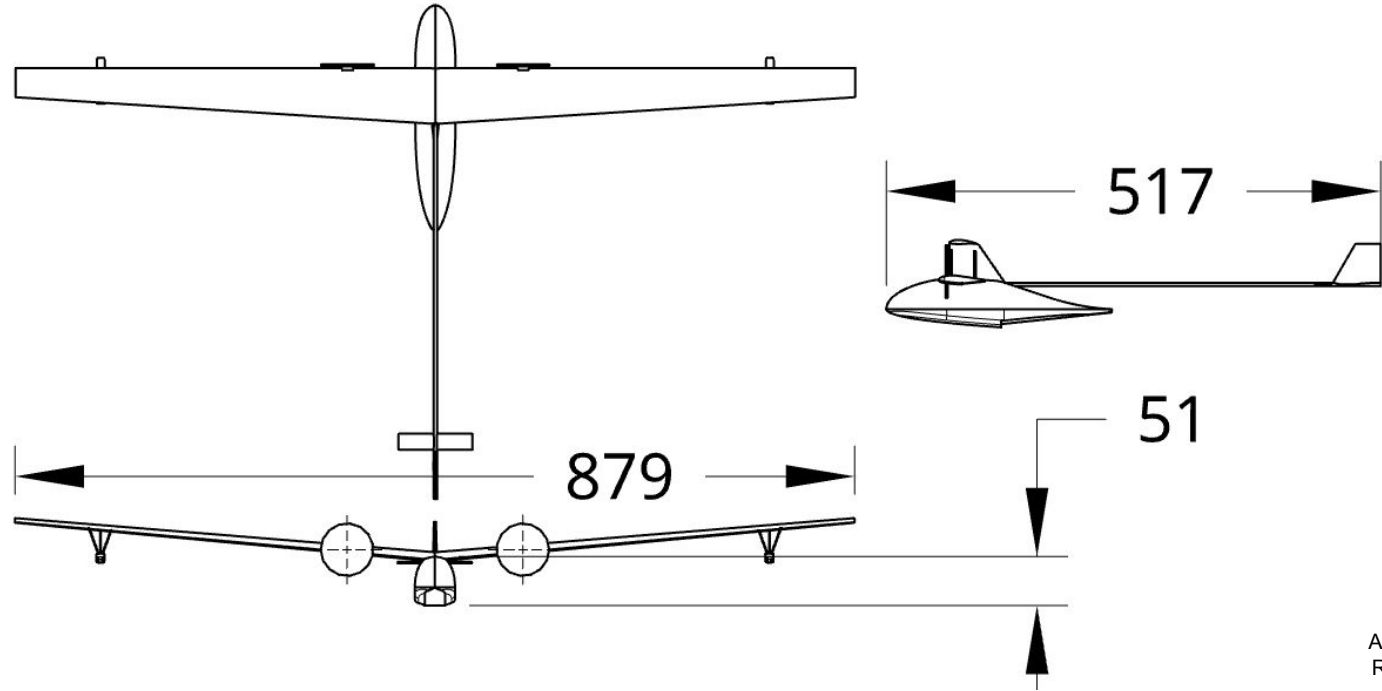
# Meet: SEAWAY

## Driven By Solar:

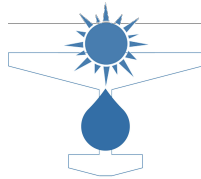
- Large Wing Area
- Efficiency-first Wing
- Small Tail Surfaces

## Driven By Water:

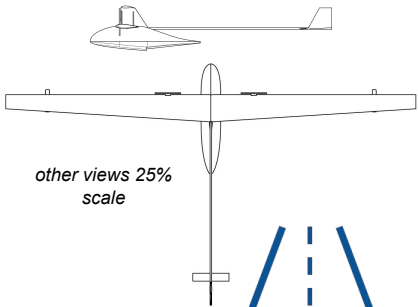
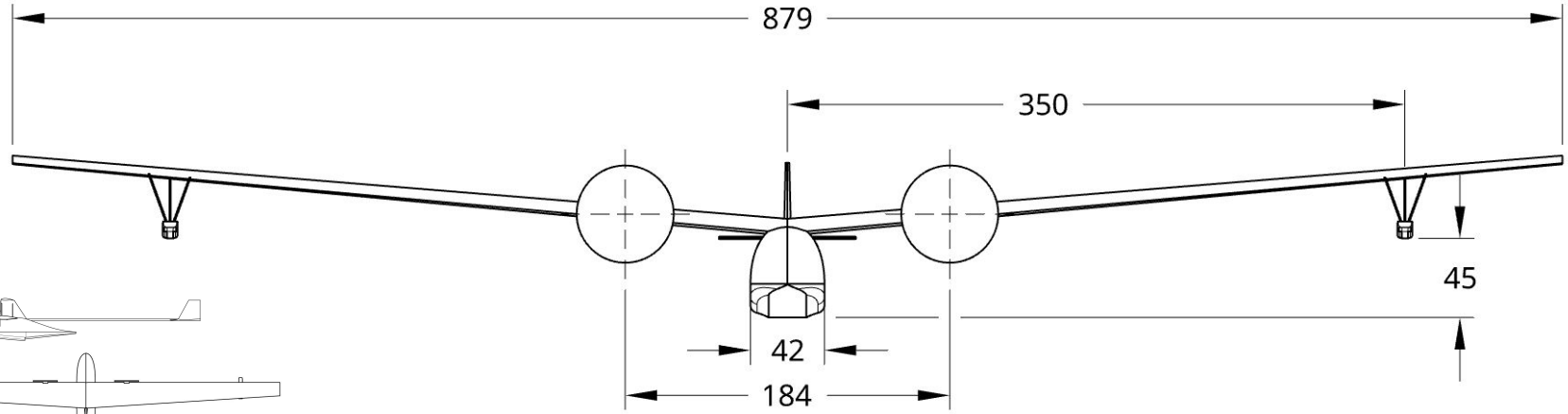
- Planing Hull
- Wing Floats
- Lifted Tail



All in inches  
Rev. 9 12/8



# Meet: SEAWAY, Head-On



**1000' Runway**

**0 Emissions**

**MTOW**  
**582 lbs**

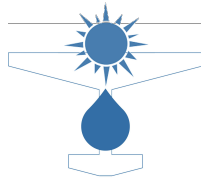
**Cruise**  
**33 KCAS**

**Stall**  
**23 KCAS**

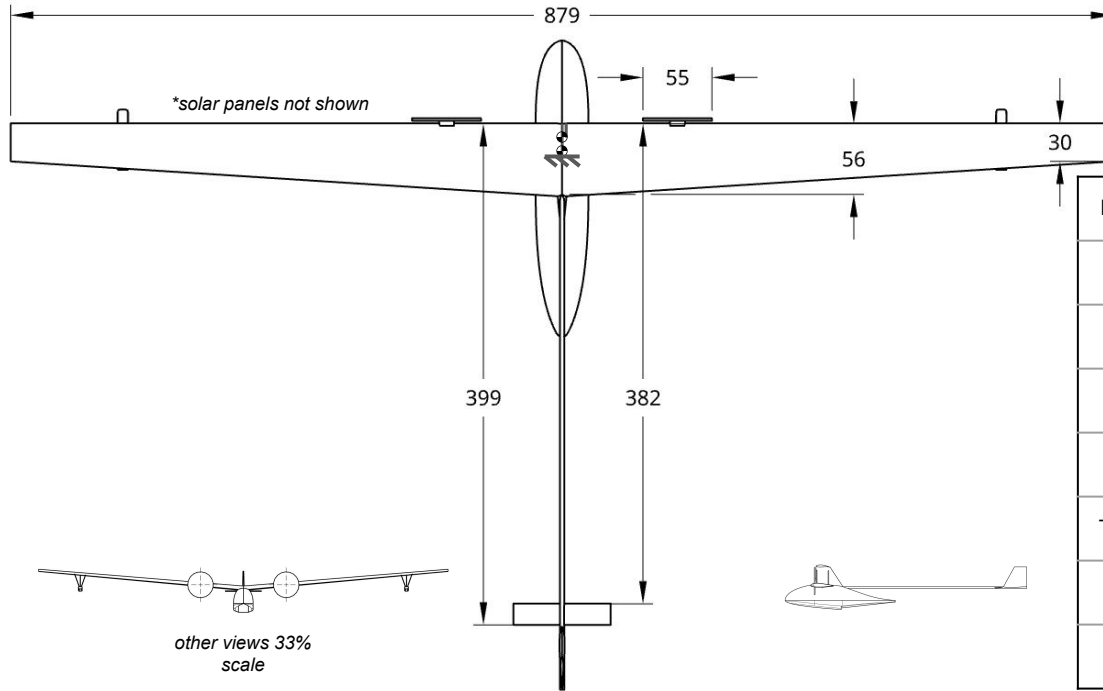
**∞ Range\***

**Max Altitude**  
**3000'**

All in inches  
Rev. 9 12/8



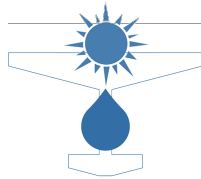
# Meet: SEAWAY, From the Top



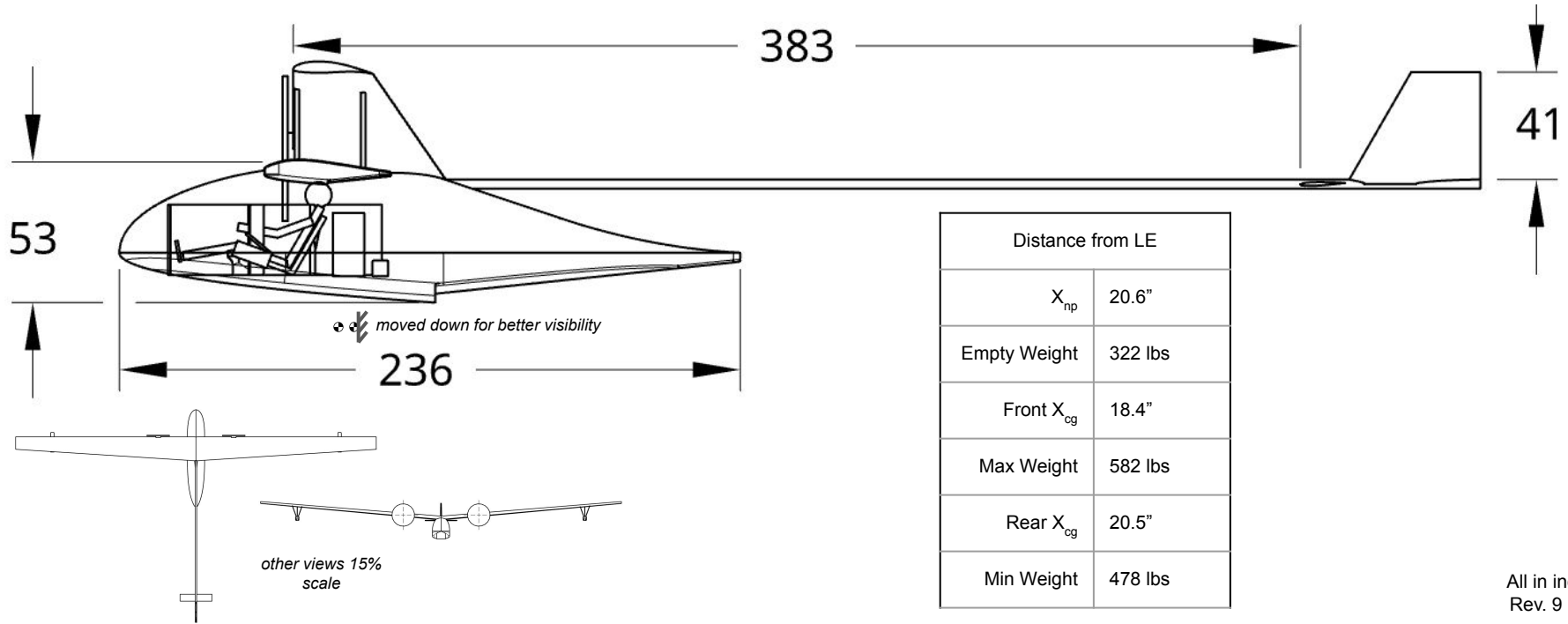
Distance from LE	
$X_{np}$	20.6"
Empty Weight	322 lbs
Front $X_{cg}$	18.4"
Max Weight	582 lbs
Rear $X_{cg}$	20.5"
Min Weight	478 lbs

Reynolds #	1,300,000
L/D	25.7
AR	19.5
↓ MTOW ↓	
Thrust <sub>cruise</sub>	195 N
Thrust <sub>TakeOff</sub>	275 N
$P_{Required}$	3300 W
$P_{Generated}$	3400 W

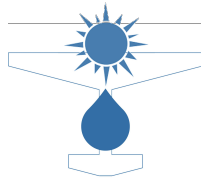
All in inches  
Rev. 9 12/8



# Meet: SEAWAY, Another Aside

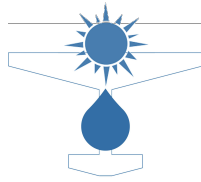


All in inches  
Rev. 9 12/8

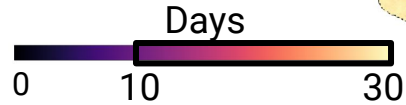
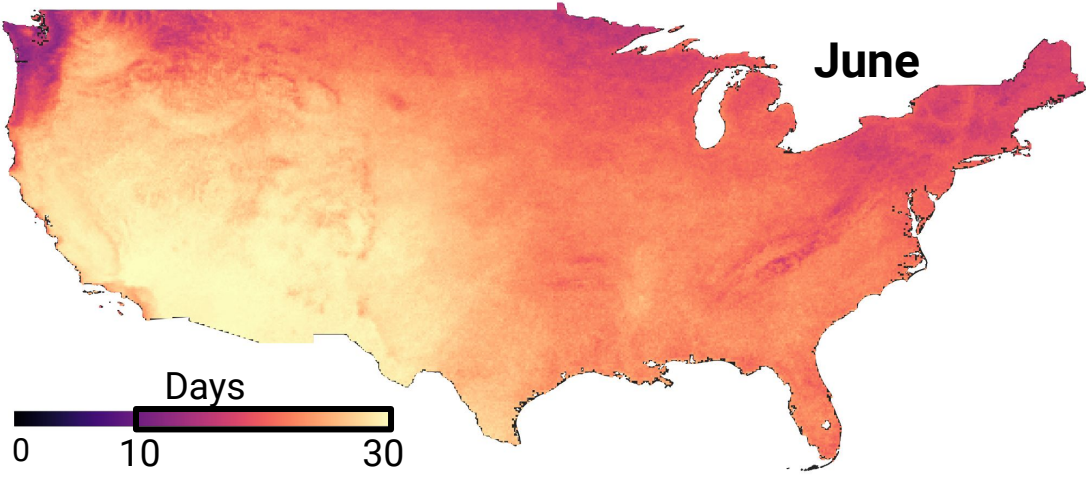


# Solar Powered Cruise Throughout US

- Designed for use in 5 months with highest solar radiation
  - **April to August**
  - **June** has the highest solar flux - *graph next slide*
  - Rest of year → solar radiation too low for reasonable wing area
- Designed for **800 W/m<sup>2</sup> solar flux**
  - Tradeoff between usability and mass budget
  - Can operate below 800 W/m<sup>2</sup>, but results in smaller range
- **Coverage throughout US** on clear days



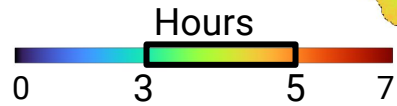
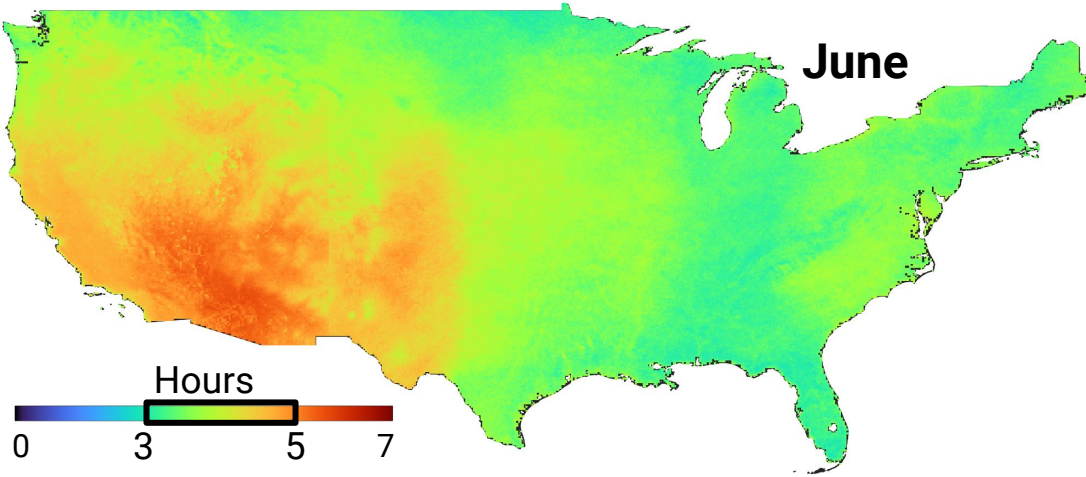
June



**Number of “clear” days:**

Average **number of days** where solar flux exceeds  $800 \text{ W/m}^2$  for any amount of time during a day

June

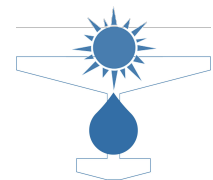


**Hours of “solar cruise”:**

Average **hours per day** exceeding  $800 \text{ W/m}^2$  on those days

drawing not to scale

Presenter: Lauren Carethers



# solar powered cruise flight

0' -



takeoff in ~1000 ft

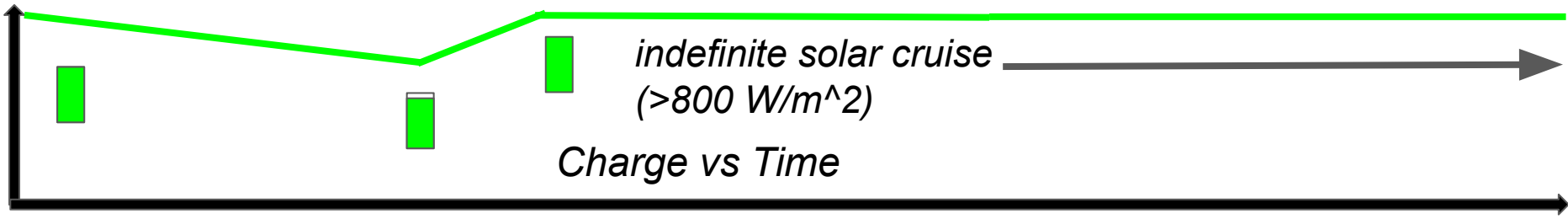


1% battery depleted during takeoff and climb to 50'. Next, slowly climb on excess solar

Charges on excess solar flux during cruise

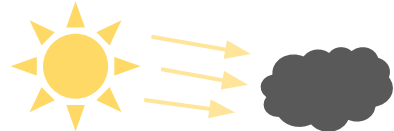
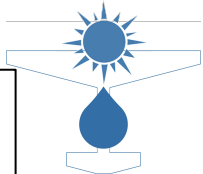


land in ~1000 ft

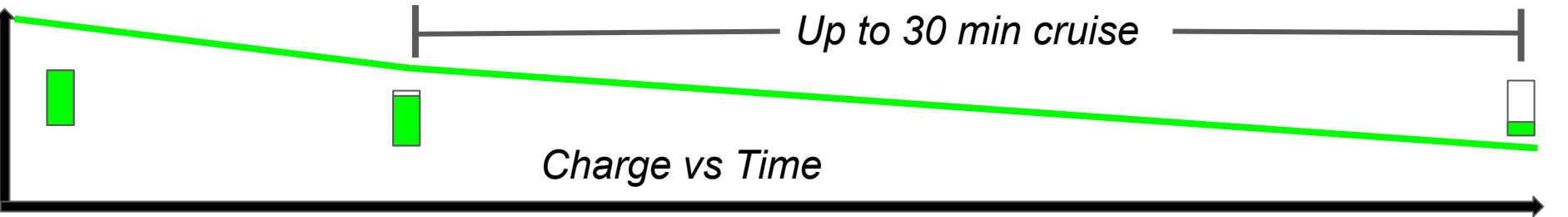
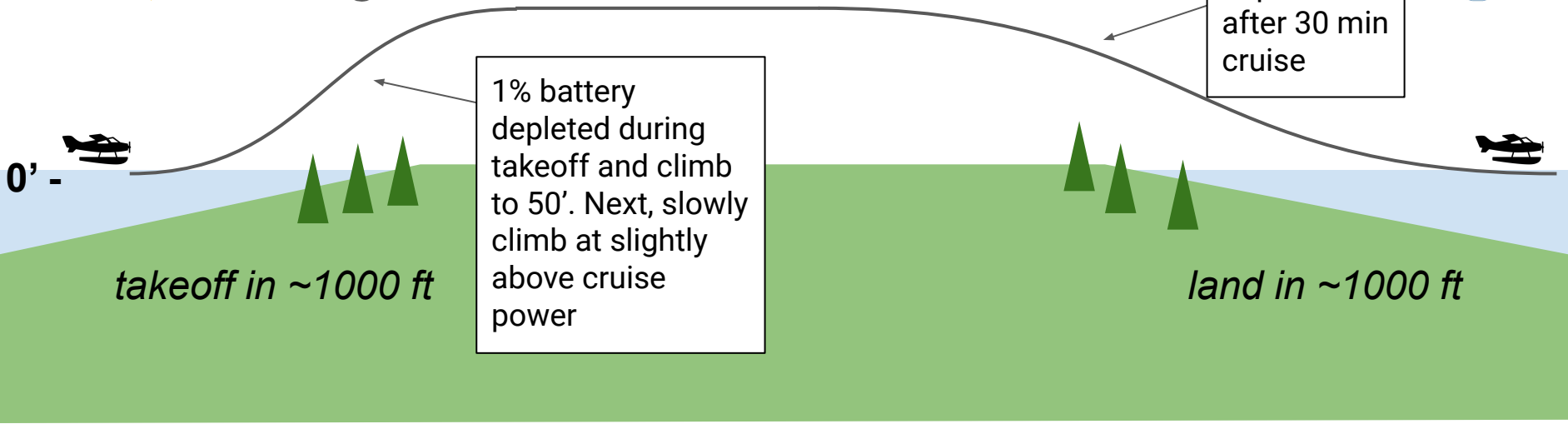


drawing not to scale

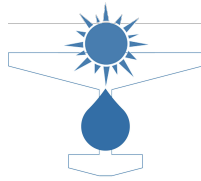
Presenter: Lauren Carethers



# battery powered backup cruise

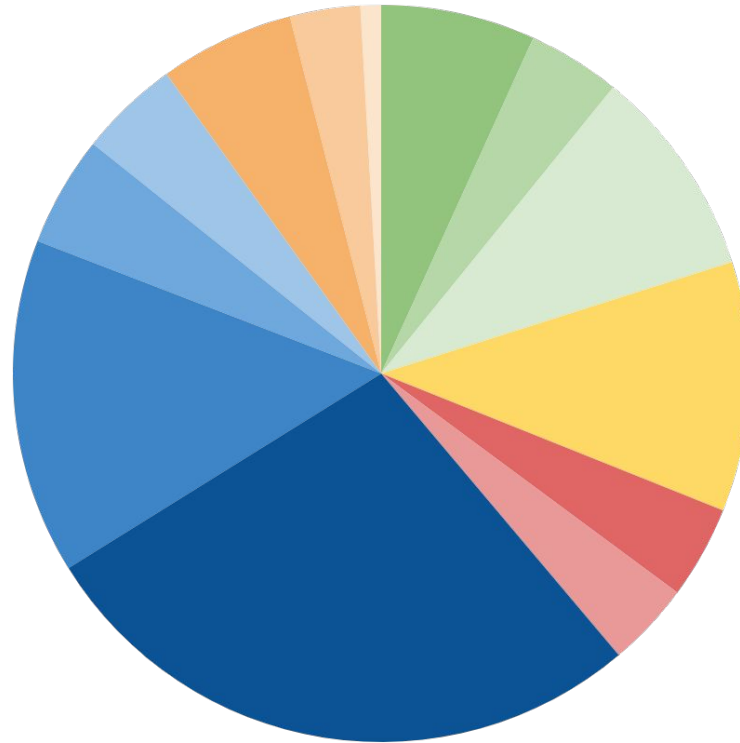






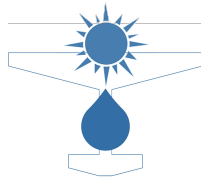
# Empty Weight Breakdown

- Current Empty Weight: 322 lbs
- Goal Weight (to be ultralight) 304
  - ❗ Currently 18 lbs overweight



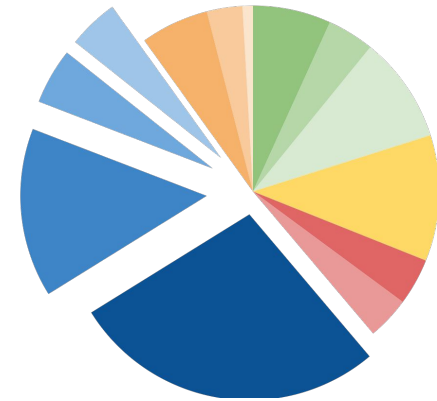
- Batteries
- MPPT
- Power Wiring
- Solar Panel (Total)
- Motors
- Propellers
- Main Wing
- Fuselage
- Floats
- Tail
- Sensors and Instruments
- Cockpit
- Control Wiring

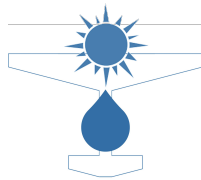
Color Key	
Cockpit and Controls	Electrical
Propulsion	Solar Panels
Key Structures	



# Structural Mass Budget

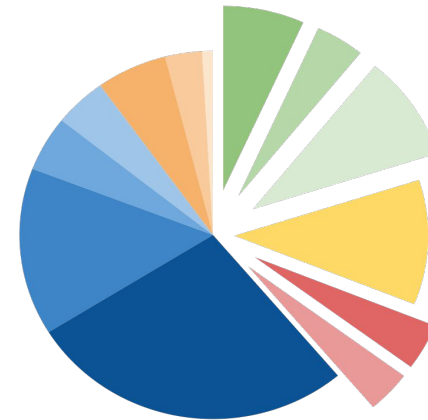
Part	Weight [lbs]	Sizing Case	
Main Wing	88.6	Bending, torsional stiffness	
Fuselage	47.7	Hydrodynamic drag, buoyancy	
Floats/Pylons	15.7	Water stability at rest	
Tail	14.2	Bending, some torsion	
<b>TOTAL</b>	<b>166.2</b>	51.3% of empty weight	

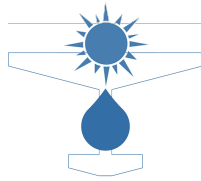




# Propulsive and Electrical Mass Budget

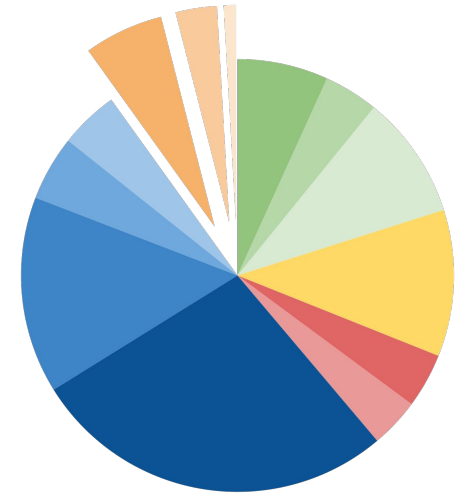
Part	Weight [lbs]	Source	
Solar Cells	19.6	Part sourcing	Yellow
Solar Protective Coating (Halar <sup>®</sup> ECTFE)	9.7	Halar <sup>®</sup> ECTFE density & coating volume	Yellow
Adhesive/Glue	6	Estimated glue area and density	Yellow
Wiring	30	Est. wire size and length	Light Green
MPPT	13.2	Part sourcing	Light Green
Battery Packs	22	Part sourcing	Light Green
Propellers	12	Size and material considerations	Red
Motors	13.2	Part sourcing	Red
<b>TOTAL</b>	<b>125.7</b>	<b>38.8% of empty weight</b>	

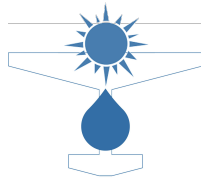




# Other Systems Mass Budget & Margins

Part	Weight [lbs]	Source	
Sensors	9.7	Avionics Architecture	
Instruments	9.5	Avionics Architecture	
Cockpit	10	Estimate from COTS parts	
Control Cables	1.2	COTS Wires, Pulleys, etc.	
<b>TOTAL</b>	<b>30.5</b>	9.9% of empty weight	

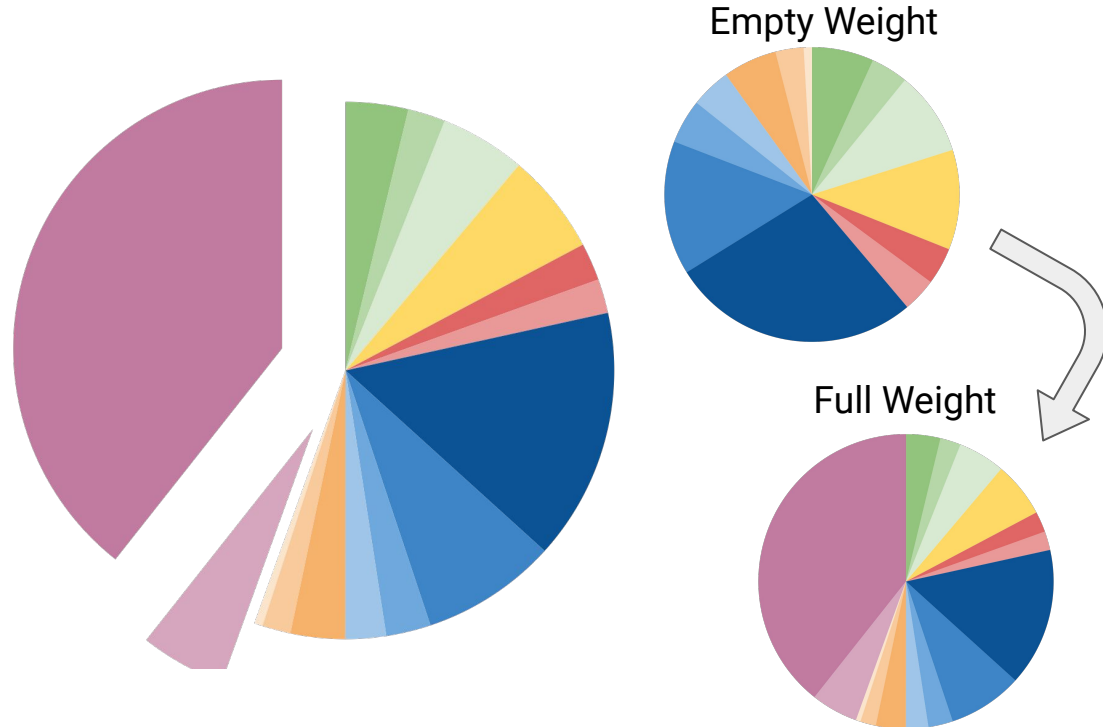


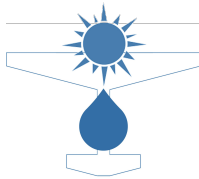


# Payload Weight Contribution

Item	Weight [lbs]	
Pilot Max	230	
Baggage Max	30	
<b>TOTAL</b>	<b>260</b>	

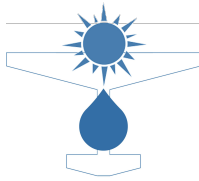
- Total Weight: 582 lbs
- At max payload, payload contributes 44.5% of weight
- Challenge for stability for different pilot weights





# Outline

1. Motivation
2. General Overview
3. **Subsystem Design**
  - a. Wing
  - b. Fuselage
  - c. Stabilizers
  - d. Propulsion
  - e. Human-Machine Interface
4. Risk
5. Conclusion



# Outline

## 3. Subsystem Design

### a. **Wing**

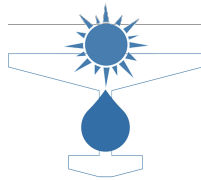
- i. Aerodynamics
- ii. Solar Cells
- iii. Structural Components

### b. Fuselage

### c. Stabilizers

### d. Propulsion

### e. Human-Machine Interface



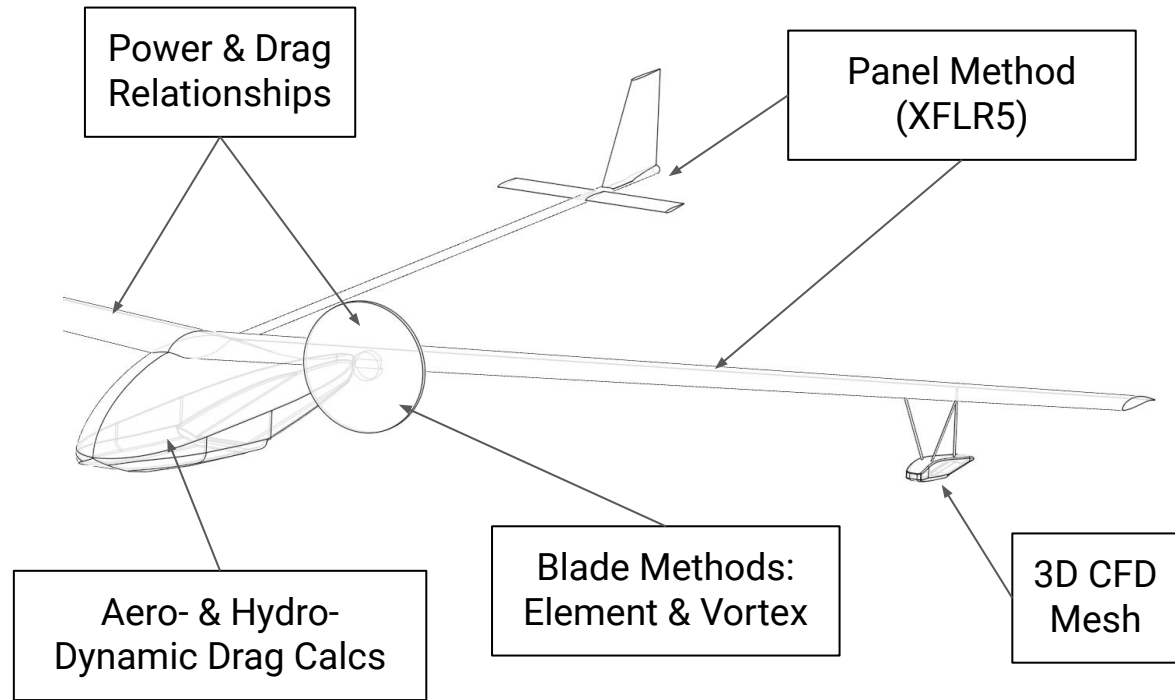
# Modeling Overview

## Assumptions:

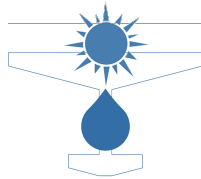
- Viscous flow estimated via panel method within order of magnitude
- Bodies & Aero Surfaces have no interacting effects

## Compensations:

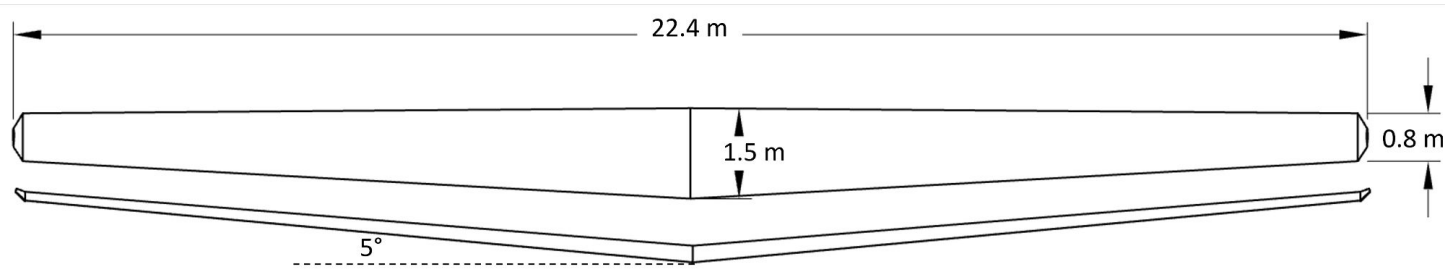
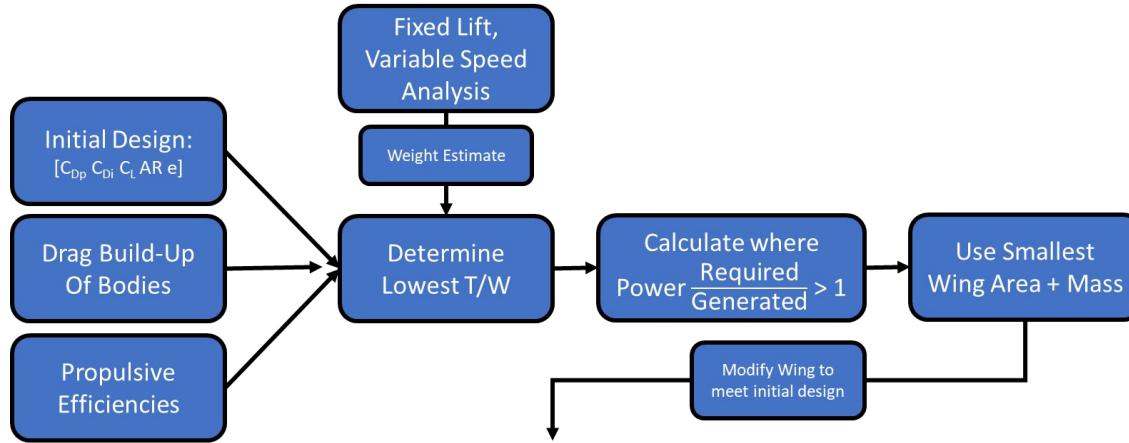
- 5% drag margin
- Meaningful analysis limited to small angles



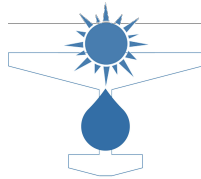




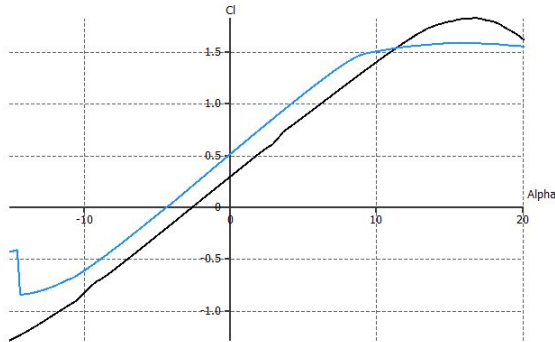
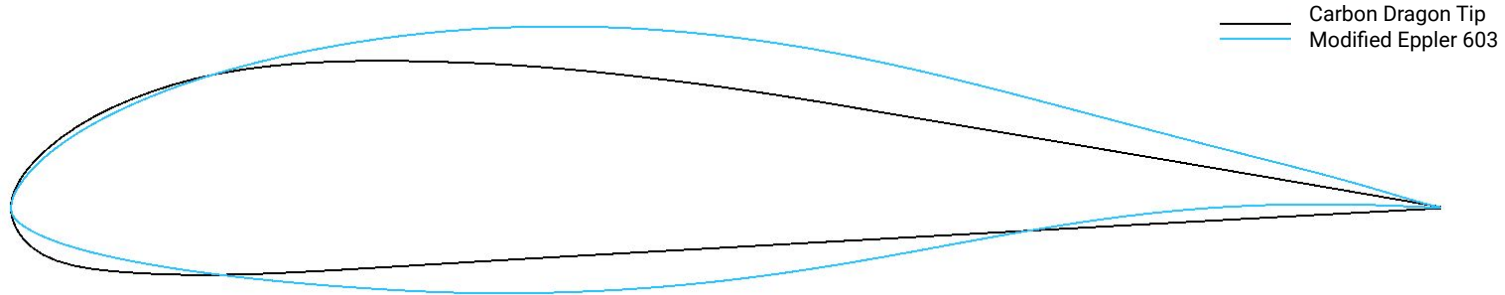
# Wing Powered by the Sun



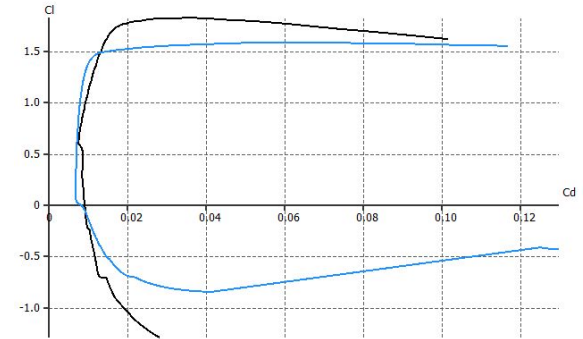
Reynolds #	1,300,000
L/D	25.7
AR	19.5
e	.8
Wing Loading	97 Pa
Thrust <sub>cruise</sub>	195 N
P <sub>Required</sub>	3300 W
P <sub>Generated</sub>	3400 W

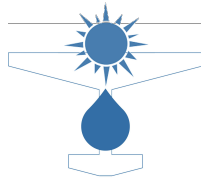


# 2D Aerodynamic Performance

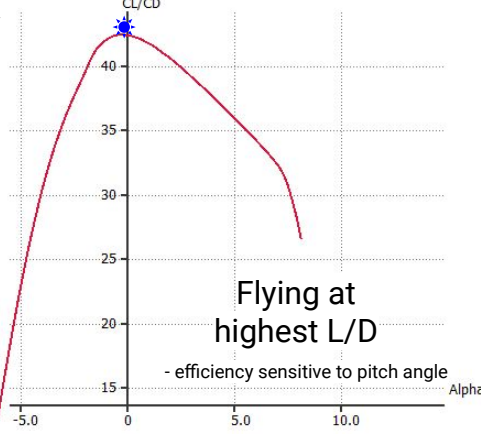
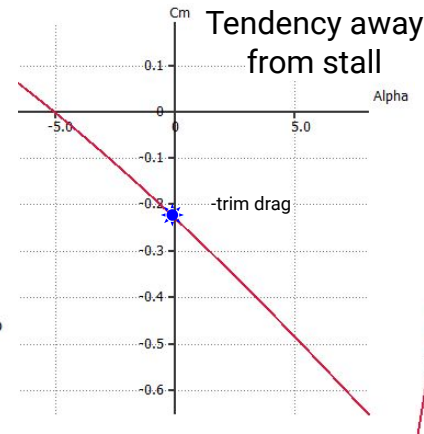
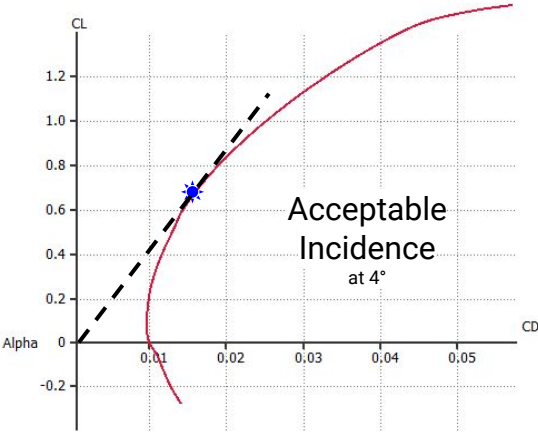
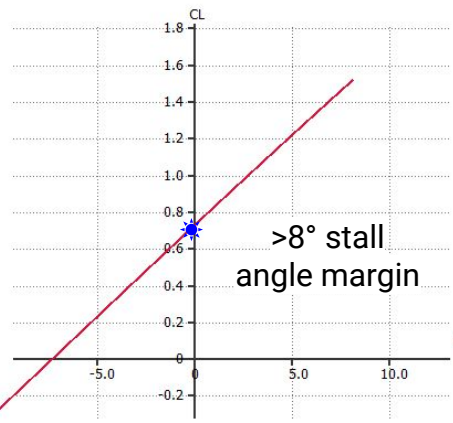
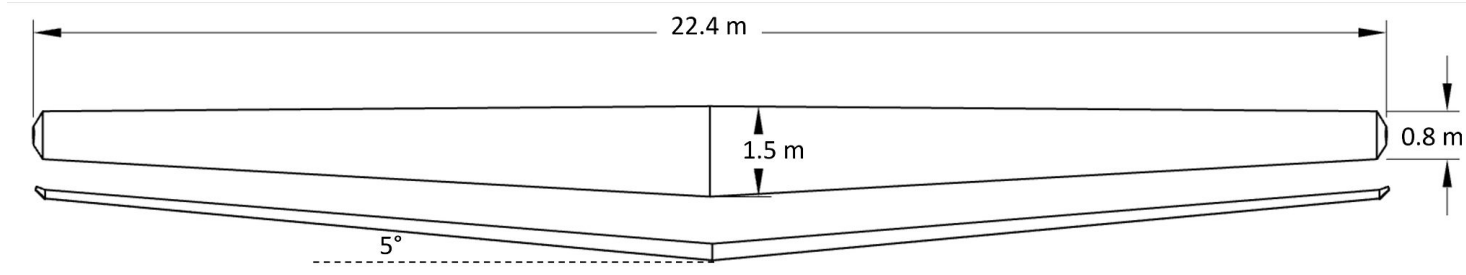


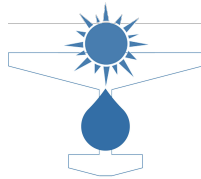
- Modified Eppler 603 at Root
- Carbon Dragon Tip Airfoil at Tip
  - Linear Interpolation
- Allows Aerodynamic Washout
  - No Twist
    - Easier solar panel mounting
    - Easier structures planning
- Adequate Low Reynolds # Performance





# 3D Aerodynamic Performance



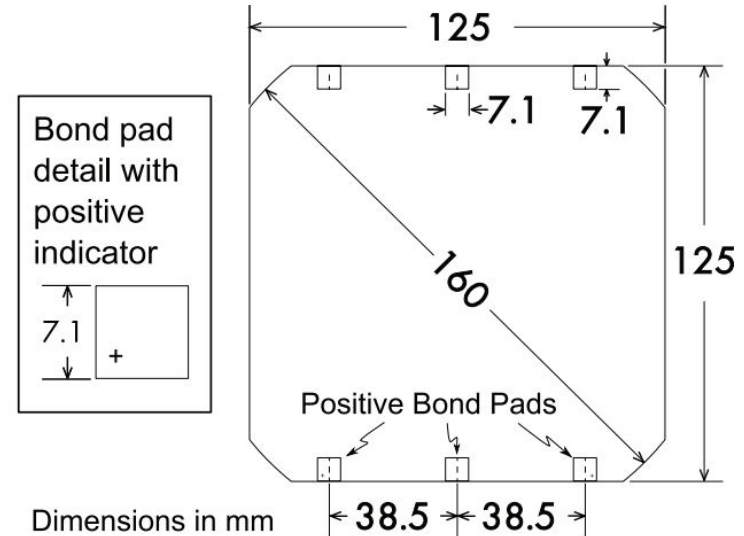


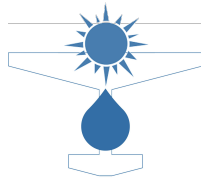
# Solar Cell Selection



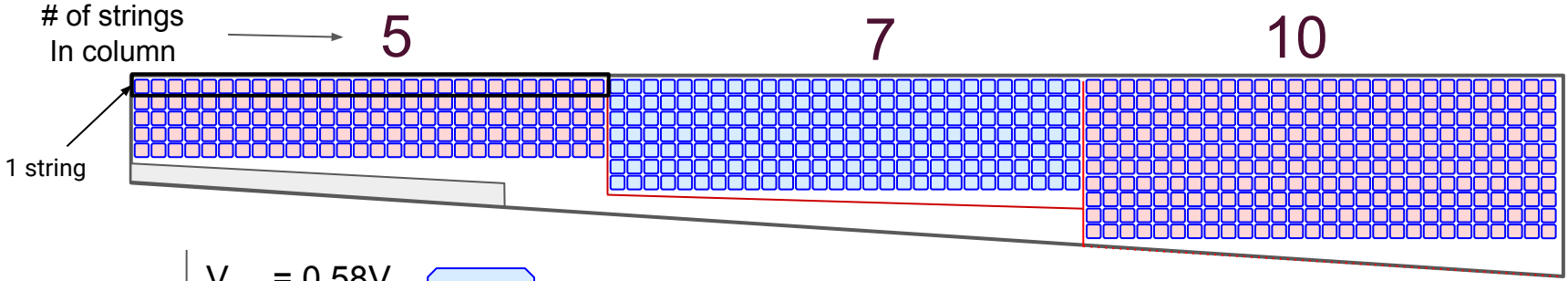
- SunPower C60 Solar Cell
- Commonly used in solar aviation
- Mono Crystalline Silicon
- Can be place anywhere on wing

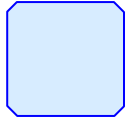

<b>Efficiency</b>	22.5
<b>Weight [lbs/cell]</b>	0.014
<b>Max Bend Angle</b>	30°
<b>Cost [\$/cell]</b>	3.4





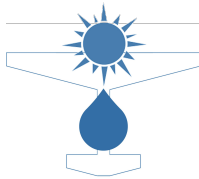
# Solar Cell Layout



1 Cell*	$V_{mpp} = 0.58V$ $I_{mpp} = 5.93A$		Total Area of Solar Cells = $19.25\text{ m}^2 \rightarrow 75\%$ of wing area 1232 cells on 1 wing $\rightarrow$ 2464 cells in total
1 String 28 Cells*	$V_{mpp} = 16.27V$ $I_{mpp} = 5.93A$		

1 Wing  
44 Strings\*\*  $P_{total, wings} = 3400W > 3300W$  Cruise Requirement

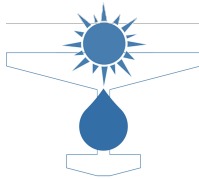
\* Electrical specifications tested at  $1000W/m^2$  flux  
 \*\*  $800W/m^2$  flux



# Solar Cell Protection

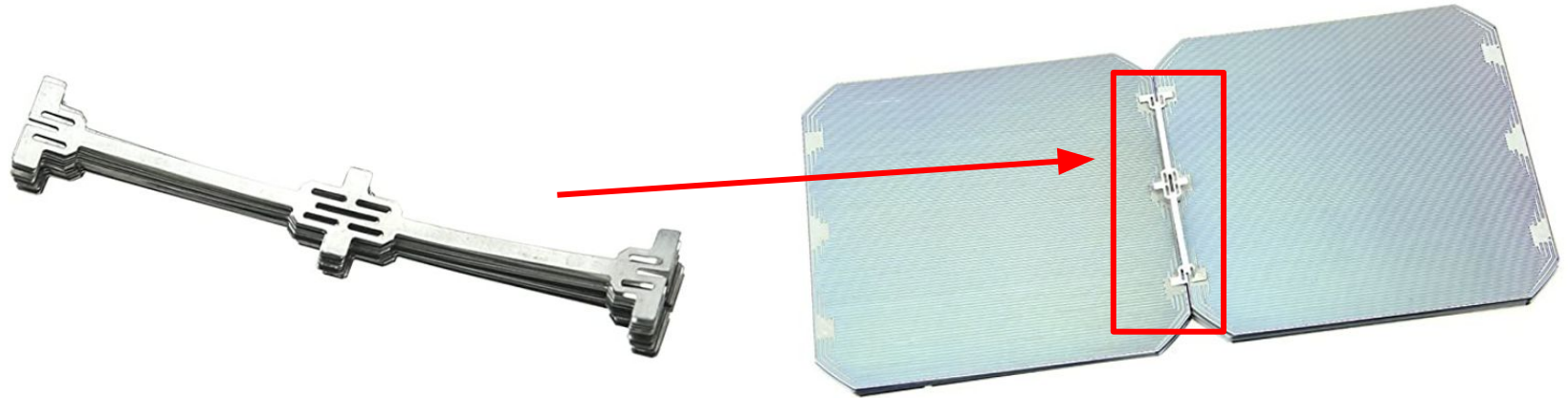
- Cover cells in a single layer of Halar® ECTFE
  - Semi-crystalline fluoropolymer
  - Used on Solar Impulse 2
  - Strong, smooth and transparent
  - Abrasion and chemical resistant
  - Excellent weathering properties
  - Low permeability → protects against various liquids and gases
- Smooth finish reduces drag across panels

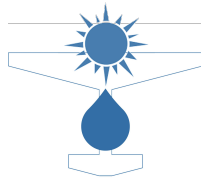




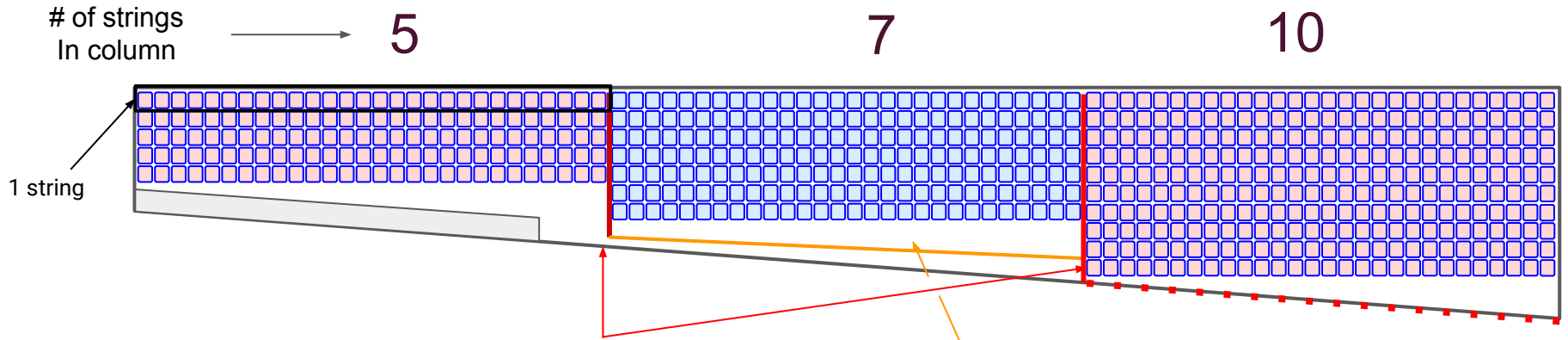
# Solar Cell Attachment

- Flexible solar cells attach to the wing fabric with Sikaflex<sup>®</sup>-221 glue
- Solar cells connected **in series** via SunPower C60 Dog Bone Tabbing Wire Connector





# Solar Cell Attachment



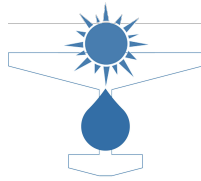
Connections that unite strings **in parallel**

- 2 connectors per wing, 1 on fuselage

Connection between 2 connectors

Connection runs under trailing edge to MPPT



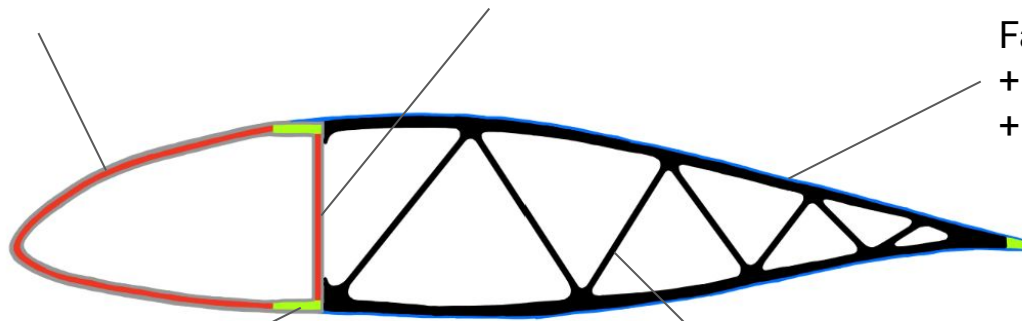


# Structural Components of the Main Wing

D-Box sizing determined by torsional stiffness

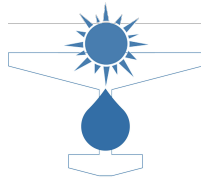
Shear web integrated in D-Box

Fabric wing skin  
+ solar cells  
+ protective film



Spar cap sizing determined by wing bending limit

Carbon fiber ribs

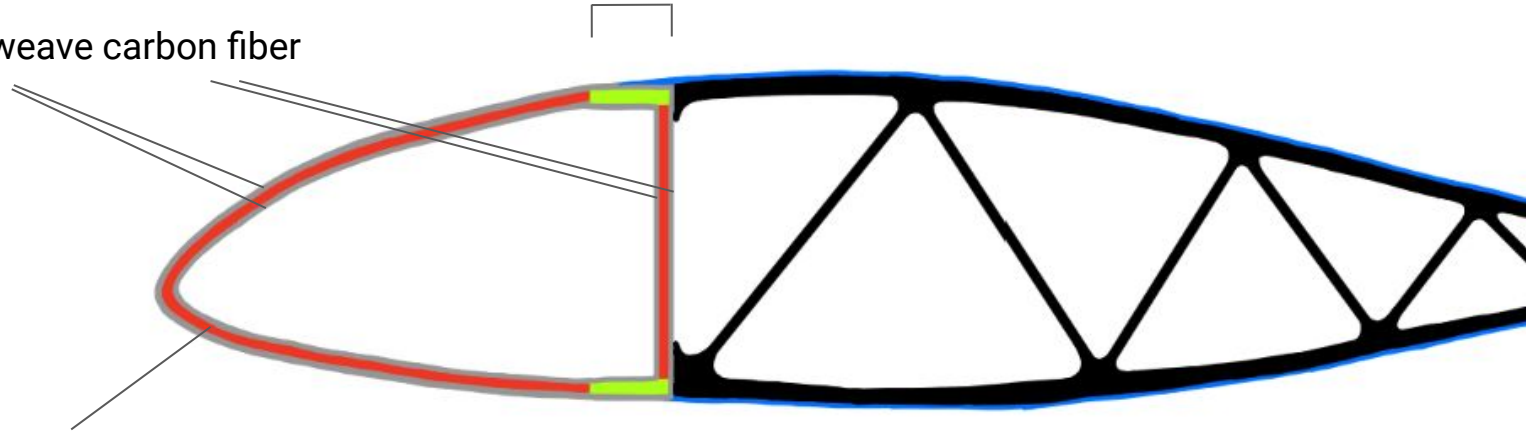


# Sizing Results

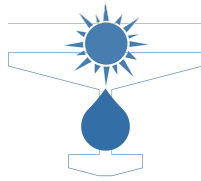
Spar Cap  
2.25 inches wide, 0.24 inches thick  
Carbon fiber

Single ply 45/45 weave carbon fiber

0.12 inches (3mm) closed-cell foam core



\* thicknesses not to scale



# Sizing Requirements Dominated by Stiffness

**D-Box** sized for torsional loads

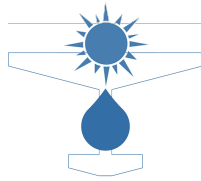
Sizing case: Max aileron deflection, tip twist limit of 2 degrees

Sized for both strength and stiffness → stiffness dominates sizing requirement

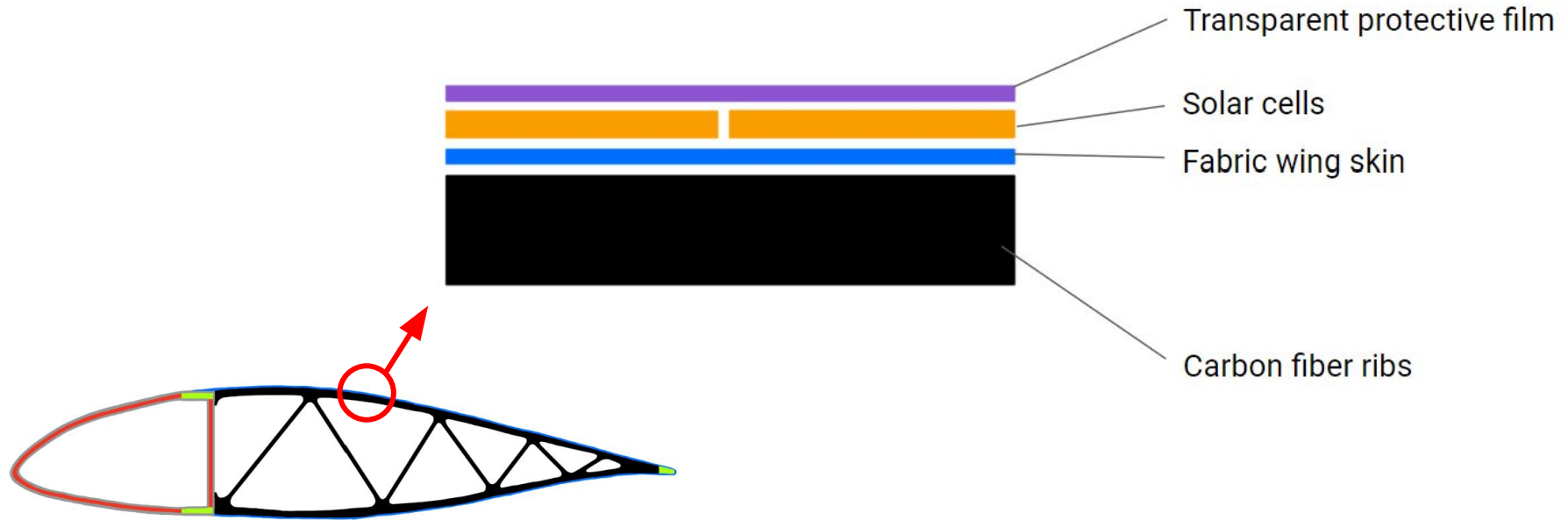
Result: **Gauge limited**

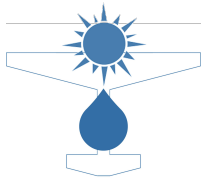
**Spar caps** sized to limit tip deflection to 6 degrees at a load factor of 4

**Shear web** is also gauge limited, therefore shear requirement is satisfied by the vertical side of the D-Box



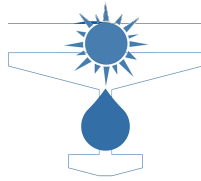
# Solar Cells Sandwiched in Wing Skin



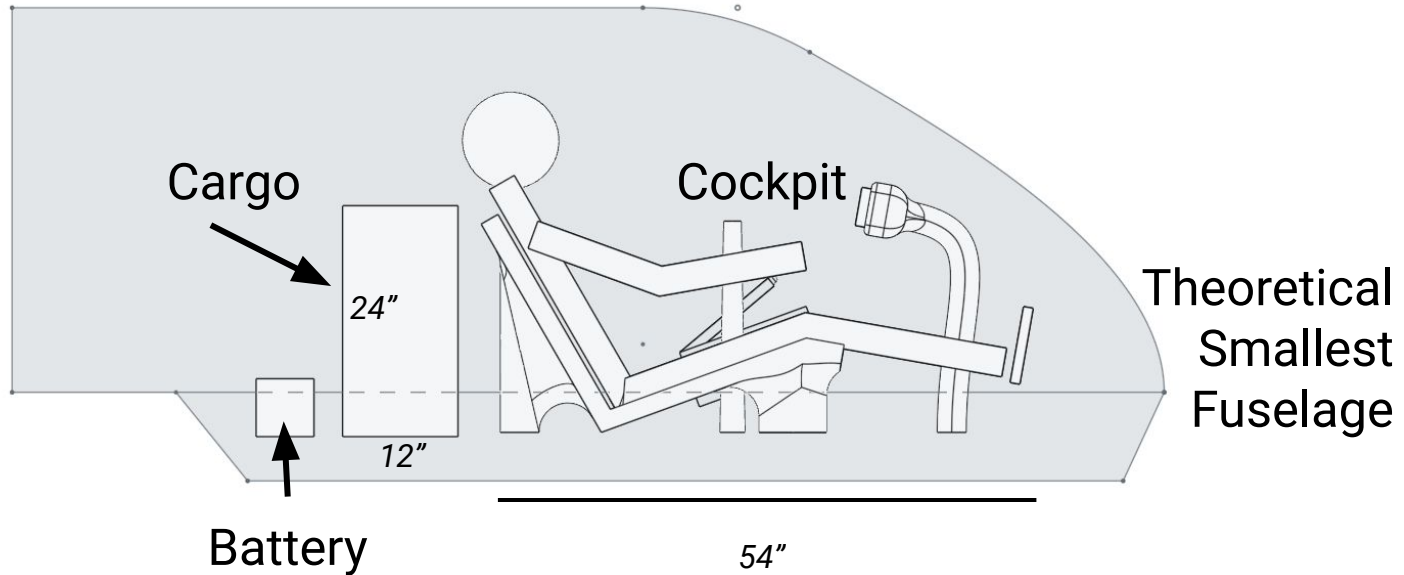


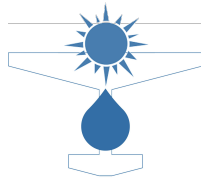
# Outline

3. Subsystem Design
  - a. Wing
  - b. Fuselage**
    - i. Shape & Design
    - ii. Structural Components
  - c. Stabilizers
  - d. Propulsion
  - e. Human-Machine Interface

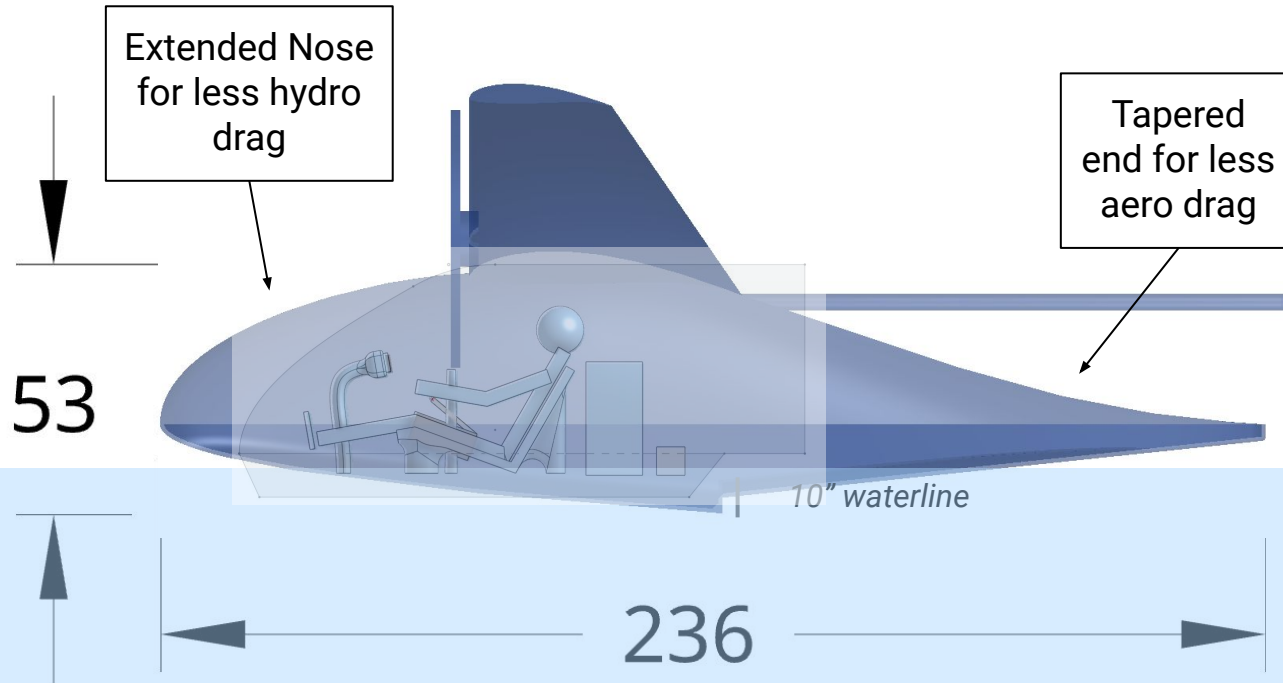


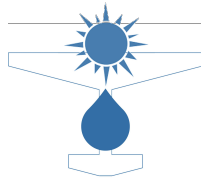
# Fuselage Sized by Payloads



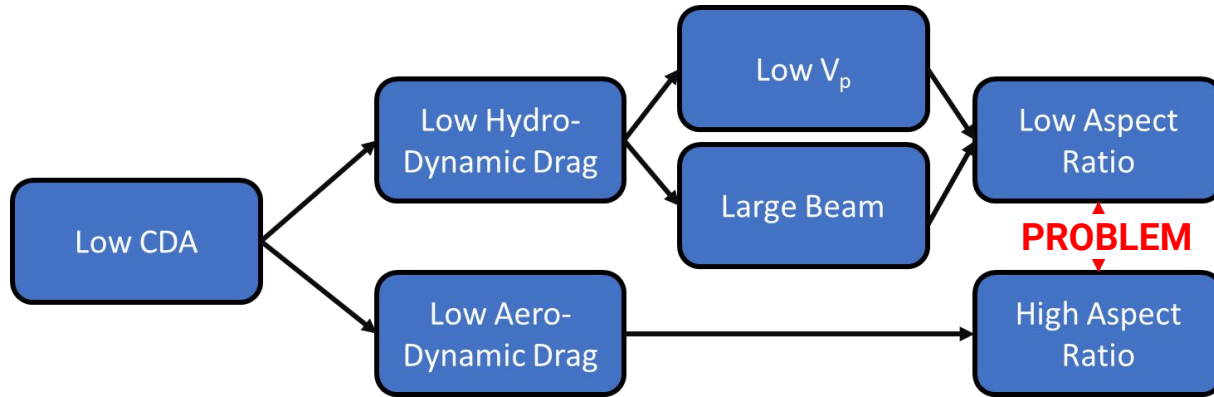
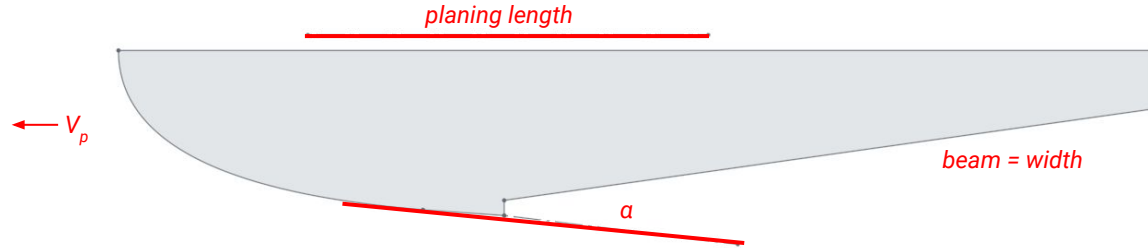


# Meet the Fuselage

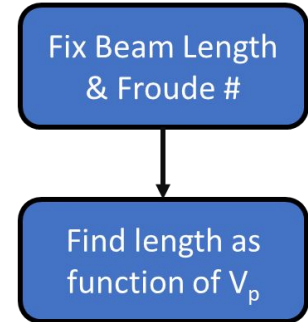




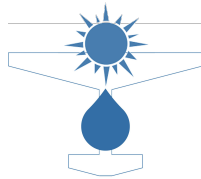
# Hull: How to Compromise on Drag



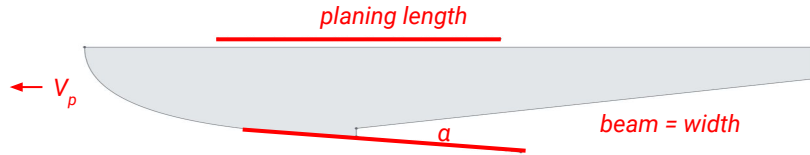
Can Compromise by:



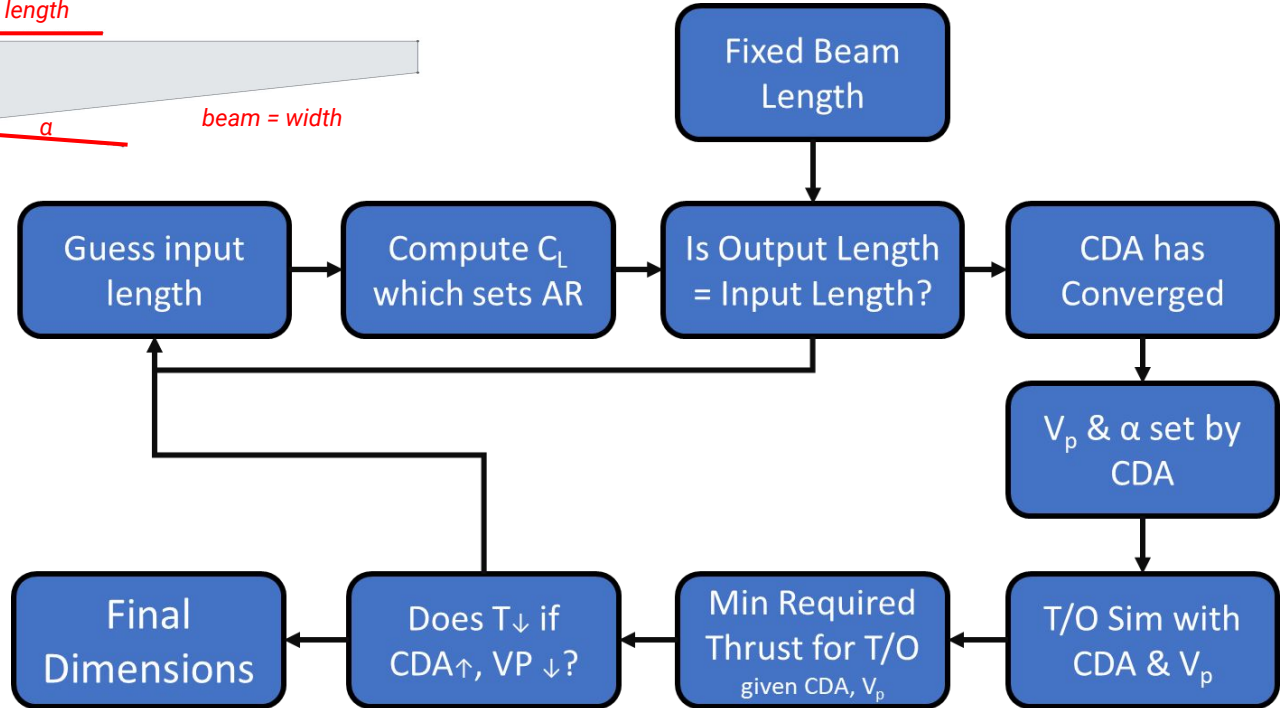


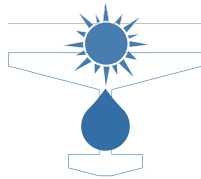


# Hull: The Drag Loop



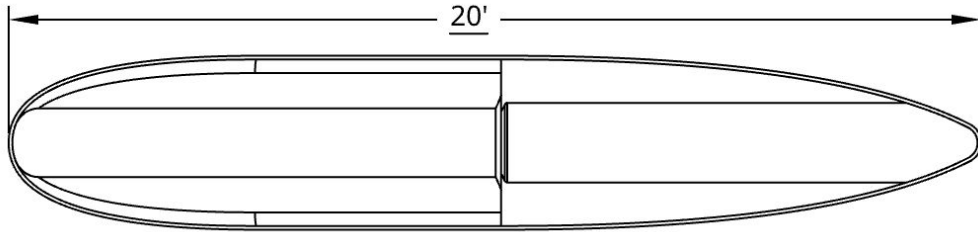
Converged Dimensions	
Trim angle, $\alpha$	4 degrees
Planing Length	10'
Beam Length	3.5'
$Fr_{min}$	1.5
$V_{planing}$	16 knots
$CDA_{planing}$	0.006 m <sup>2</sup>



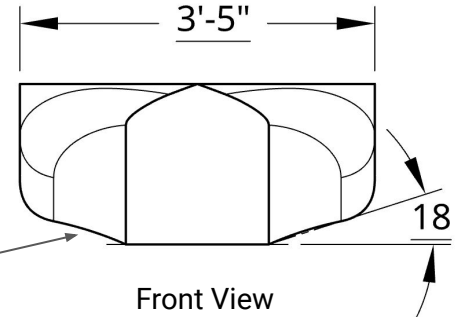
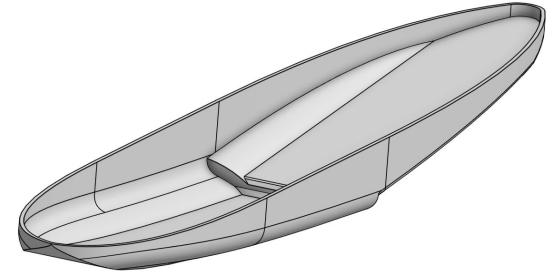
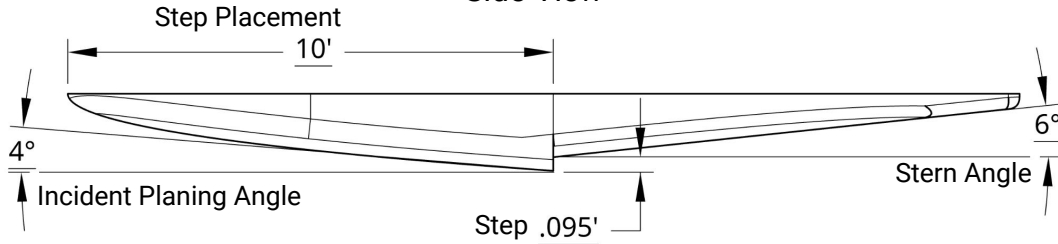


# Determined Planing Hull Geometry

Top view

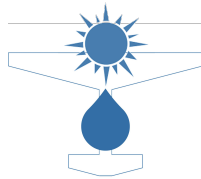


Side View

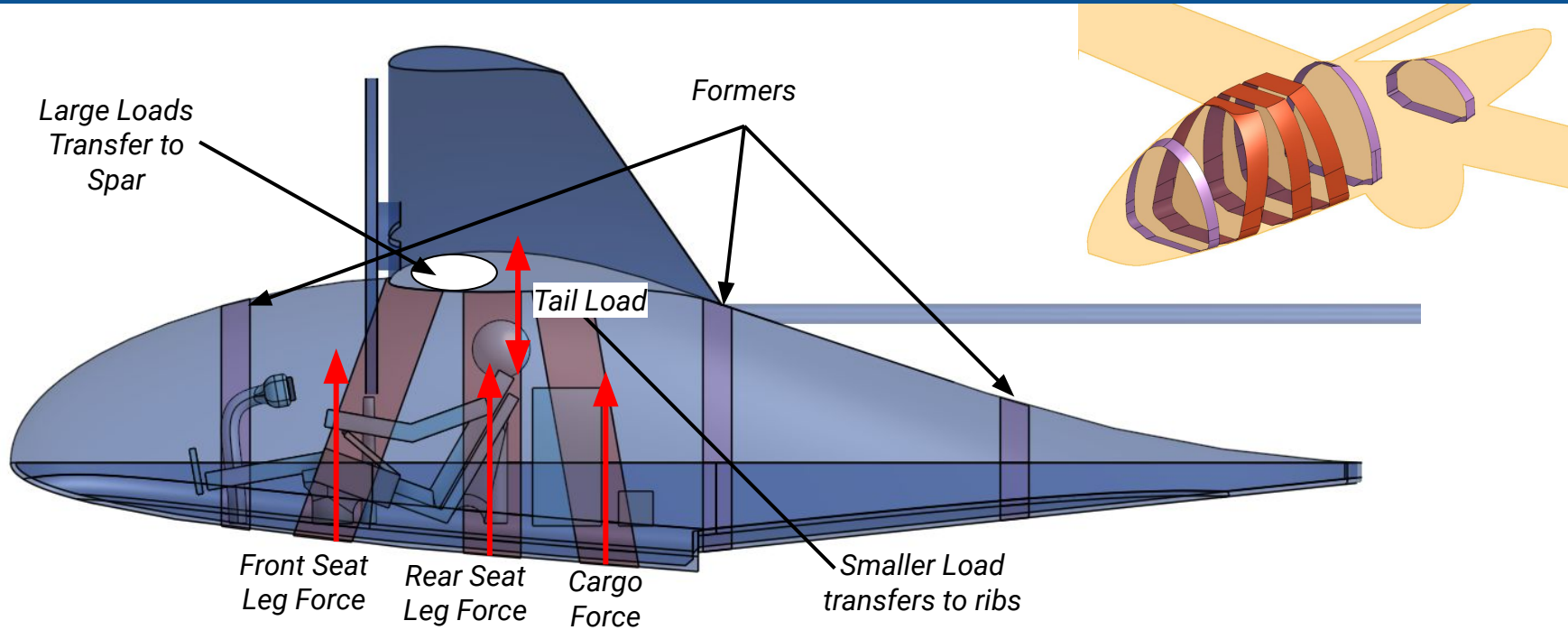


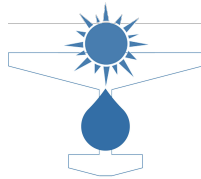
Flared Deadrise

Front View



# Bulkheads Positioned by Load Pathing





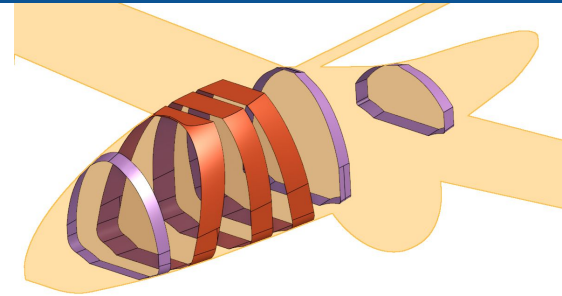
# Fuselage Structure Sized by Landing


- Recommended sizing from 14 CFR 25.527
  - Solving gives us 1.61x load factor
  - Minimum from same regulation is 2.33x
- Going with 2.5x gives us >1.5x safety factor

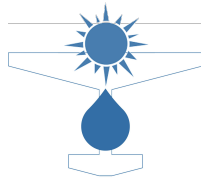
$$n_w = \frac{C_1 V_{s0}^2}{\left( \tan^{\frac{2}{3}} \beta \right) W^{\frac{1}{3}}}$$

**2.5G = 2550 N Load**

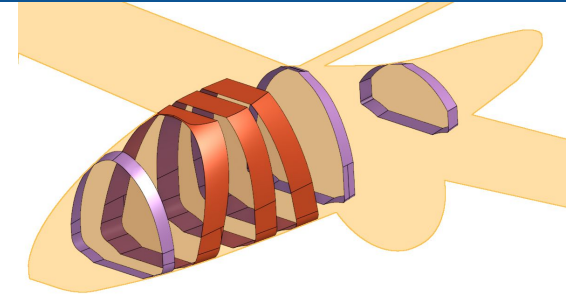
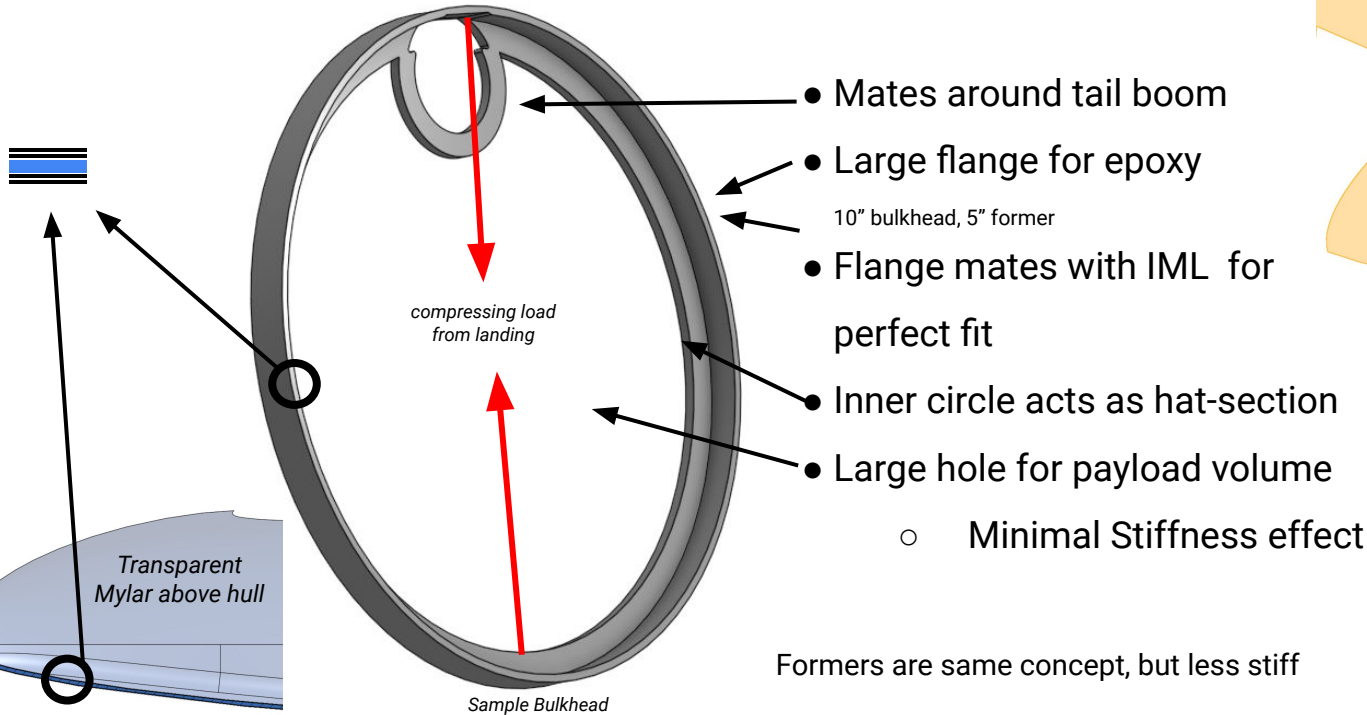
- Each bulkhead takes 191 lbs of weight
  - Most pilots can step on bulkheads as they step in
    - Preliminary: structures made of same cross-section as spar <sup>^</sup>



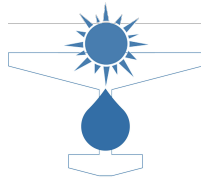

 2x Carbon  
 plies per side  
 1" foam core



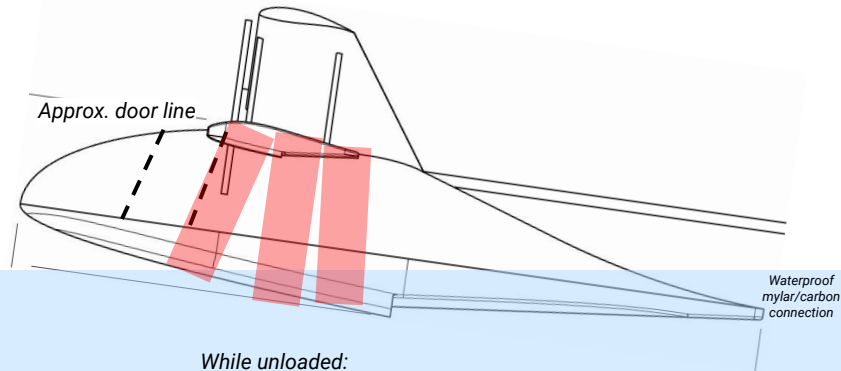
# Hull & Bulkhead Cross-Section



Estimated Weights (lbs)	
3x Bulkheads	10
3x Formers	5
Hull	15
Mylar Covering	3
total	33

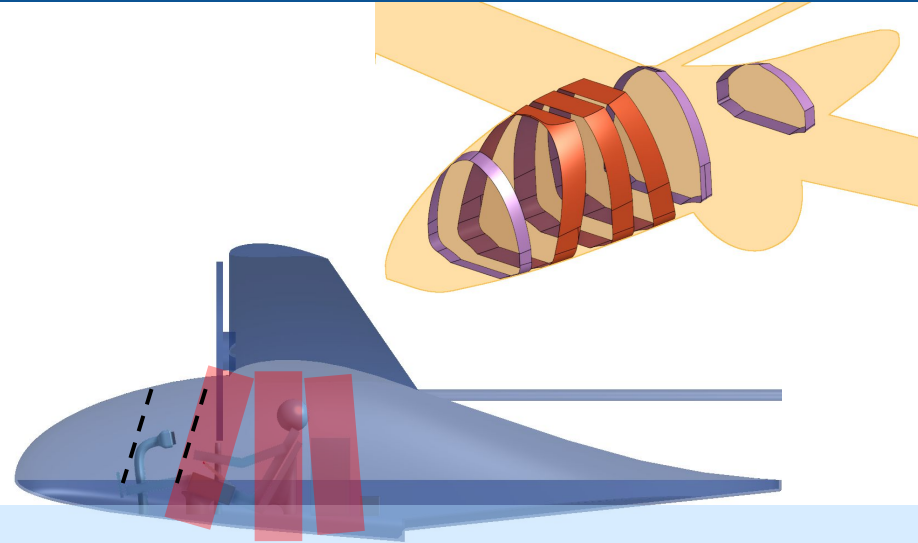


# Stepping into the Fuselage



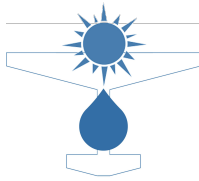
*While unloaded:*

- Plane rests on tail (8°)
- Door doesn't interfere with bulkheads
- Pilot steps on front bulkhead **slowly**
- Enough room for pilot to pivot around, sit, and extend legs to pedals



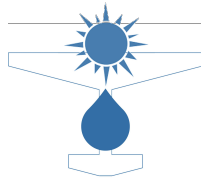
*While loaded:*

- Plane rests on hull (0°)
- Mylar door is closed (zipped or velcro'd)
- If cargo, pilot set inside before stepping in
- To leave: pilot steps on bulkhead, **slowly** steps out, letting plane rest on tail

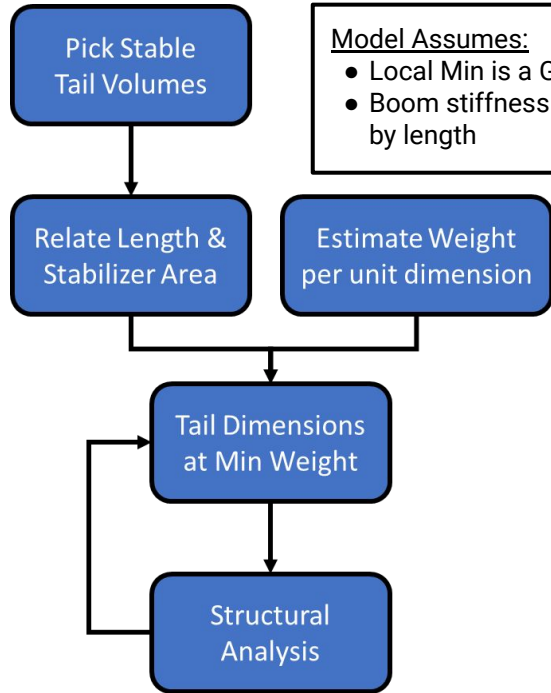


# Outline

3. Subsystem Design
  - a. Wing
  - b. Fuselage
  - c. **Stabilizers**
    - i. Empennage
    - ii. Ailerons
    - iii. Elevator
    - iv. Rudder
    - v. Pylons
  - d. Propulsion
  - e. Human-Machine Interface



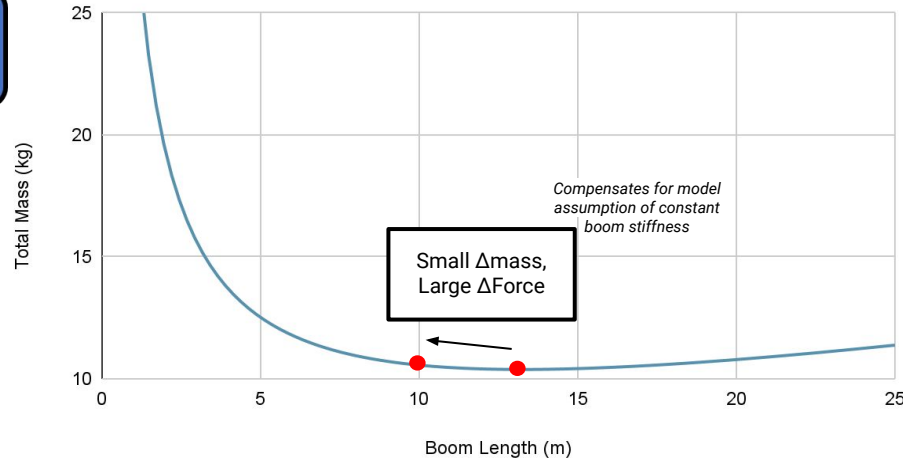
# Tail Size Dominated by Minimizing Weight



**Model Assumes:**

- Local Min is a Global Min
- Boom stiffness constant by length

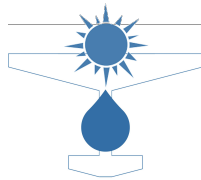
Mass of Boom & Tails vs Boom Length



Final Dimensions

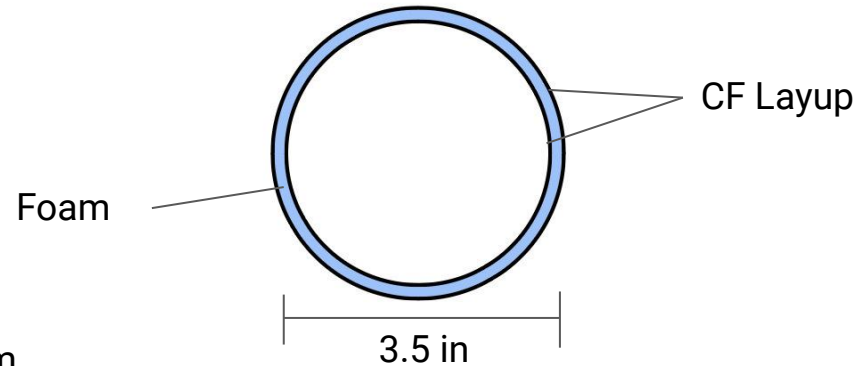
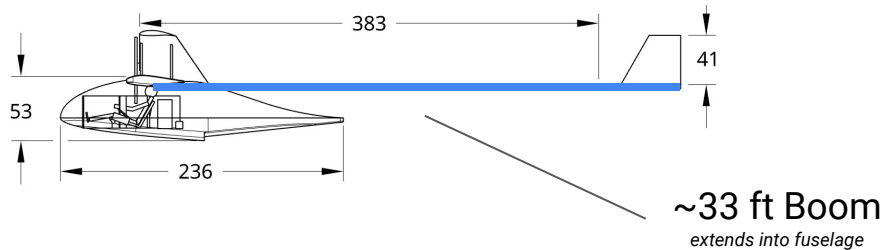
Boom Length	10 m
H-Stab Area	0.82 m <sup>2</sup>
H-Stab Mass	4.66 kg
V-Stab Area	1.05 m <sup>2</sup>
V-Stab Mass	3.9 kg

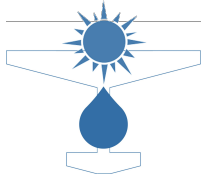




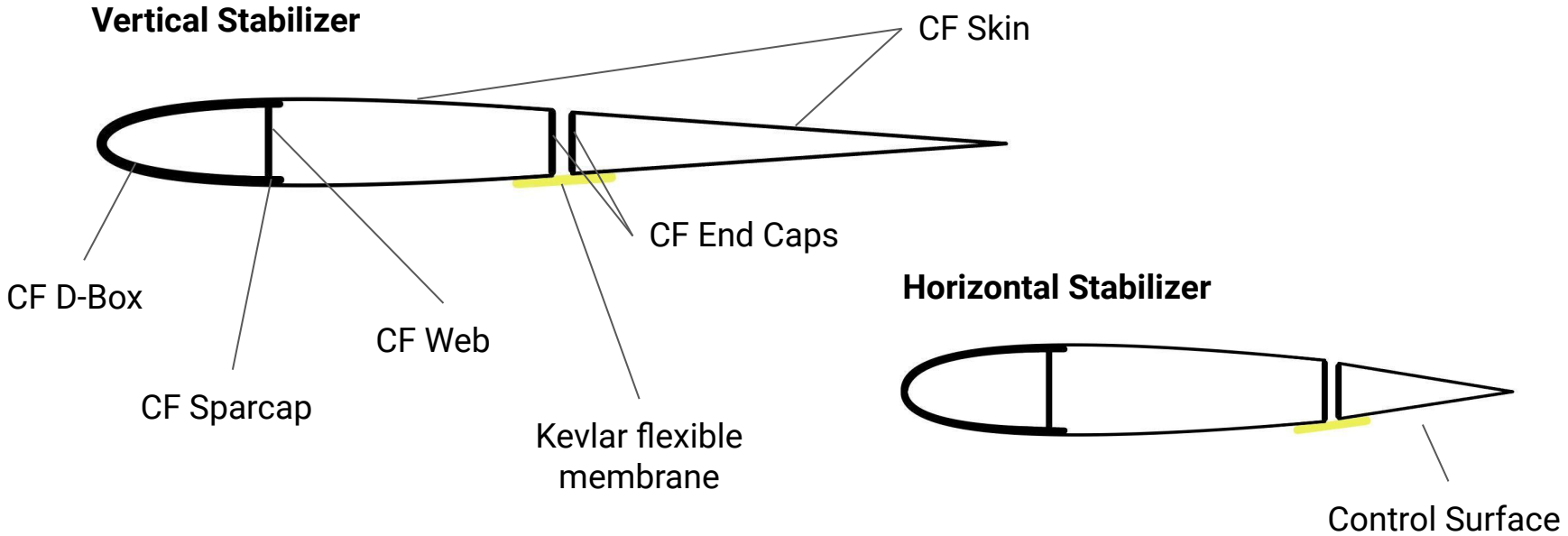
# Boom Is Carbon Fiber Composite Sandwich Tube

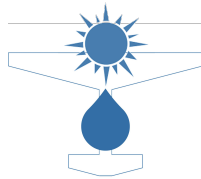
- Tube chosen for its good bending and torsional resistance
  - Bending deflection in z-axis is primary sizing case (lift and weight)
  - Torsion considered for rough landing
- 1 layer CF + thin layer of foam + 1 layer CF
  - Prevent ovalization or denting
  - Relatively lightweight



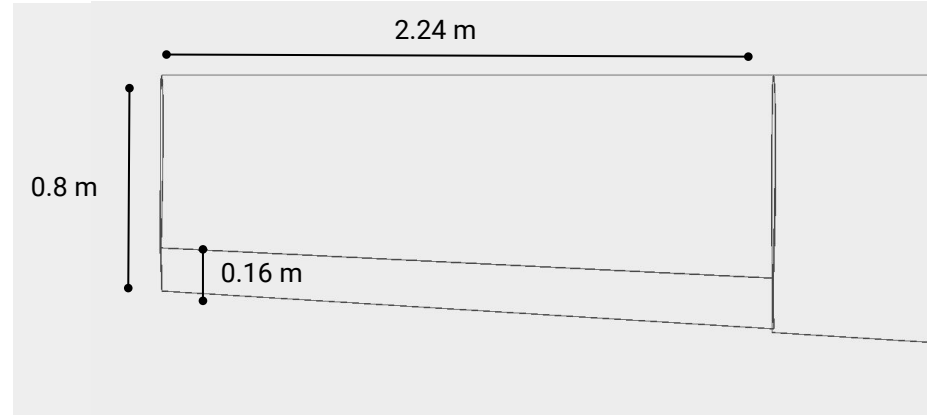
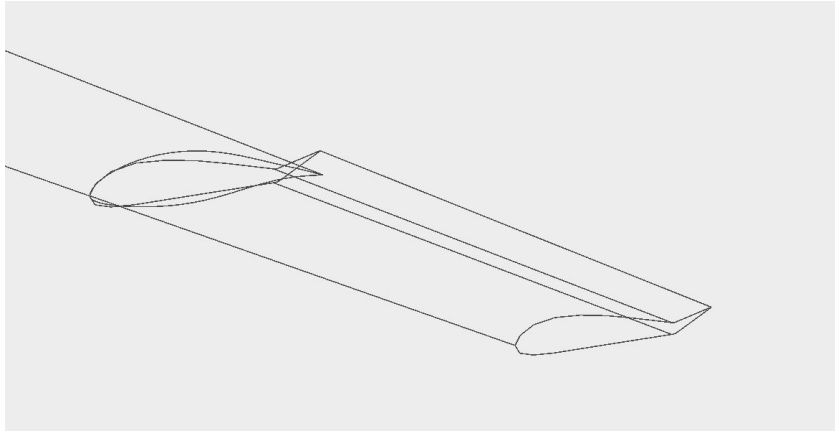


# Structure of Stabilizers is **Carbon Fiber Shell**

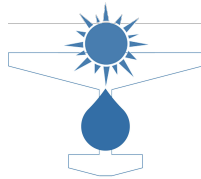




# Aileron - Geometry

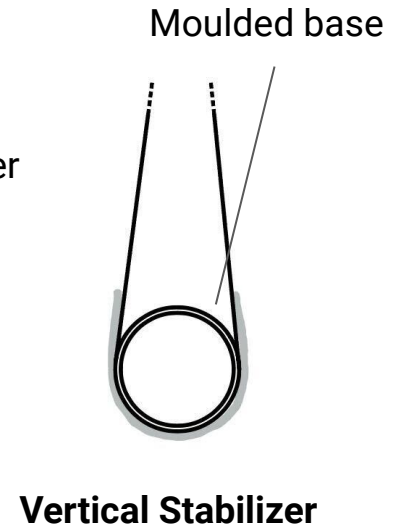
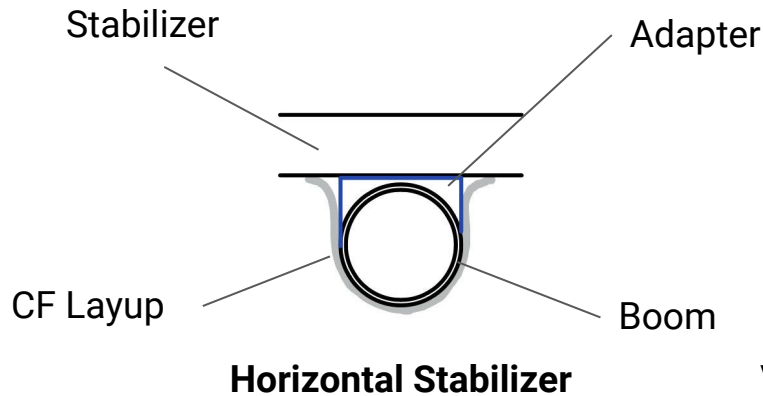
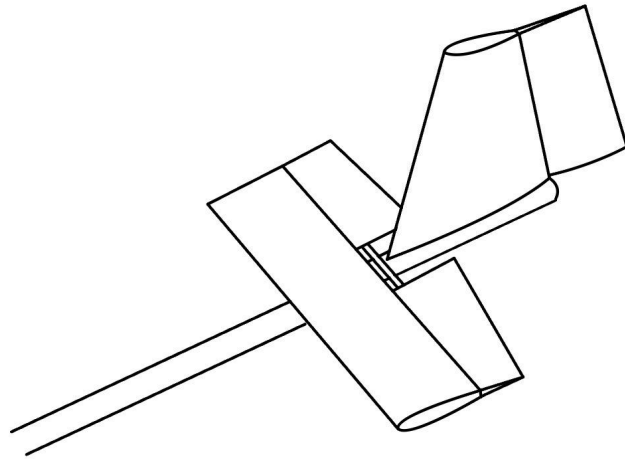


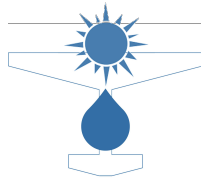
20% root chord, 20% semispan from tip, max deflection 25°



# Stabilizer Mounting Configuration

- Saves overall weight, is structural and constructable
- Foam adapters interface stabilizer with boom tube
- Unidirectional CF layup for strength



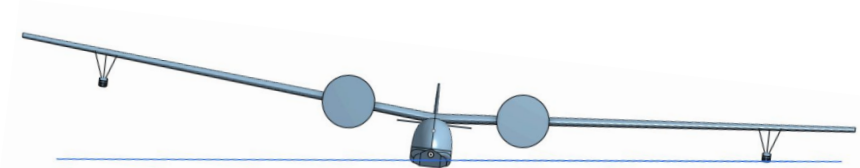


# Pylon + Floats

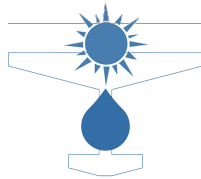
- Float placement constraints
  - Propeller clearance from waves at rest (>18in)
  - Float clearance during landing (>18in)
- Floats attached to wing with pylon structures made from symmetric airfoil shaped carbon fiber tubes
- Ultimate constraint for placement of floats is maximizing distance from waterline on landing



Configuration when flat in water/airborne

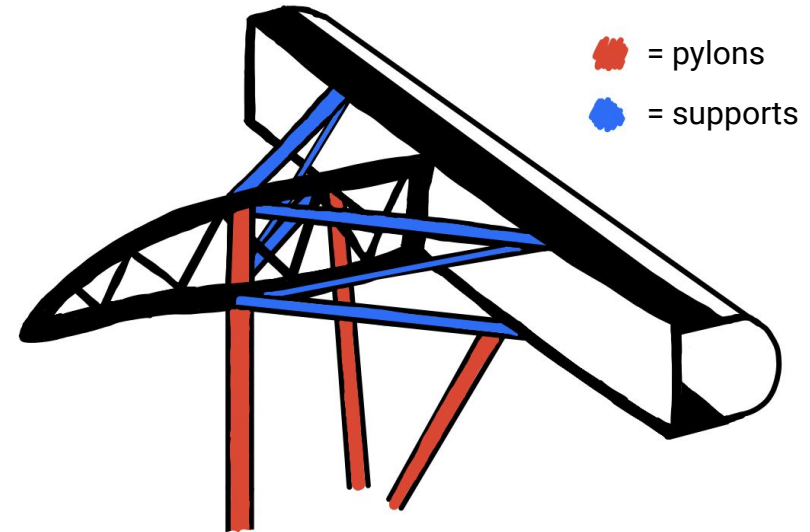


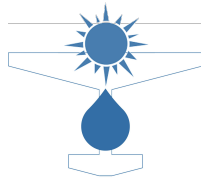
Configuration when resting on floats



# Pylon Connection

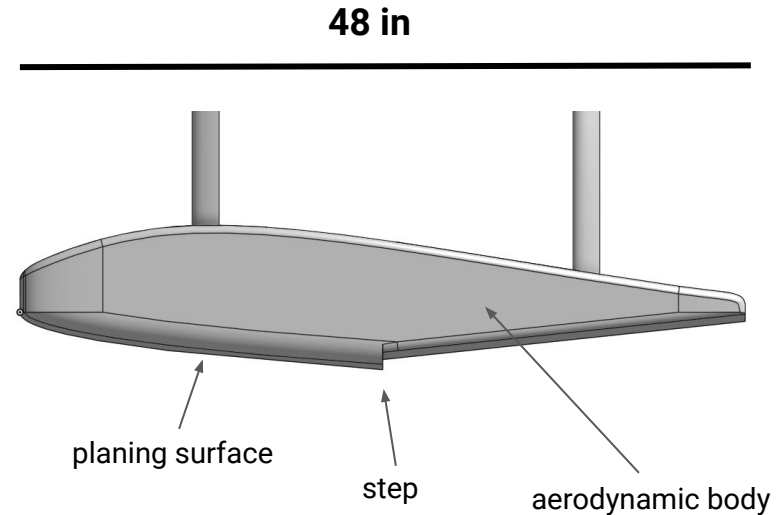
- Two front pylons are connected to the spar
- Back pylon connects to a reinforced CF rib
  - Rib is reinforced and attached to the spar with supports so the float assembly can withstand hard landings
- Molded inverted-wingtip design not possible due to wing structure

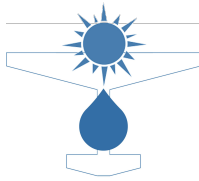




# Float Sizing and Shaping

- Floats were sized to correct for 15 mph winds when at rest and support the weight of the wing
  - Provide roll-axis stability in water
  - Designed to provide 1.5x needed moment for safety margin
- **Required Volume (per float) > 2.35 ft<sup>3</sup>**
- Floats have a planing surface and step to reduce hydrodynamic drag and encourage separation from the water

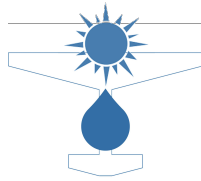




# Outline

3. Subsystem Design
  - a. Wing
  - b. Fuselage
  - c. Stabilizers
  - d. Propulsion**
    - i. Propulsion Requirements
    - ii. Propeller
    - iii. Motor
    - iv. Battery
    - v. MPPT
  - e. Human-Machine Interface

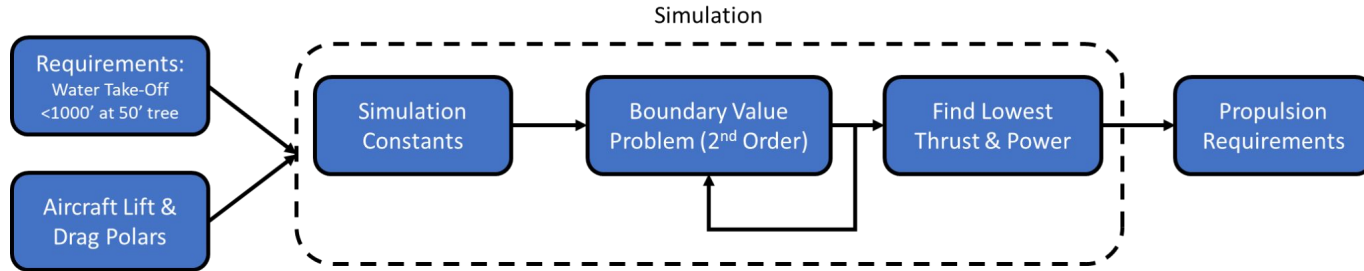


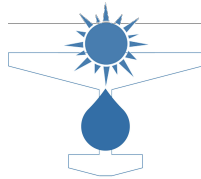


# Take Off Power Sizes the Propulsion System

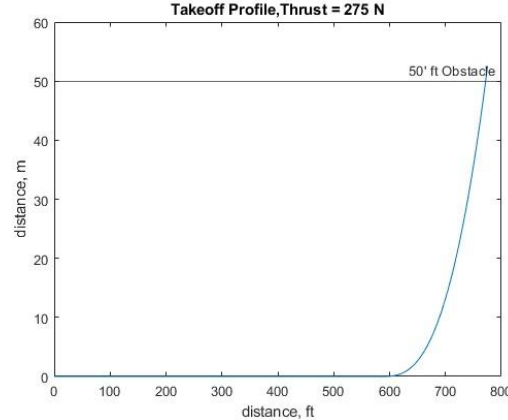
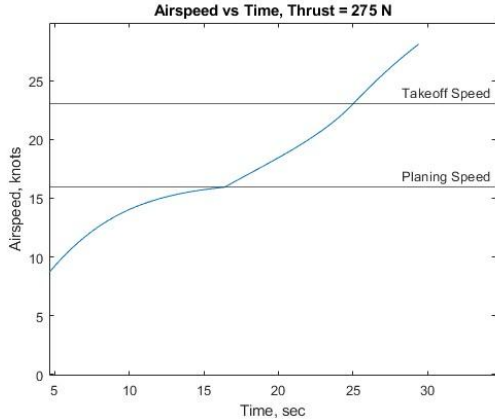
“What does the plane need to do that the solar panels can’t provide?”

Take-Off Power  $\gg$  Cruise Power

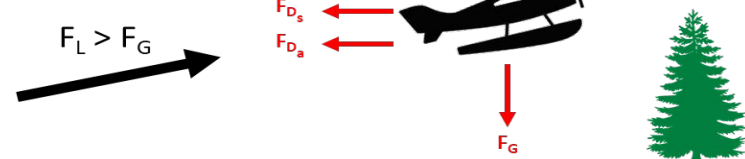
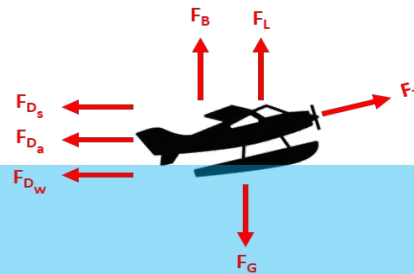
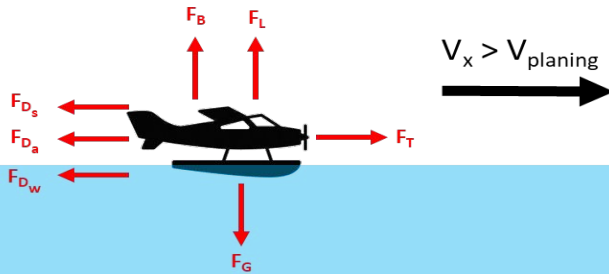




# Planing Speed Sets Minimum Thrust

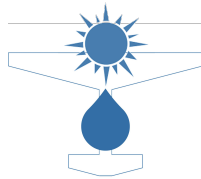


Propulsion Requirements	
Cruise Thrust	195 N
T/O Thrust	275 N
Cruise $P_{Required}$	3300 W
T/O $P_{Required}$	4000 W

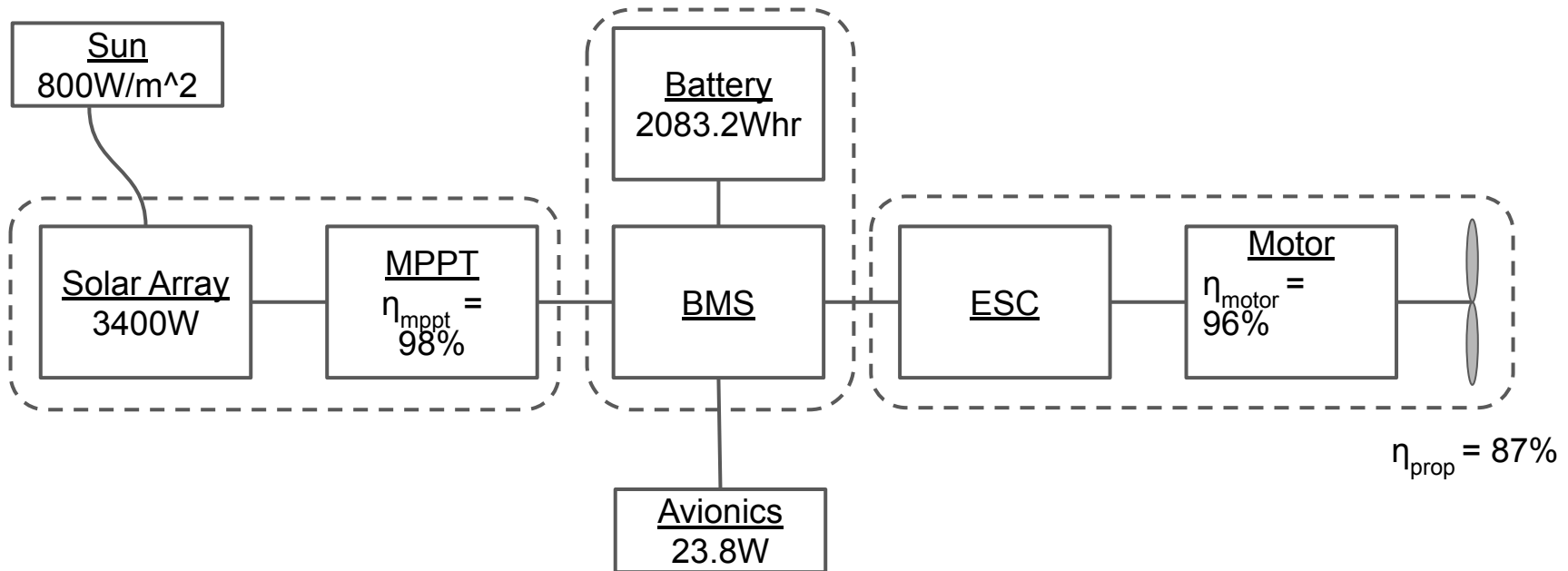


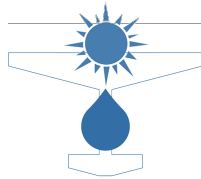
Assumptions:

- Plane “snaps” from pre to post planing
- Linear decrease in area between planing and liftoff



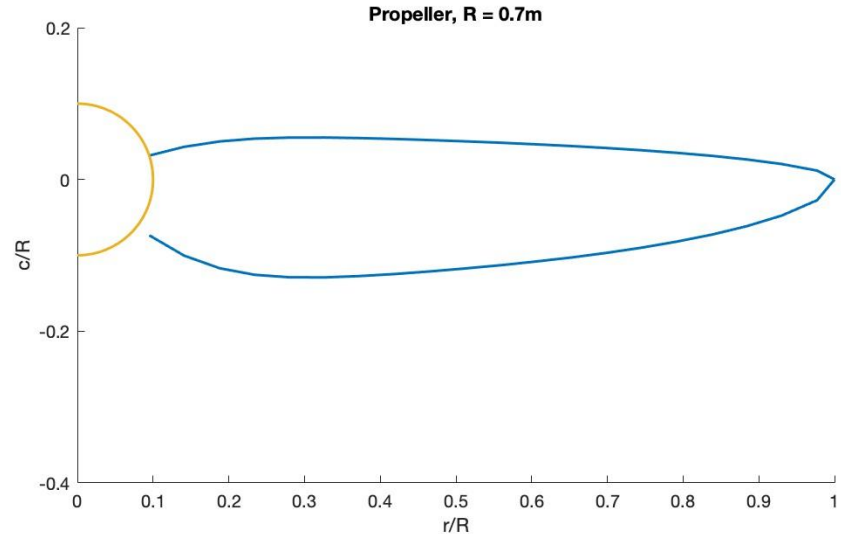
# Powertrain Power Requirements & Efficiencies

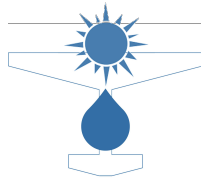




# Propeller Designed For Cruise

- QMIL Propeller Design
  - 2-bladed, 1.4m (4.6ft) diameter propellers
- Considerations:
  - Torque set  $< 20$  Nm
    - $Q \propto W_{motor}$
    - $Q_{cruise} < Q_{max}$
  - Thrust / Power set by T/O Sim



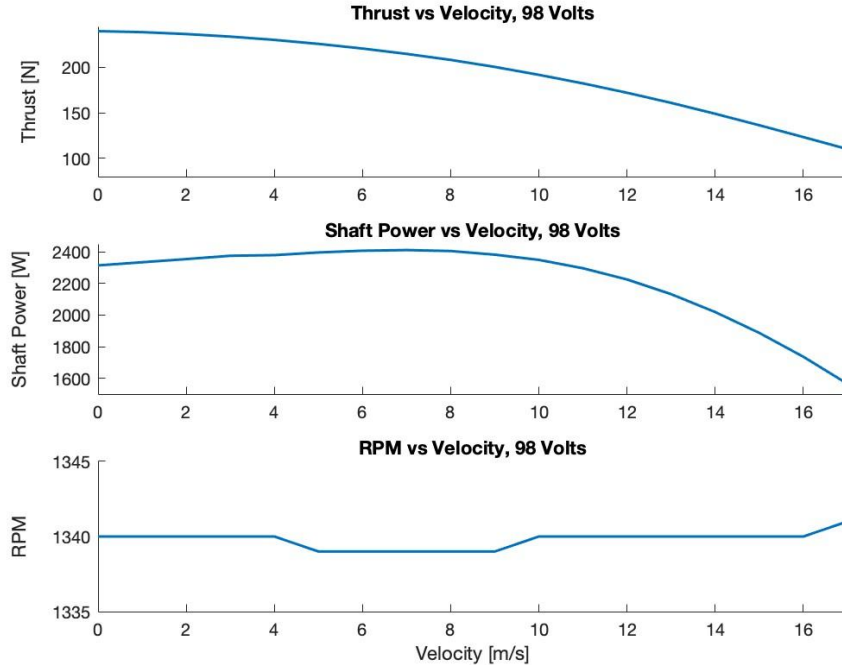


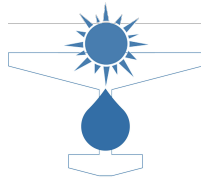
# Propeller Performance

## QPROP analysis\*

$\lambda$	0.17
$\Omega_{cruise}$	1340 RPM
$\eta_{prop, cruise}$	84%
$Q_{cruise}$	15.86 N-m
$P_{takeoff} (V=12 \text{ m/s})$	2225 W
$P_{cruise} (V=17 \text{ m/s})$	1565 W
Voltage	96 V
$K_{V, required}$	14

\*per propeller

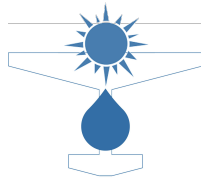




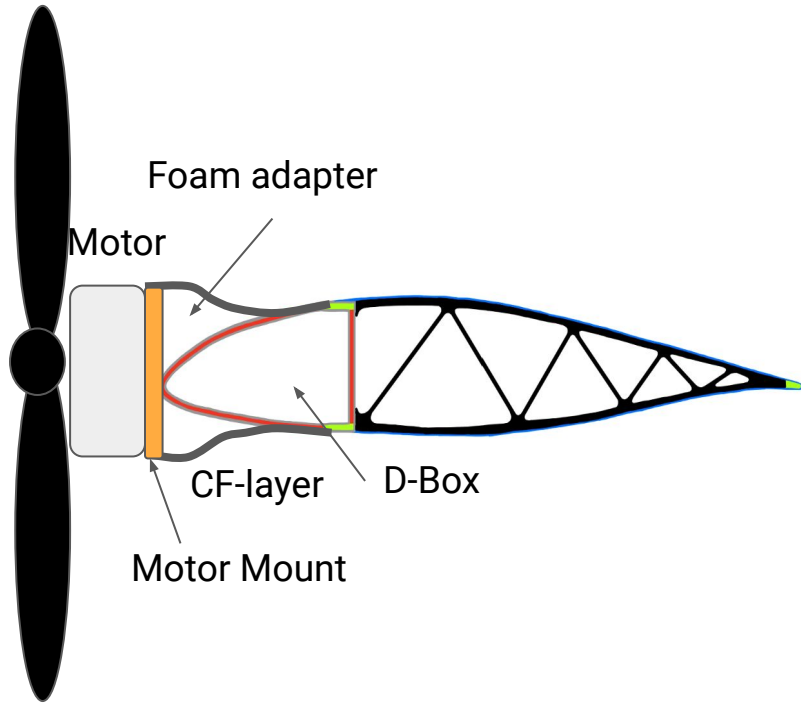
# Motor/Motor Controller Selection

Manufacturer	MAGicALL
Model	6
Torque, max	18 N-m
RPM, max	8000
KV	83 (Will rewind)
Mass	1.5 kg
Efficiency	90.5%
Cooling	Air flow on fins
Dimensions	4.5" diam. 3.5" leng.

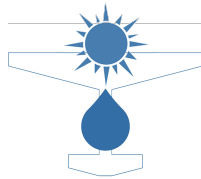




# Motors Attached via Composite Mount



- Motors interfaced with main wing on D-box and main spar using foam adapters
- Attach motor mount via foam adapters and molded carbon fiber composite
- Screw motor on mounting plate



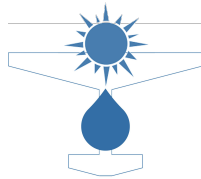
# Battery Specifications & Selection

Battery Pack Specifications	
Chemistry	Li-Po
Capacity	21.7 Ah
Voltage	96 V
Cells in series	26
Cells in parallel	10
Weight	19.5 lbs
Volume	316 cubic inches

Battery Cell Specifications	
Capacity	2.2 Ah
Voltage	3.7 V
Max C-Rate	5
Cell Energy Density	260 Wh/kg



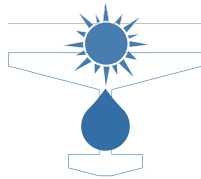




# Battery Charge/Discharge

Flight Phase	Time	Battery Energy used	Battery Charge Used (21.7 Ah total capacity)	SOC (End of Phase)
Take-off	30sec	5.5Whr	0.054 Ah	99.66%
Climb (50ft)	8sec	10.80Whr	0.2 Ah	99.01%
Cruise (charging)	40min (13min / 1 DOD)	CV = 109.2V	-	100%
Cruise (Battery Powered)	30min	1650Whr	17.2 Ah	20.78%



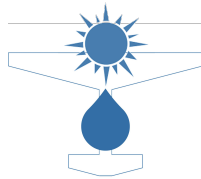


# MPPT

Manufacturer	MakeSkyBlue
Model	96V45A
Max Current Output	45A
Voltage Output	96V
Max PV Input Power	4500W
Max Efficiency	98.2%
Total Mass	1.1kg
Dimensions/unit	8.5" x 4.5" x 2.0"

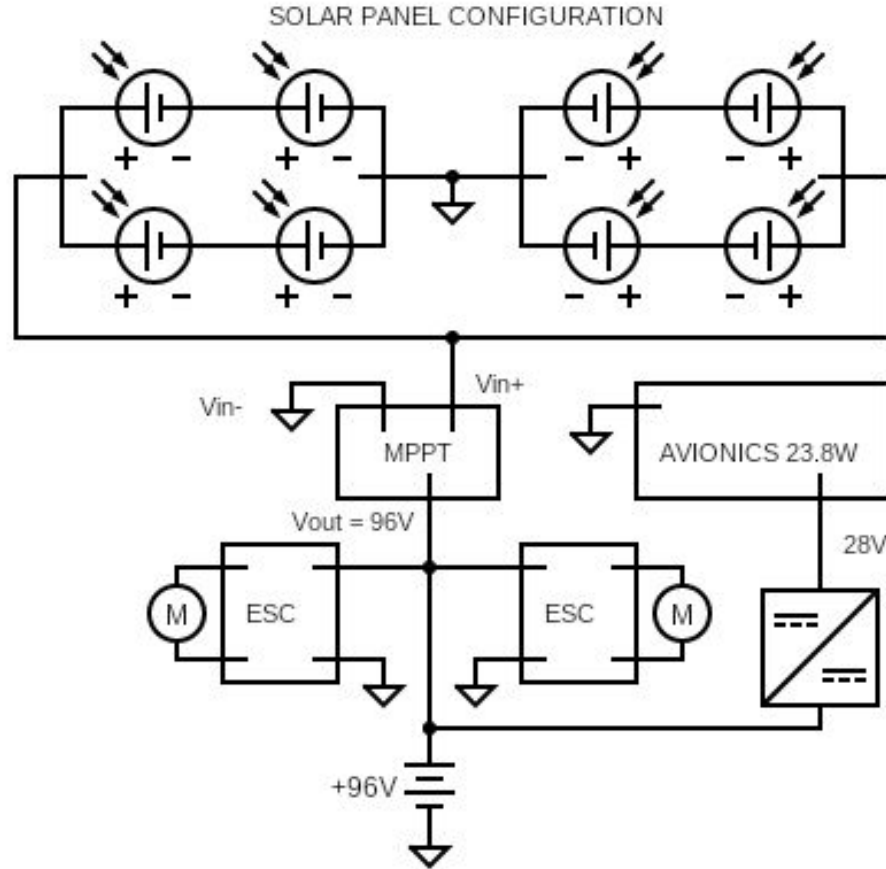


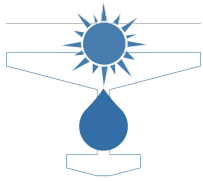
- Matches battery voltage
- PV power < Max input power



# Circuit Diagram

- MPPT inputs variable panel voltage (up to 500V), outputs 96V
- DC/DC converter inputs 96V from battery, outputs 28V for avionics

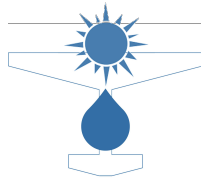




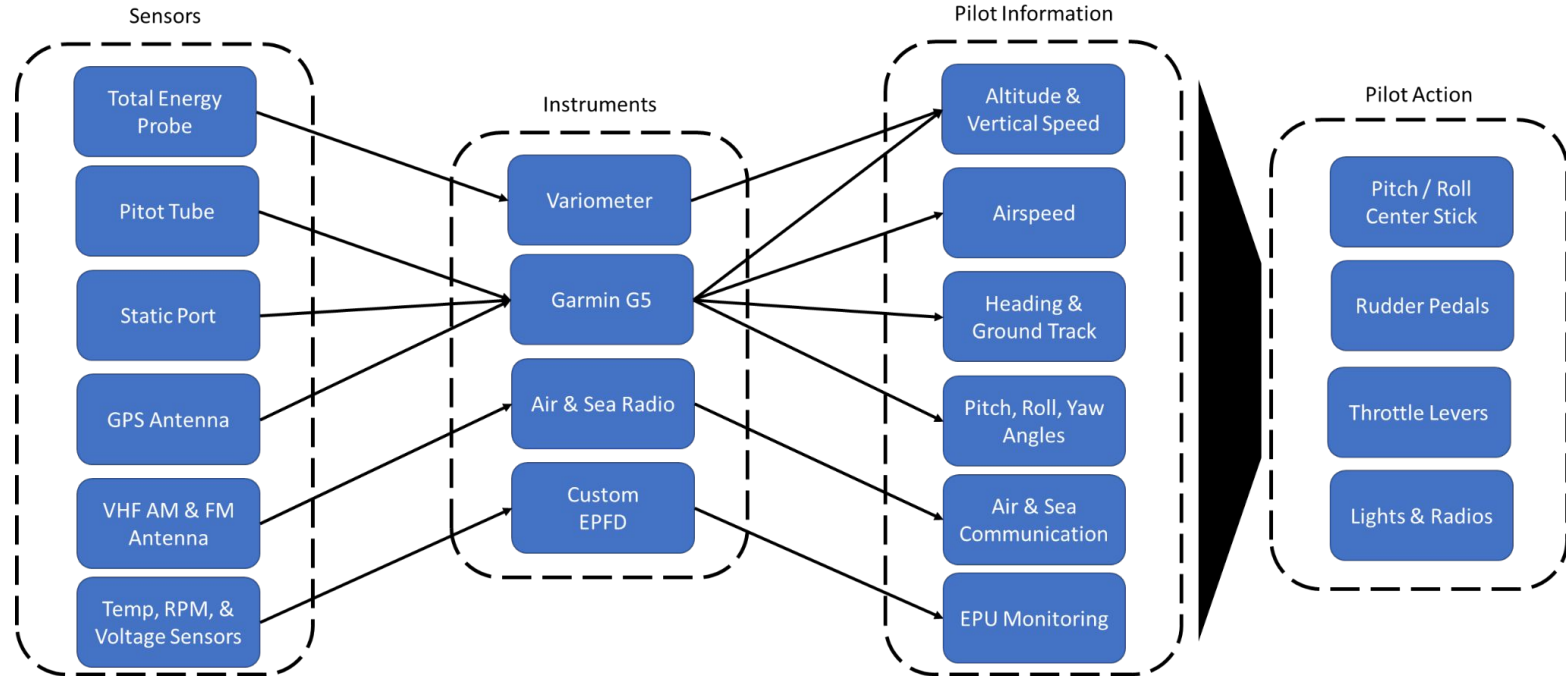
# Outline

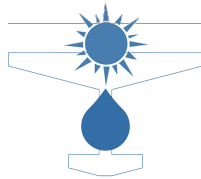
## 3. Subsystem Design

- a. Wing
- b. Fuselage
- c. Stabilizers
- d. Propulsion
- e. Human-Machine Interface**
  - i. Avionics
  - ii. Cockpit
  - iii. Control Routing



# The Human-Machine Interface



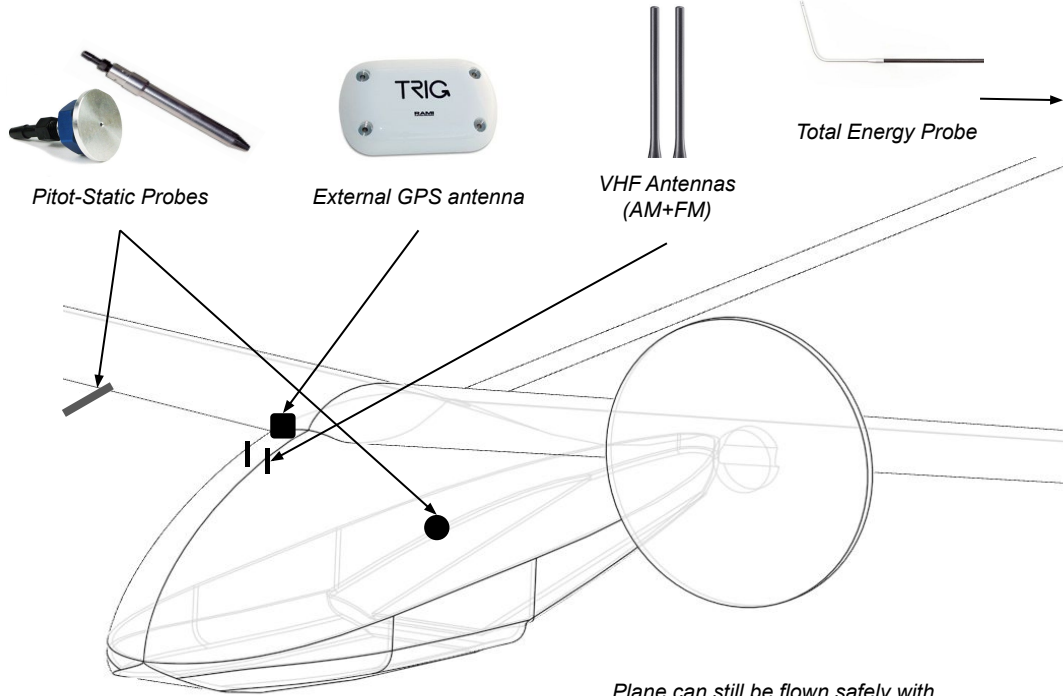


# Simple Sensors

Sensors

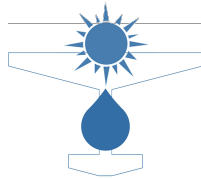
Instruments

Pilot Info



Part	Weight (lbs)
Pitot Static Probes & ADC	1.50
Total Energy Probe	0.50
GPS Antenna	0.31
VHF Antenna Extension (x2)	1.10
LM90 Temp Sensors (x5)	0.50
Antenna + Signal Wiring	3.00
<b>Total</b>	<b>9.73</b>

*Plane can still be flown safely with single or multiple sensor failures*



# Simple Instruments

Sensors

Instruments

Pilot Info



MPPT



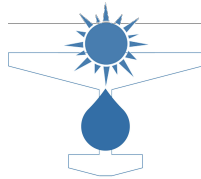
30W 96V/28V DC-DC



Part	Weight (lbs)	Power @ 28V (W)
Garmin G5	0.84	2.8
Custom EPFD	2.00	3.0
Strobe Lights (x2)	0.22	3.0
Air + Marine Radio	1.22	12
100' 12AWG Wire	4.00	-
Variometer	1.01	0
<b>Total</b>	<b>9.50</b>	<b>23.8</b>

# Simple Cockpit

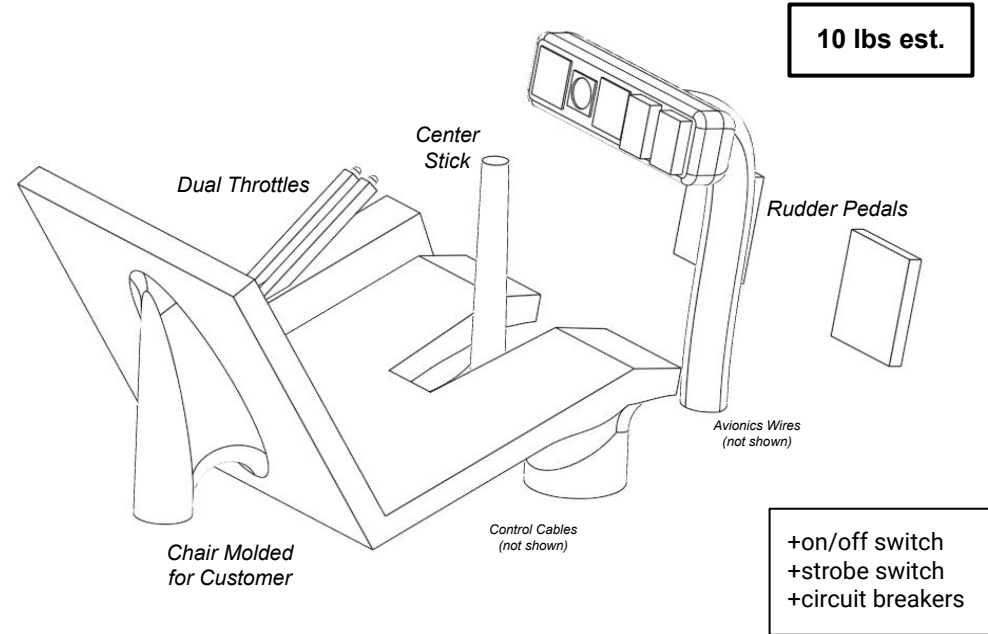
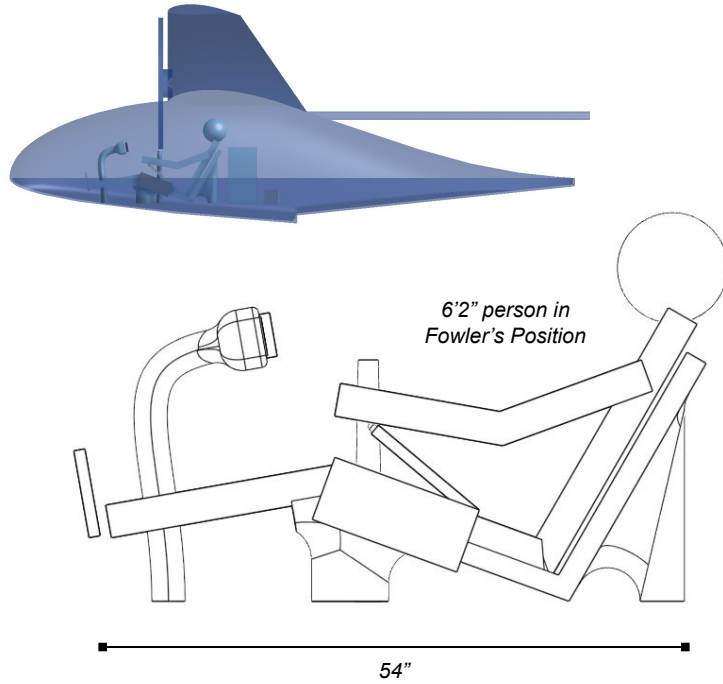
Presenter: Amira Malik



Sensors

Instruments

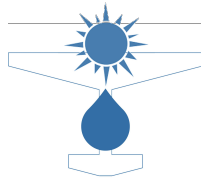
Pilot Info





# Simple Panel

Presenter: Amira Malik



Sensors

Instruments

Pilot Info



Electric Propulsion  
Flight Display (EPFD)

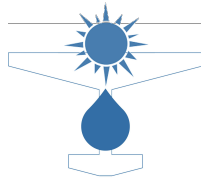
Variometer

Garmin G5

Striped VHF Radios

# Simple Display

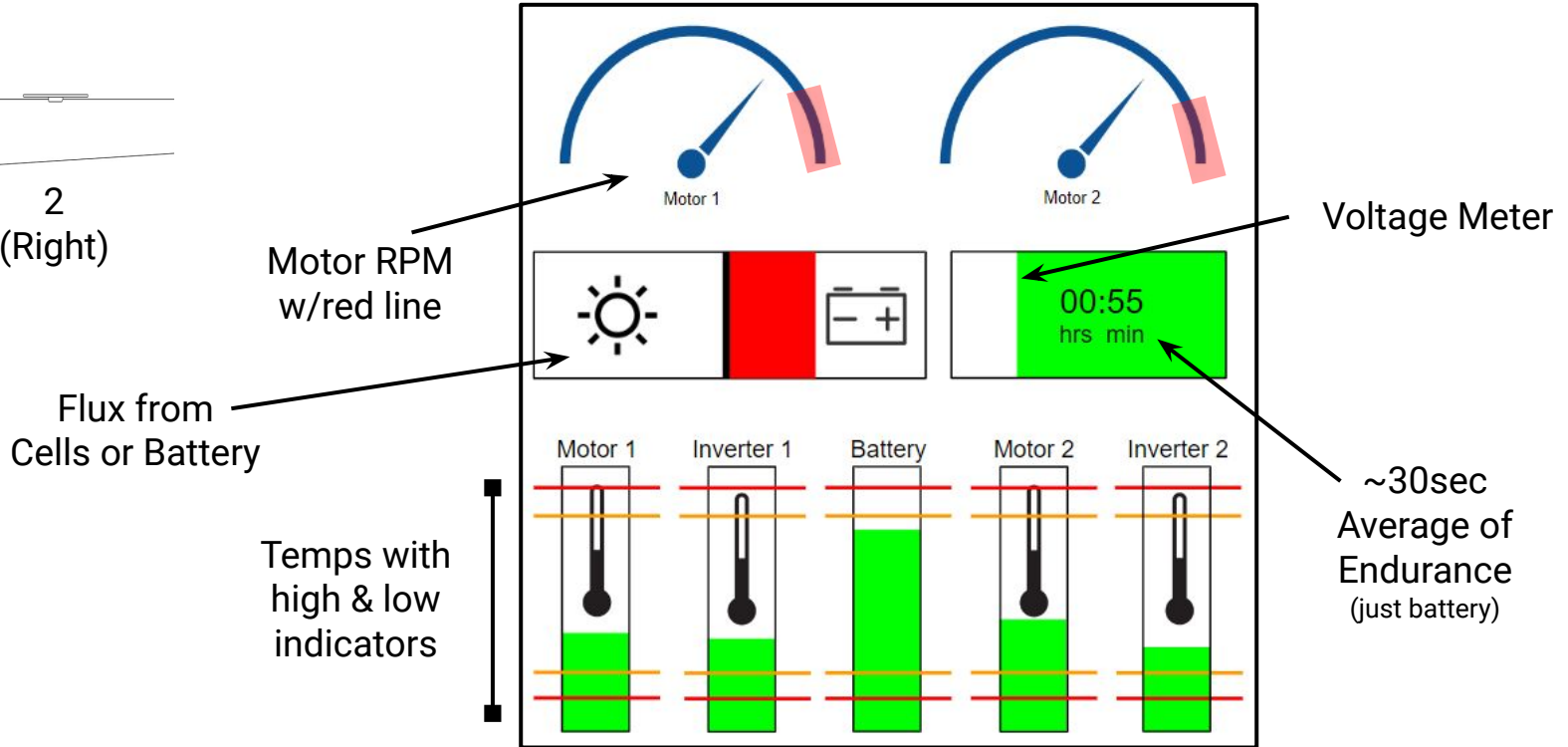
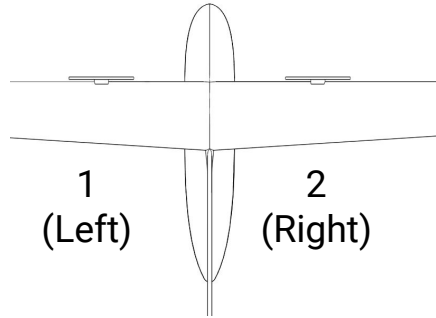
Presenter: Amira Malik

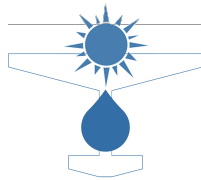


Sensors

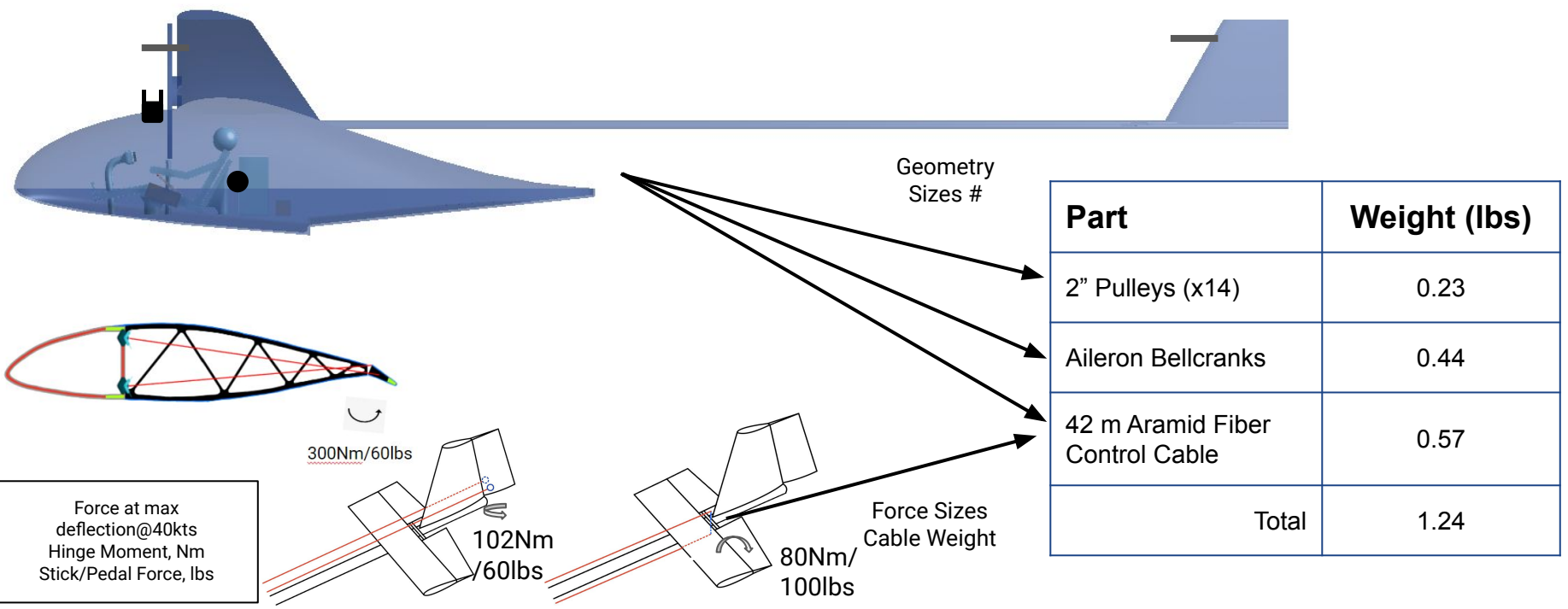
Instruments

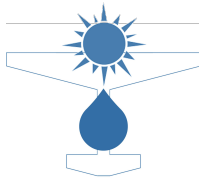
Pilot Info





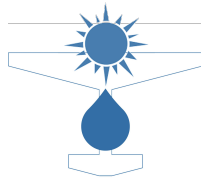
# Simple Controls





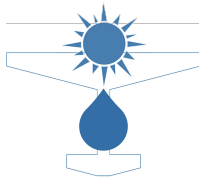
# Outline

1. Motivation
2. General Overview
3. Subsystem Design
4. **Risk**
5. Conclusion



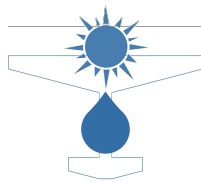
# Risks

- Project risk: Currently over ultralight requirement weight by 18 lbs
  - Key components to check: Electrical wiring, wing, planing hull.
- Current configuration allows a pilot of 170 lbs with full 30 lb cargo, or a pilot 155 lbs or lighter with no cargo.
  - To expand our pilot weight envelope, we can move the batteries or the entire hull a bit forwards to better align the CG's of the pilot and the empty weight
- Motors and Propellers currently not powerful enough to sustain necessary thrust
  - Will be analyzed and fixed



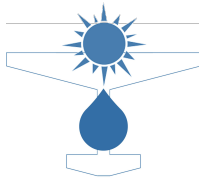
# Outline

1. Motivation
2. General Overview
3. Subsystem Design
4. Risk
5. **Conclusion**
  - a. Short Term
  - b. What's Next?
  - c. Special Thanks!



# Possible Short-Term Design Improvements

- Further airfoil modification for high L/D low Re
- Modeling viscous and interference drag more accurately
- Turbulent flow visualization for total energy probe placement
- Verify the dynamic stability polars are sufficient
- Load pathing between major elements
  - Tail -> Bulkheads -> D-Box
  - Pylon bracing to wing structure
  - Wing skin load paths



# What's Next?

**Buy it** - all components are either COTS or its constituents are defined

**Build (some of) it** - with current sketches, test structures can be built

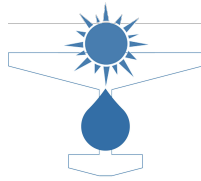
**Test it** - each test section is verified before being built in their final form

**Build (all of) it** - from testing, the design can be modified and built

**Fly it** - on-ground system tests leading to flight tests

**Sell it** - purchase a factory and undergrad labor to assemble and deliver





# Special Thanks

R. John Hansman

Mark Drela

Peter D. Sharpe

Jessie Stickgold-Sarah

Rebecca Thorndike-Breeze

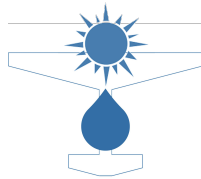
Robert Liebeck

Demet

Team Air, our good competition



# Backup Slides

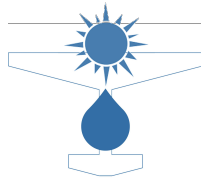


# Possible Scale Models

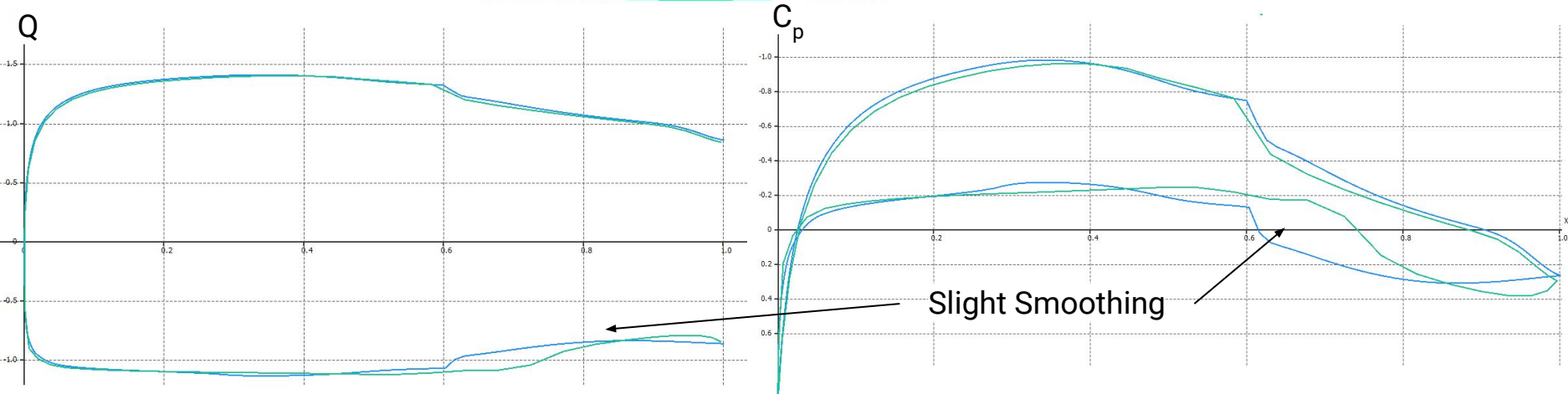
## Major Risk: Weight & Size Mitigation: Scale Design

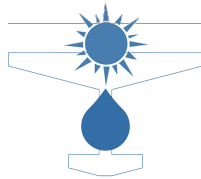
By Dimension	Wingspan (ft)	MTOW (lbs)	Payload (lbs)	Certification Type
Full Scale	74	582	260	Piloted Ultralight
<b>6/7 Scale</b>	<b>63</b>	<b>370</b>	<b>163</b>	<b>Piloted Ultralight</b>
<b>3/4 Scale</b>	<b>56</b>	<b>245</b>	<b>110</b>	<b>UAV (Waiver Needed)</b>
<b>1/2 Scale</b>	<b>37</b>	<b>73</b>	<b>33</b>	<b>UAV (Waiver Needed)</b>
<b>4/9 Scale</b>	<b>33</b>	<b>51</b>	<b>23</b>	<b>107 Compliant</b>
<b>1/3 Scale</b>	<b>24</b>	<b>22</b>	<b>10</b>	<b>107 Compliant</b>

# Aerodynamics

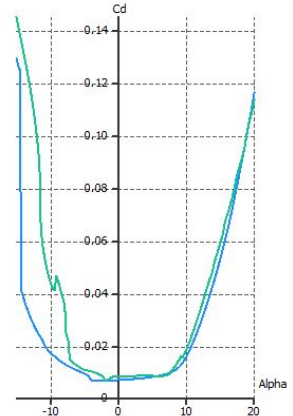
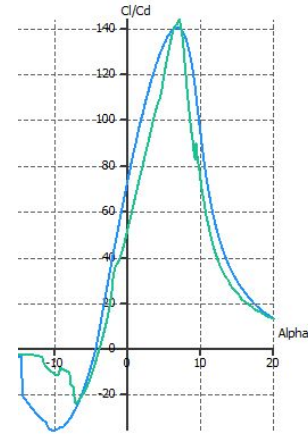
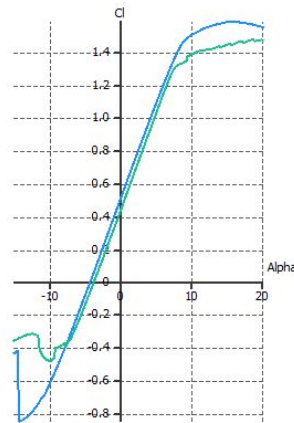
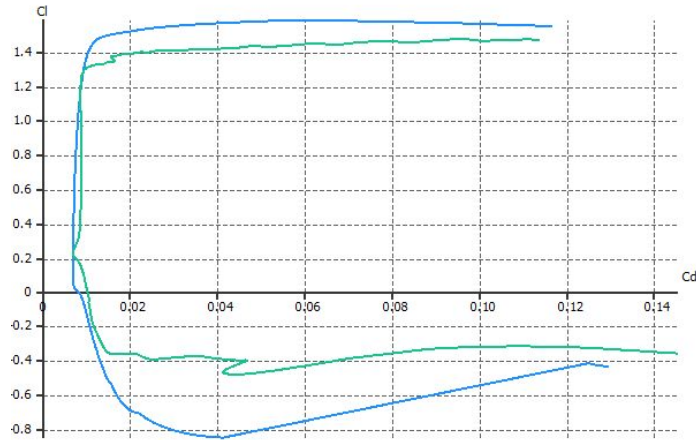


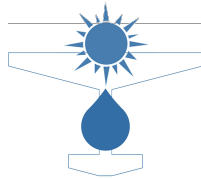
# Modified Eppler 603 Airfoil





# Modified Eppler 603 Airfoil





# Wing Design Formulation

## Known Variables

The governing equations

$$L = \frac{1}{2} C_L \rho S V^2$$

$$D = \frac{1}{2} C_D \rho S V^2$$

$$P_{required} = \frac{S}{\eta_P} \sqrt{\frac{2}{\rho}} \left( \frac{C_D}{C_L^{\frac{3}{2}}} \right) \left( \frac{W}{S} \right)^{3/2}$$

$$P_{generated} = \eta_P \eta_m \eta_s \eta_a S Q$$

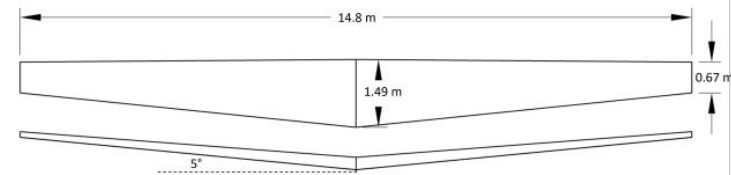
$$\frac{T}{W} = q C_D \left( \frac{1}{W/S} \right) + k \left( \frac{1}{q} \right) \left( \frac{W}{S} \right)$$

With  $W=L$ , all can be parametrized by speed  
So, code sweeps speeds

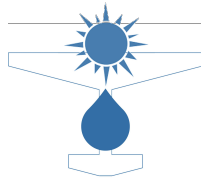
Symbol	Known Variables	Value (SI units)
L, W	Weight-Force at Cruise [6]	2510 N
$\rho$	Density Altitude [6]	.91 kg/m <sup>3</sup>
Q	Determined Value [2]	800 W/m <sup>2</sup>
$\eta_s$	Determined Value [3]	22.4%
$\eta_p$	Determined Value [4]	76.5%
$\eta_m$	Determined Value [4]	96.22%
$\eta_a$	Determined Range [5]	[75%, 85%]

## Initial Design

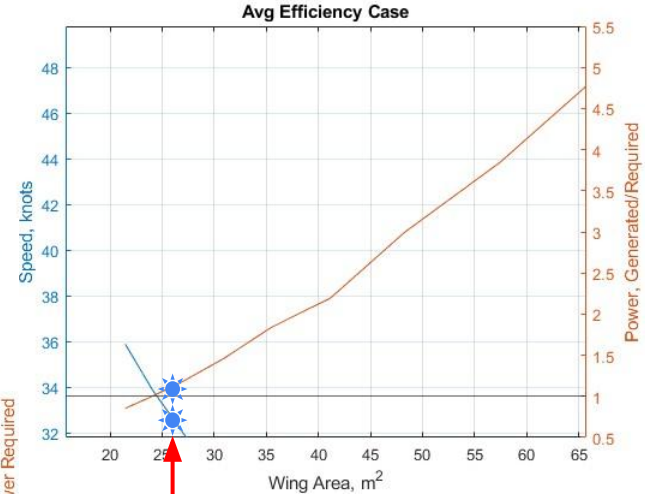
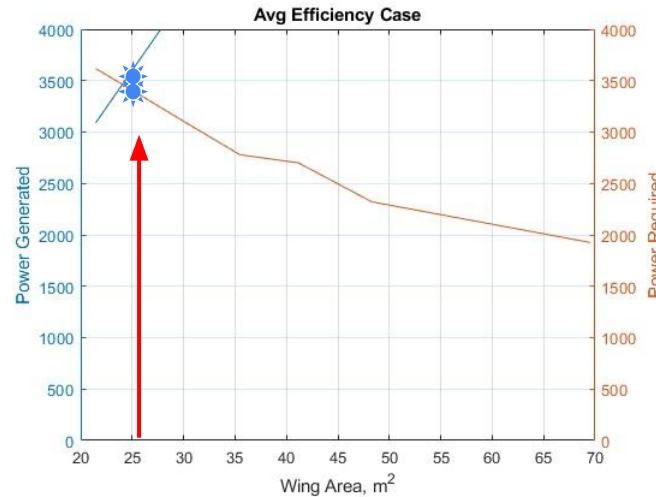
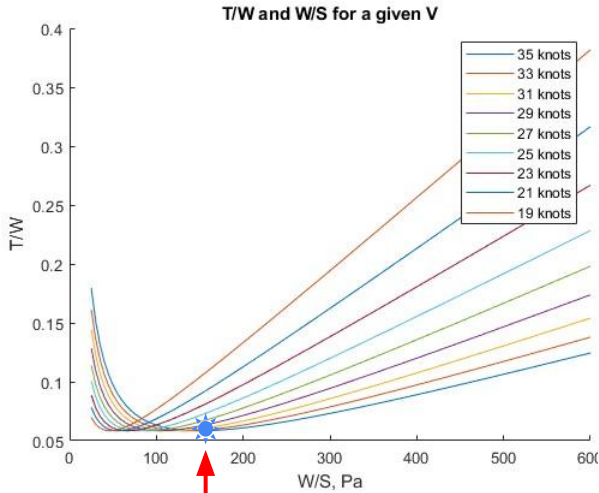
Variable	Assumed Value
airfoil	Eppler 603
L/D, aircraft	22
L/D, wing	36
$\mathcal{R}$	15
e	.8
$c_L$	1.2



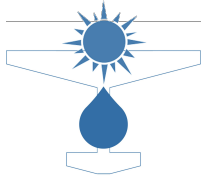
The dimensions of the wing dimensions from which we start



# Wing Design Speed Sweep Results



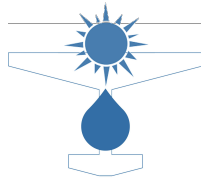




# Backup slide: Air Drag of Bodies Build Up

MASTER VARIABLES		WETTED AREAS		ESTIMATED CD <sub>s</sub>		CRUISE BODY DRAG		
Speed	17	Fuselage	9	Fuselage (NACA0030)	0.02	Fuselage	31.86225	91.0
Air Density	1.225	Sponsons	0.1884954	Sponsons (NACA0040)	0.01	Sponsons	0.3336604199	1.0
Water Density	1027	Tail Boom	0	Tail Boom (cylinder)	0	Tail Boom	0	0.0
		Struts	0.16	Struts (NACA0010)	0.005	Struts	0.14161	0.4
		Wing	25.76	Wing (Eppler 603)	0	Wing	0	0.0
		H-Stab	0.8461	H-Stab (NACA0008)	0.008	H-Stab	1.19816221	3.4
		V-Stab	1.05	V-Stab (NACA0008)	0.008	V-Stab	1.486905	4.2
						Drag	35.02258763	
						Lift	2510	
		CdA is comparable						
		CdA of a step is equal to the area of the step no question, always dragy						
						L/D	71.66821157	
						CD	0.005346734692	

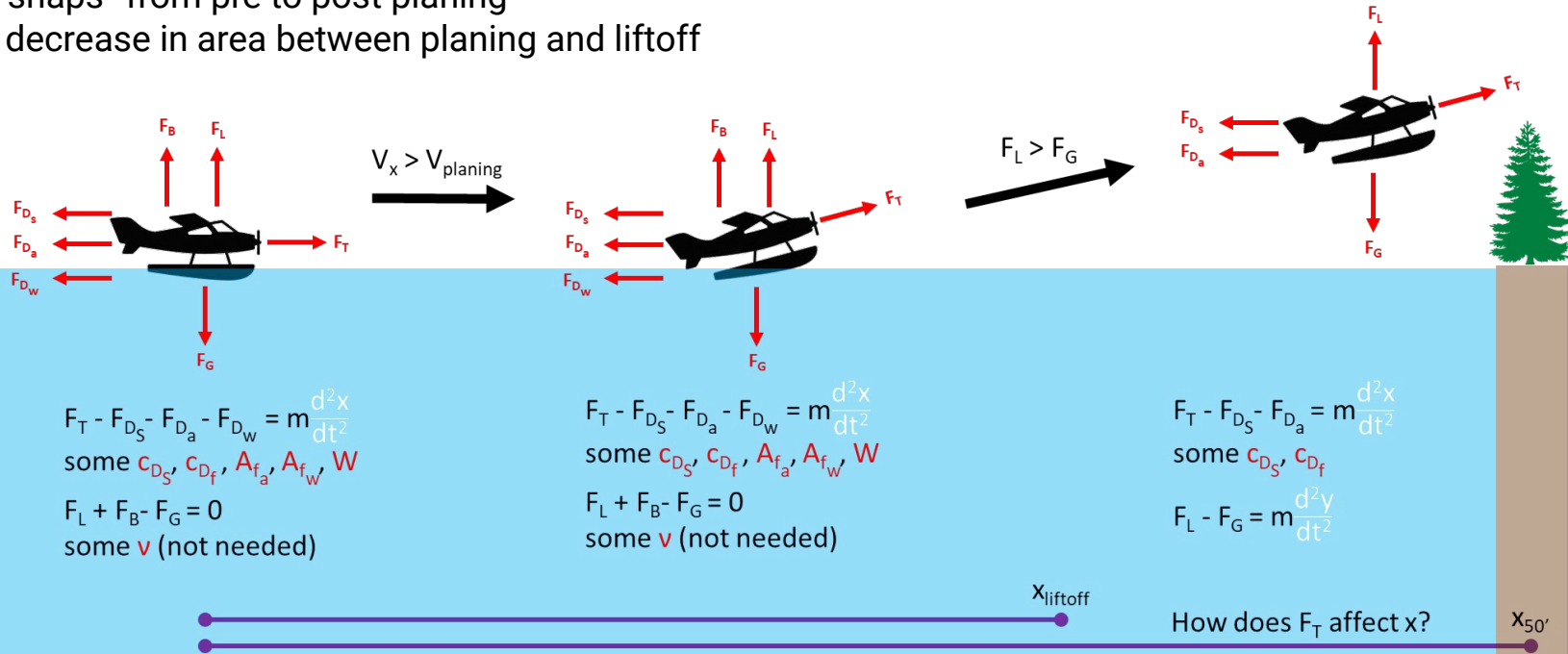
# Power



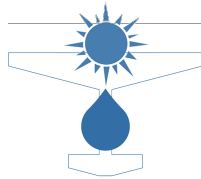
# Takeoff Simulation Forces

## Assumptions:

- Plane “snaps” from pre to post planing
- Linear decrease in area between planing and liftoff



How does  $F_T$  affect  $x$ ?



# Propulsion Requirements Recap

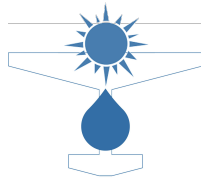
**Cruise power** comes from solar panels with 100W margin

**Cruise-Climb power** comes from solar panels with 0W margin (~100 fpm)

**Takeoff power** requirement comes from takeoff sim

**Expedited climb** has no requirement: if needed, will come from battery margin

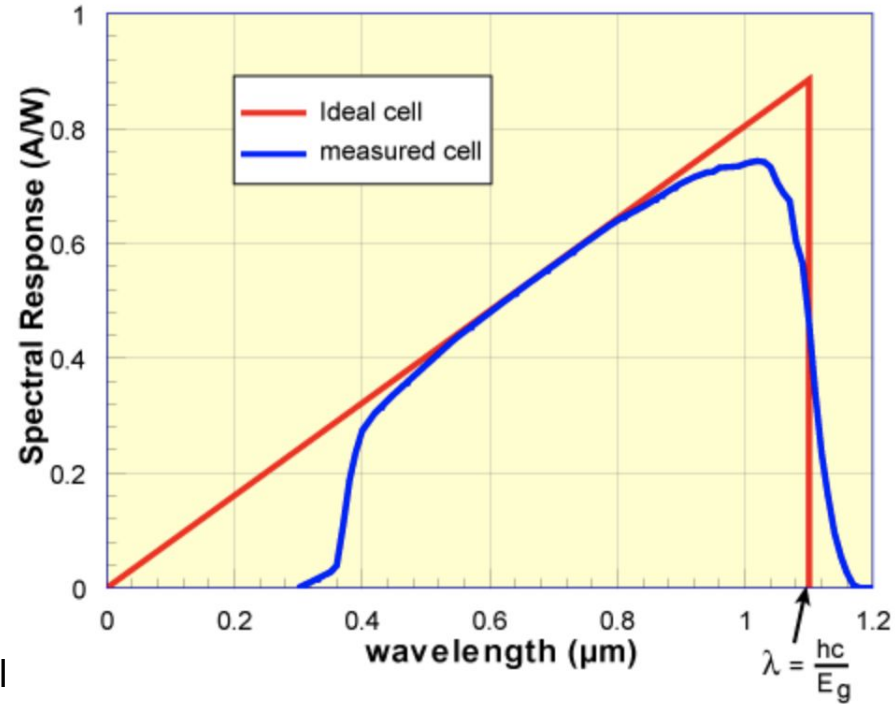
Cruise Propulsion		Climb Propulsion		Takeoff Propulsion	
Cruise Thrust	195 N	Climb Thrust	200 N	Takeoff Thrust	275 N
Cruise Speed	33 KCAS	est. $V_y$ Speed	35 KCAS	Avg. Speed	28 KCAS
Cruise Power	3300 W	Climb Power	3400 W	Takeoff Power	4000 W
Power Margin	+100 W	Power Margin	-0 W	Power Margin	-600 W

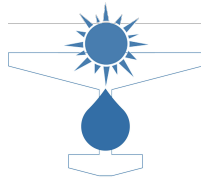


# Solar Cell Protection Backup

- Cover cells in a single layer of Halar® ECTFE
  - Resistant to UV light radiation → irrelevant!
- Typical solar cells perform **best** in **0.4–1.1 μm** wavelength range (visible light and IR)
  - Outside of UV **0.01-0.4 μm** wavelength range

SR = current generated by cell ÷ power incident on cell



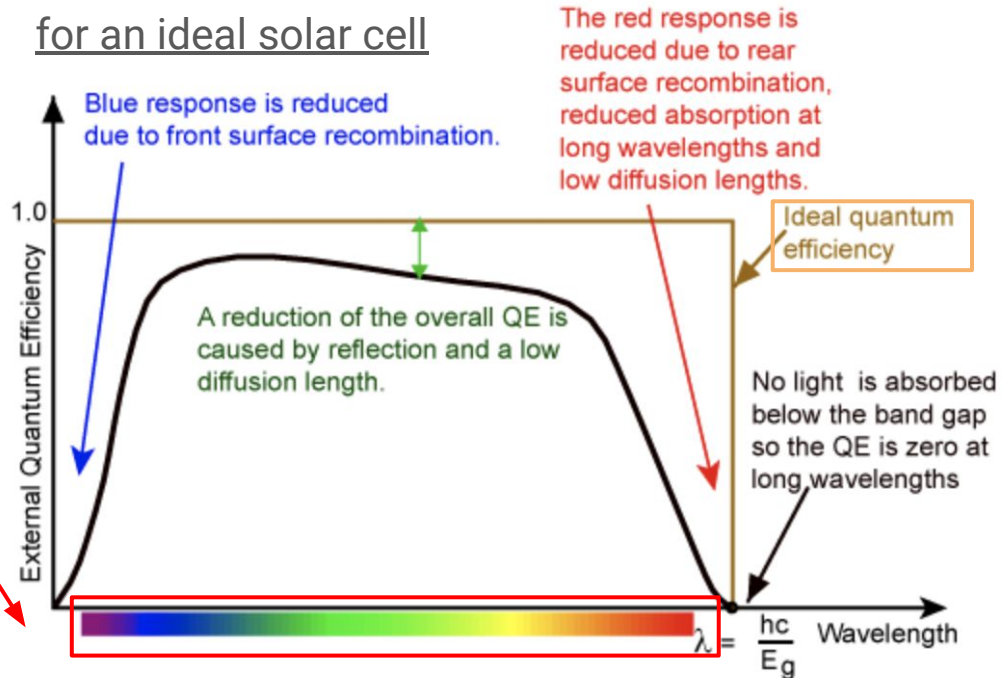


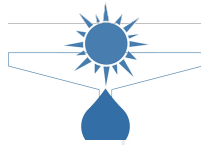
# Solar Cell Protection Backup

- Cover cells in a single layer of Halar® ECTFE
  - Resistant to UV light radiation → irrelevant!
- Highest quantum efficiency in **visible light spectrum** for typically solar cell
- SunPower C60 cells also do well in IR

number of carriers collected by cell  $\div$  number of photons of a given energy incident on the solar cell

Quantum efficiency curve for an ideal solar cell





# Battery Weight Breakdown Backup Slide

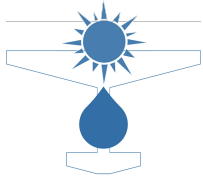
Sized by voltage of 96 V



Sized by max power needed and capacity

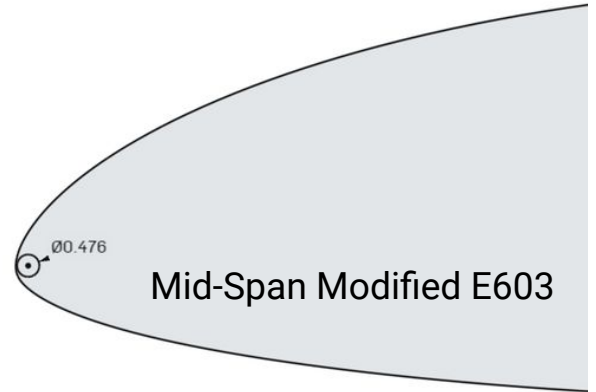
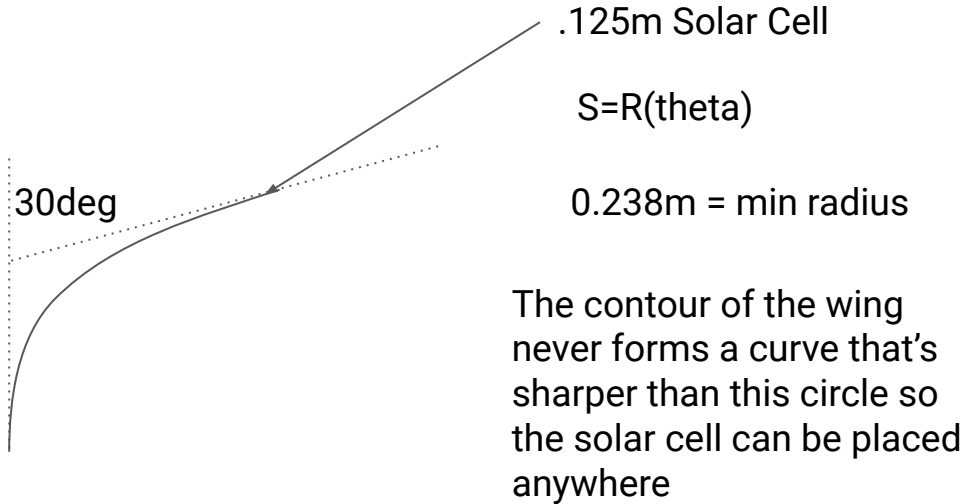


	Endurance Sizing	Power Sizing	
cells in series	26.0	26.0	
parallel strings	11.0	7.0	
number of cells	286.0	182.0	
cell mass	9.0	5.7	kg
pack mass (inc BMS)	9.7	6.2	kg
pack mass in lbs	21.4	13.6	lbs
Specific Energy	260	Wh/kg	Li-ion
<b>Specific Power</b>		W/kg	Li-ion
depth of discharge	0.8		
cell capacity	2.2	Ah	
cell voltage	3.7	V	
max C rate	5		
mass per cell	31.3	g	High Rate Discharge Li Polymer Battery part
battery packing factor	0.92		

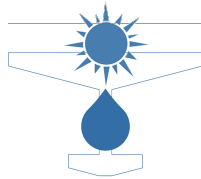


# Solar Cell Placement Backup

Solar cell max bend angle = 30deg

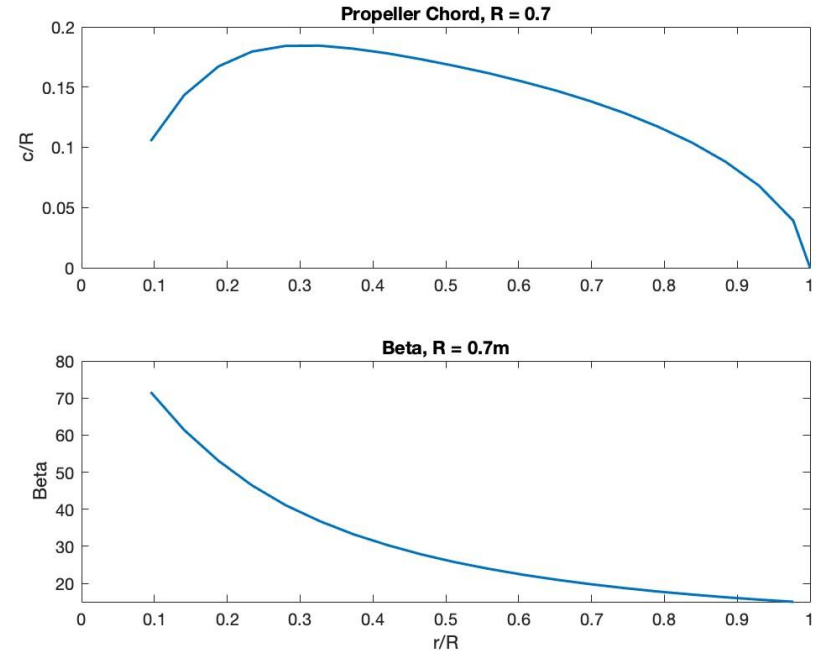




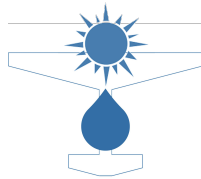


# Propeller Backup

- $\eta_i = 89\%$ 
  - Induced efficiency is a little low, could increase propeller radius to help
- Power consumption sensitive to voltage, thrust,  $d\beta$
- Variable pitch is an option, but increases motor weight

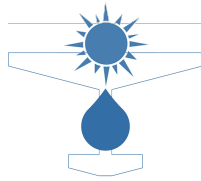


# Structures

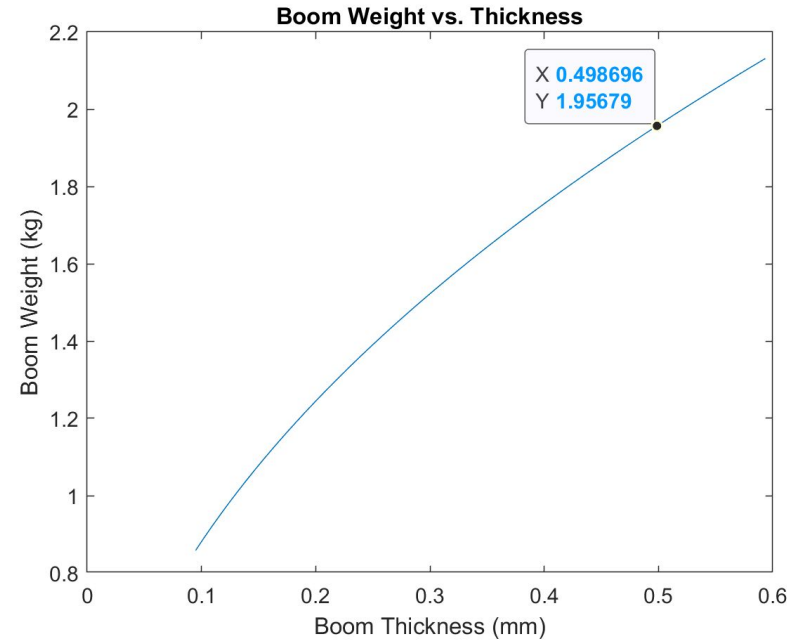
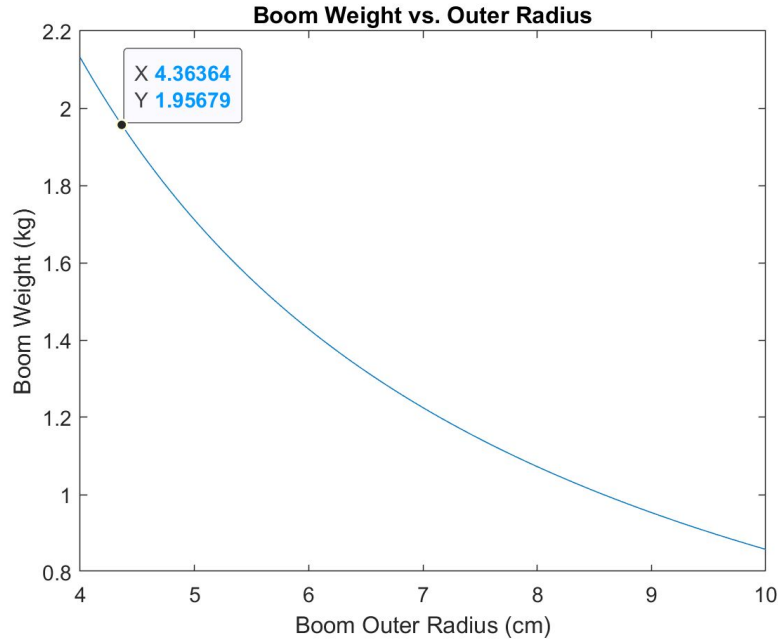


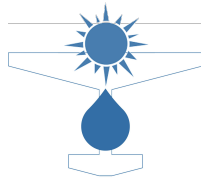
# Wing Weight Breakdown

Component	Weight [lbs]	Weight [kg]	Sizing Case
D-Box	31.6	14.3	Torsional stiffness
Spar Caps	26.4	12.0	Bending stiffness
Ribs	10.8	4.9	Bending stiffness
Fabric	13.3	6.0	Standard
Trailing edge support, aileron hinge	6.5	2.9	Best guess
<b>Total</b>	<b>88.6</b>	<b>40.2</b>	



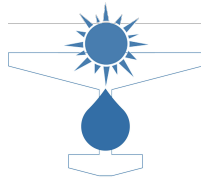
# Boom Weight and Sizing from Bending





# Assumed Forces for Boom and Stabilizer Calcs

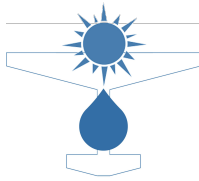
<b>Force</b>	<b>Value</b>	<b>Notes</b>
Horizontal stabilizer lift	812 N	-z direction, elevator fully deflected
Vertical stabilizer lift	552 N	+/- y direction, rudder fully deflected
Weight of horizontal stabilizer	30 N	-z direction
Weight of vertical stabilizer	35 N	-z direction



# Stabilizer CF Layer Thicknesses

Quantity	Value	Notes
# of layers on skin	2	For both horizontal and vertical stabilizers
# of layers for D-box	2	For both stabilizers, 4 total with skin layered on top
# of layers in web	4	For both stabilizers
# of layers for kevlar membrane	1-2	For both stabilizers
Horizontal stabilizer sparcap area	0.0151 in <sup>2</sup>	Cross-sectional area
Vertical stabilizer sparcap area	0.0114 in <sup>2</sup>	Cross-sectional area

# Hull Design



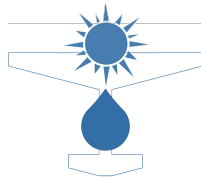
# Fuselage/Planing Hull Sizing References

- 1) Hoerner's Fluid Dynamic Drag
  - a) For axisymmetric streamlined components (assuming  $d = 1.37$  m and  $l = 6.096$  m)
- 2) Planing Flow Lift and Drag Modeling Module on Canvas
- 3) Gudmundsson's General Aviation Aircraft Design: Applied Methods and Procedures Appendix C3: Design of Seaplanes



# Fuselage/Planing Hull Sizing

Presenter:



Froude's liquid resistance formula:

$$R_{Froude} = f \cdot S_{wet} \cdot V^n$$

(C3-18)

Where:  $f$  = Coefficient of frictional resistance  
 $S_{wet}$  = Wetted area in  $\text{ft}^2$   
 $V$  = Speed in knots  
 $n$  = Constant, dependent on surface quality.

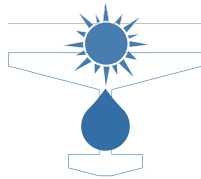
The term  $f$  varies depending on surface quality. For surfaces ranging from 2 to 20 ft in length, it can be taken to be 0.012 to 0.010 for smooth surfaces, 0.0231 to 0.0137 for surface quality resembling fine grit sandpaper, 0.0257 to

$$V = Fr_{\min} \sqrt{g\ell}$$
$$C_L \simeq C_{L_{\max}}$$
$$S_{\min} = \frac{W}{\frac{1}{2}\rho V^2 C_L}$$

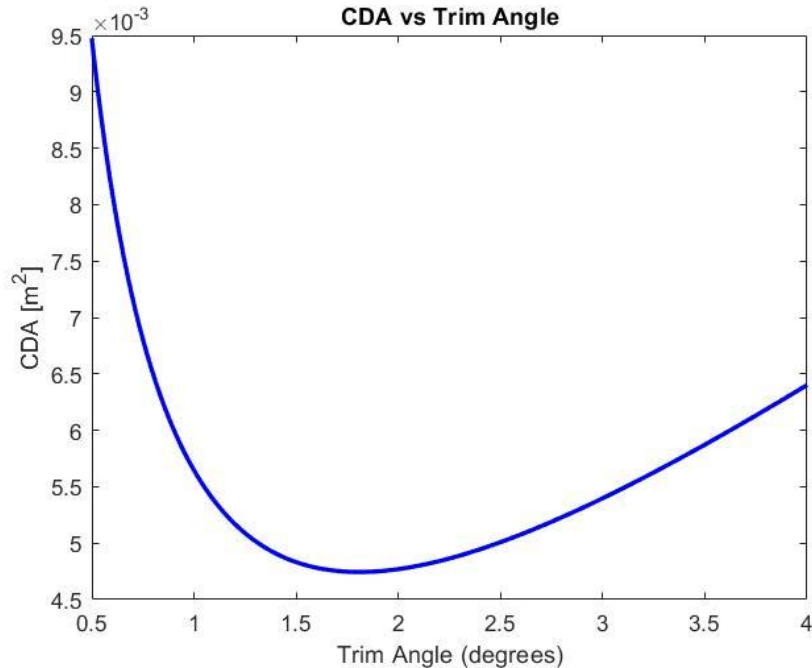
$Fr_{\min} = 1.5$  and  $C_{L_{\max}} = 0.1$ , although the hull shapes. Another requirement is that the

$$V_{\min} \geq k \frac{W}{\rho g}$$

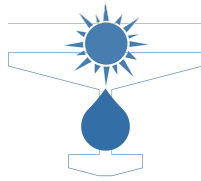
$$C_L \simeq \begin{cases} \frac{\pi}{2} \frac{AR}{1+AR} \alpha & , AR \gg 1 \\ \frac{\pi}{4} AR \alpha + 0.88 \alpha^2 & , AR \ll 1 \end{cases}$$



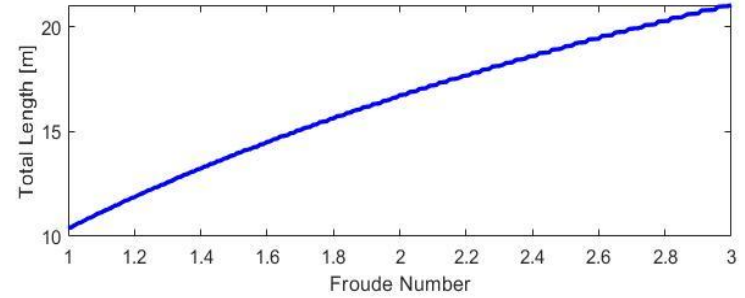
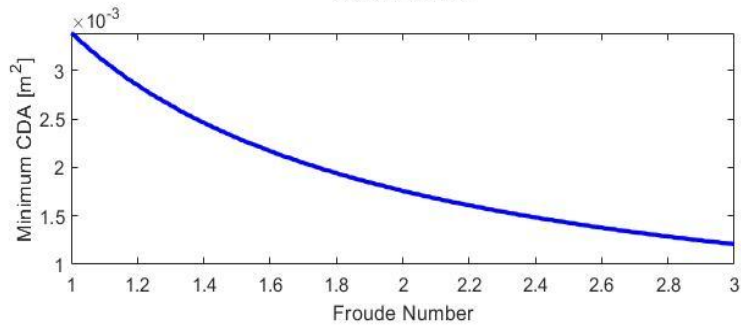
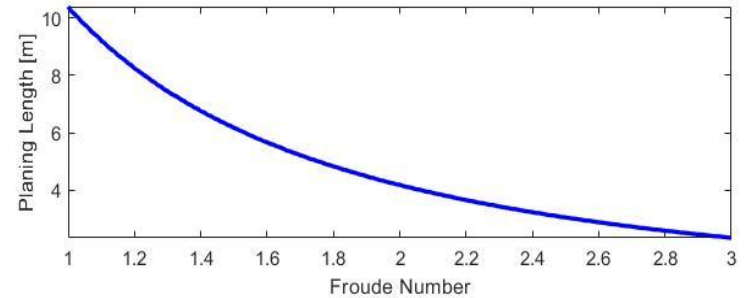
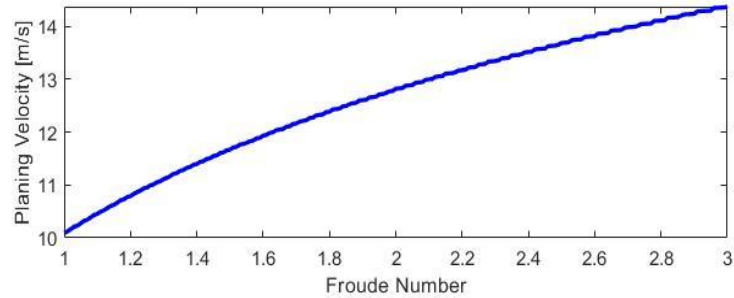
# CDA vs alpha

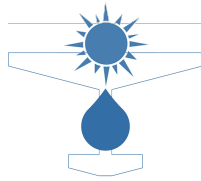


Although alpha and planing length are coupled in the equations we see before, we can actually get a sense of what the optimal alpha value is for a given length. The graph is a CDA vs alpha graph of our dimensions. As you can see, an alpha of 4 degrees results in a CDA of about  $0.006 \text{ m}^2$ .



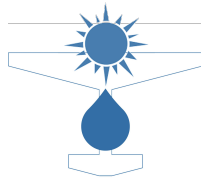
# Planing Hull Optimization Results



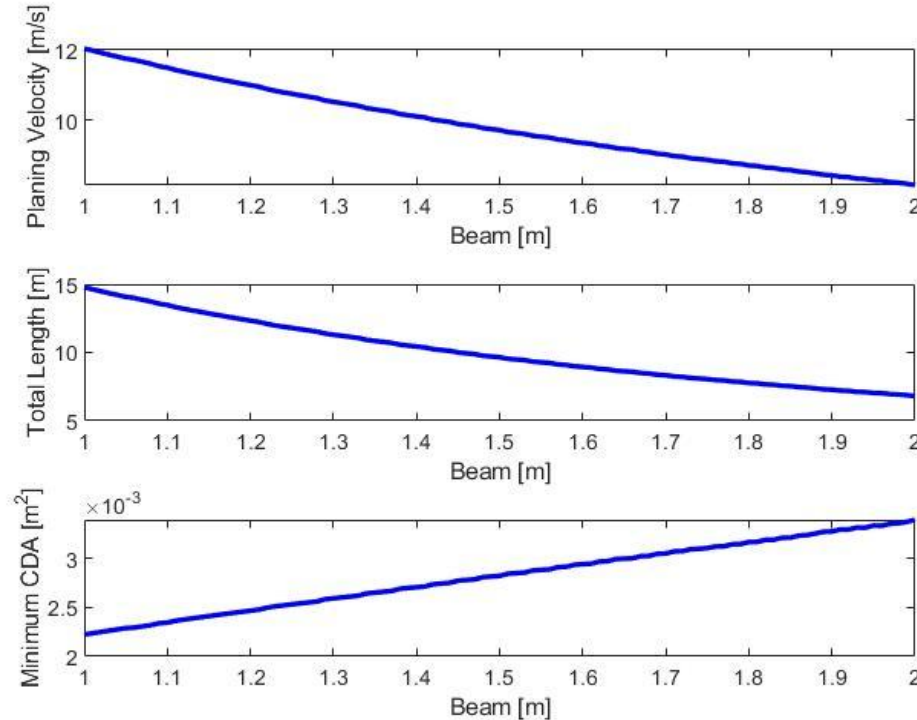


## Context for the graphs on the previous slide

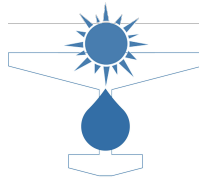
By varying the  $Fr_{min}$  and freezing the beam length to be 1.0668 m, we can see how  $Fr_{min}$  affects our hydrodynamic performance. The graph on the left show Min CDA vs  $Fr_{min}$  and the respective planing velocity. Although the Fr number decreases the min CDA during planing, the planing velocity is actually significantly increases. This can explained with the graph on the right. The length of the planing surface is decreasing because, but because the Froude number<sup>2</sup> is a ratio of the total length vs the planing length, the total length of the hull actually increases (explaining the increase in planing velocity). We want to be planing quick to reduce the effects of pre-planing drag.



# Planing Hull Optimization Continued



From these graphs, it is clear that although you are potentially increasing the planing CDA by about 50 percent going from a beam length of 1 m to 2 m, the total length of the hull decreases significantly, as well as the planing hull. This is consistent with the block diagram where we want a larger beam so that we can plane quicker.



The total drag, based on wetted area is consequently

$$\boxed{C_{D_{wet}}/C_f = 1 + 1.5 (d/l)^{3/2} + 7 (d/l)^3} \quad (28)$$

The graph shows that the third term of this equation is practically negligible up to  $d/l \approx 0.2$ .

**Frontal Area.** The wetted surface area of streamline bodies is approximately

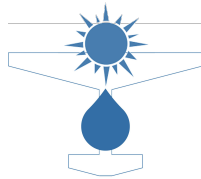
$$S_{wet} = (0.7 \text{ to } 0.8) \ell \text{ (perimeter)}$$

$$CDA = A_{wet} \bar{C}_f K_f \quad (\text{streamlined component})$$

friction coefficient  $\bar{C}_f(Re_\ell, Re_{x_{tr}})$  is assumed to correspond to that on a mix of laminar and turbulent flow values  $\bar{C}_{f_l}, \bar{C}_{f_t}$ , and depends on the length number  $Re_\ell$ , and the transition-length Reynolds number  $Re_{x_{tr}}$ . Approximations given in many references, e.g. Schlichting's *Boundary Layer Theory*,

$$\bar{C}_{f_l} = \frac{1.328}{Re_\ell^{1/2}} \quad (\text{fully laminar})$$

$$\bar{C}_{f_t} = \frac{0.455}{(\log_{10} Re_\ell)^{2.58}} \quad (\text{fully turbulent})$$

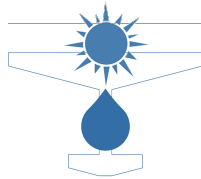


# Fuselage/Planing Hull Drag

Given the beam,  $Fr$ ,  $\alpha$ , and hull lengths, I approximated the CDA of the skin friction drag on the fuselage to be  $0.081 \text{ m}^2$ . It is safe to say that the induced drag from the fuselage is negligible because the ratio max fuselage width (roughly 4.5') to the total span of the main wing is miniscule. I didn't account for any appendages either. Either way, the equations above tell us that larger fineness ratios (i.e. smaller  $D/L$ ) result in lower CDA fuselage which again supports the block diagram in the main presentation (slide 38). Our numbers on slide 39 provide acceptable CDAs for both cruise and takeoff (at 1000').

# Human-Machine Interface





# Sensors/Instruments Justification

## **Why Any Primary Flight Display (PFD)?**

There is no requirement for ultralights and little need for VFR flight outside of airspeed and altitude. However, we prioritize safety and want to mitigate inadvertent IFR flight, so having airspeed, altitude, pitch angle, roll angle, turn coordinator makes the plane much much safer.

## **Why a Variometer?**

We have twin electric motors and can fly on just solar power, but with our wing, you can also simply soar! To have an accurate vertical speed and aircraft energy, a variometer is very helpful.

## **Why Strobes?**

We have a large wingspan and being electric, we are quiet. We need some sort of lighting for hazard avoidance and for people to notice the aircraft approaching unprepared bodies of water. There is no real need for navigation, landing, or taxiing lights, and strobe lights strobe, and so draw more attention. And being on either wingtip shows people on the ground how large our wingspan is.

## **Why custom EPFD?**

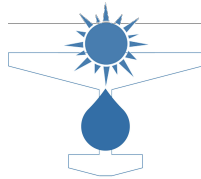
We need to know the state of charge, charge flux, and temps for each component, and motor RPM. It's likely either no COTS solution would exist for this specific use case or that such solution would have to be heavily modified, so we assume a custom EPFD.

## **Why two radios?**

While both are VHF radios, marine and air radios are either AM or FM and thus have different circuits and antennas. Since we fly but also land on water, we need both types to communicate with all other relevant vehicles to our operation.

## **Why external antennas?**

We are concerned about EMI in the aircraft; if, once built, EMI is not an issue, the antennas can be easily relocated inside the cabin



# Handheld Radios are Lighter & Cheaper



Panel Mounted Aviation Radio



Panel Mounted Marine Radio

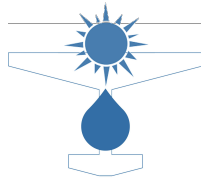


Handheld Aviation Radio



Handheld Marine Radio

Weight (lbs)	Price	Antenna Included	Operational Cons
1.91 lbs	\$1425	No	-Additional wiring -Extra mounting
2.2 lbs	\$130	No	
.57 lbs	\$300	Yes	-Finding radio -Hands Occupied
.65 lbs	\$200	Yes	



# Electronic PFD is Lighter (primary flight display)

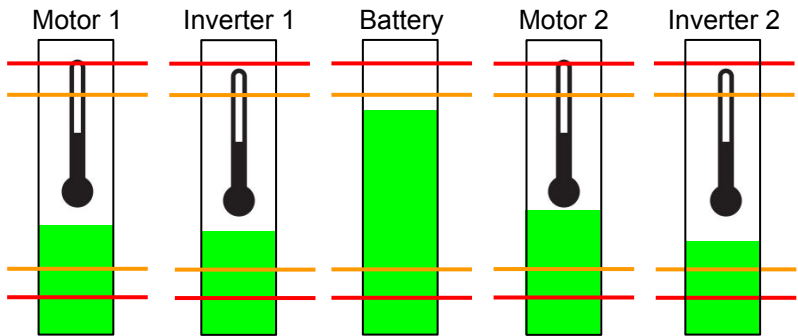
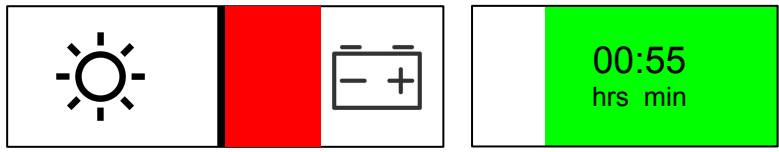
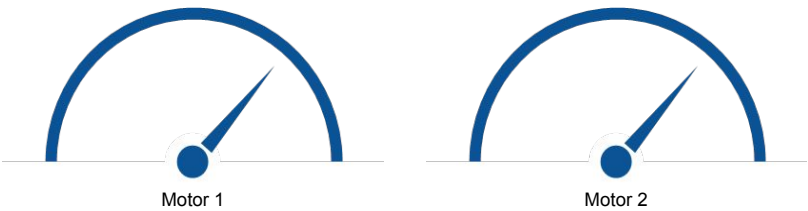


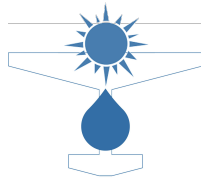
Weight (lbs)	Operational Pros	Operational Cons
2.4	Zero Power Required	More complicated IP wiring / routing Larger IP
.66		
.78		
.84+.31+.50	Much smaller IP	2.8W during cruise

\*Low Voltage Bus needs to exist anyway for lights, radio, and EPFD, so the Bus itself is not a con for G5

AI weight: does not include associated vacuum system  
G5 weight: G5+GPS+ADC

# Drawing the EPFD



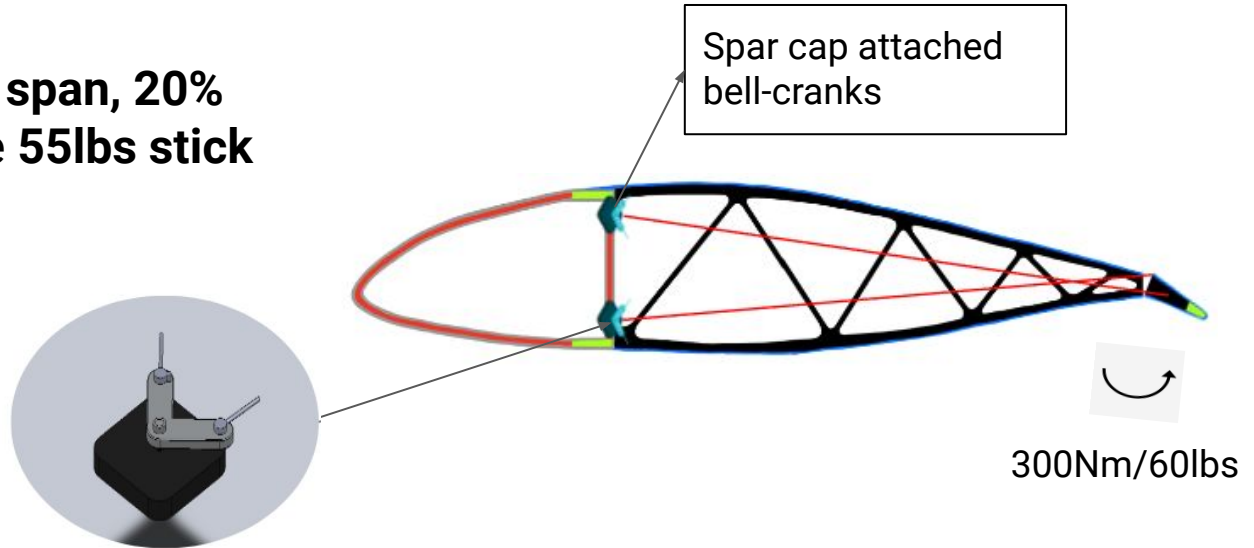


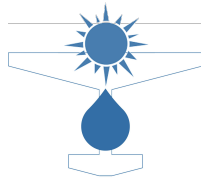
# Control Hinge moment and Stick Force

## Takeaway:

Max deflection, 40kts

- **Aileron(20% semi span, 20% Chord) experience 55lbs stick force**

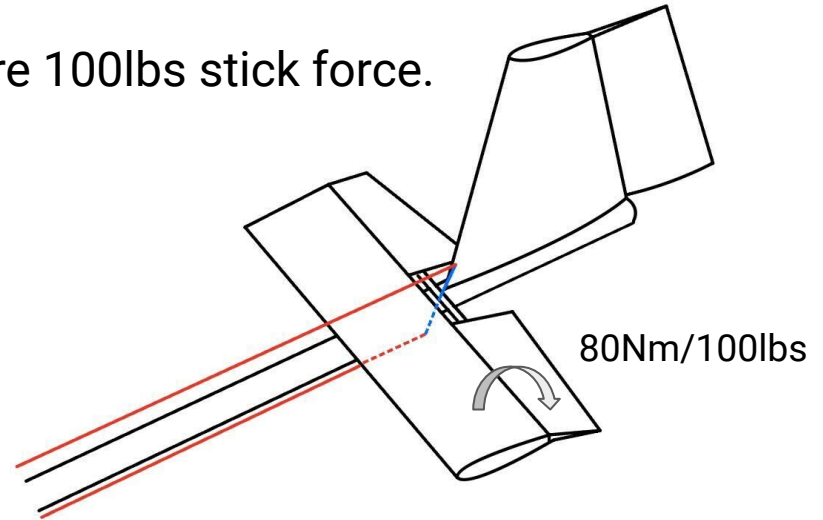
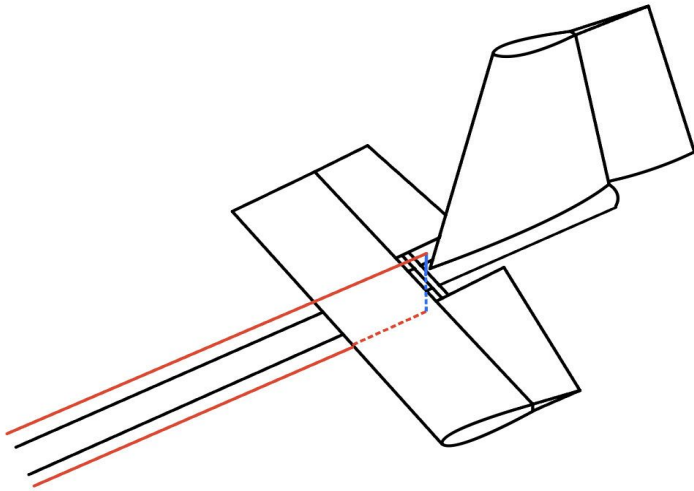


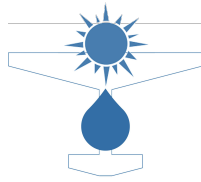


# Control Hinge moment and Stick Force

## Takeaway:

- Max deflection, 40kts
- Partial H-Elevators  $C_e/C_h \sim 0.41$  require 100lbs stick force.

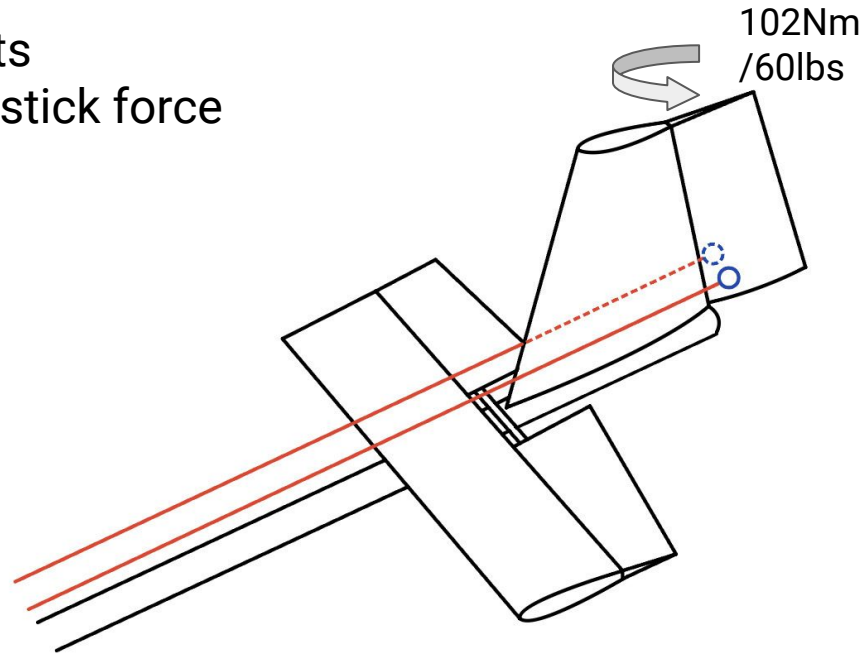


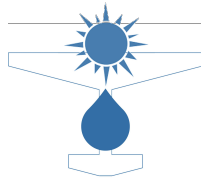


# Control Hinge moment and Stick Force

## Takeaway:

- Max deflection, 40kts
- Full V-Stab at 60lbs stick force





# Generalised Controls Modelling of Pulleys

## Model Constraints and Assumption:

- General legal constraints of 40-67lbs stick forces for ailerons and 100lbs-167lbs for elevator as in figure 2
- All pulleys will be modelled in the fashion of figure 1

Fig 1

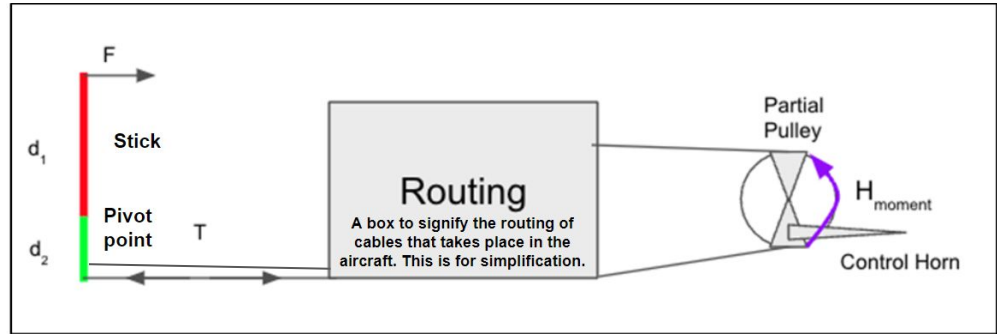
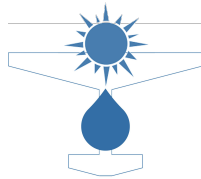


Fig 2

Control	Maximum forces or torques for design weight, weight equal to or less than 5,000 pounds <sup>1</sup>	Minimum forces or torques <sup>2</sup>
<b>Aileron:</b>		
Stick .....	67 lbs .....	40 lbs.
Wheel <sup>3</sup> .....	50 D in.-lbs <sup>4</sup> .....	40 D in.-lbs. <sup>4</sup>
<b>Elevator:</b>		
Stick .....	167 lbs .....	100 lbs.
Wheel (symmetrical) .....	200 lbs .....	100 lbs.
Wheel (unsymmetrical) <sup>5</sup> .....	.....	100 lbs.
Rudder .....	200 lbs .....	150 lbs.





# Pulley Modelling and Equations

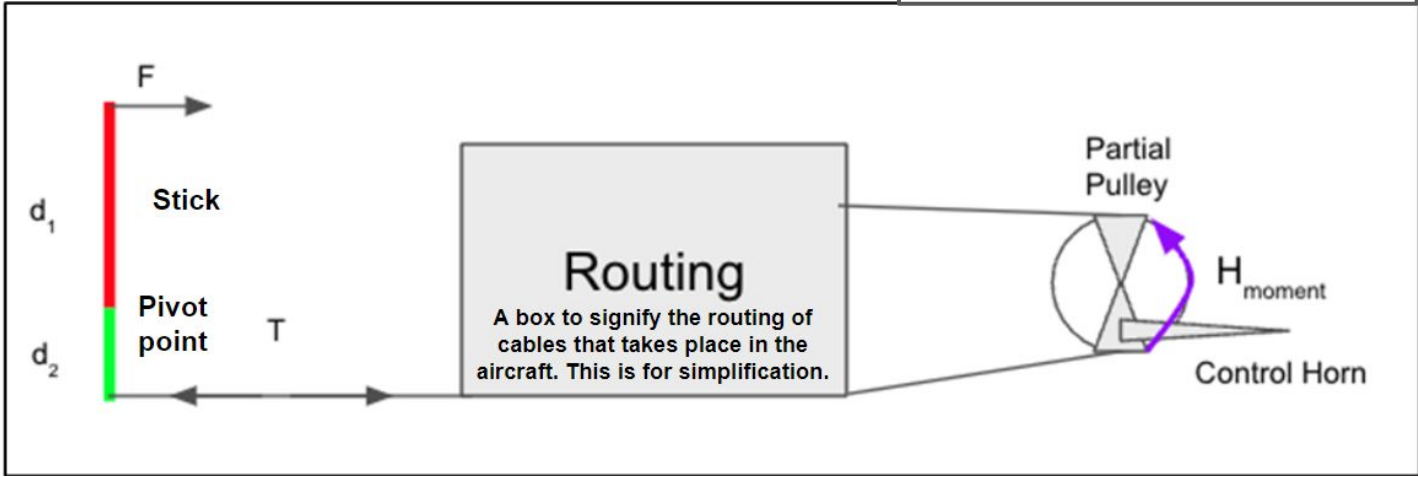
$$F * d_1 = T * d_2$$

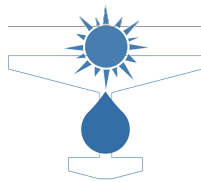
$$T * d_{pulley} = H_{moment}$$

$$F * d_1 / d_2 = H_{moment} / d_{pulley}$$

$$d_p = (H_{moment} / F) * (d_2 / d_1)$$

$$d_1 + d_2 = 1 m$$





# Aileron Hinge Moment and Pulley Analysis

## Design Choice:

- Based on XFLR5 analysis, it seems appropriate to use a 0.8m lever arm with a pulley radius of 0.27m causing a cable tension of 980N and matching 300 Nm hinge control moment at 55 lbs stick force.

$$M / b = q * C_M * c_{ref}^2$$

### Definition:

$M$ , Moment, Newton – meter

$b$ , Aileron Span, meter

$C_m$ , Moment Coefficient, Dimensionless

$c_{ref}$ , Chord reference, meter

$q$ , Dynamic Pressure, Pascal

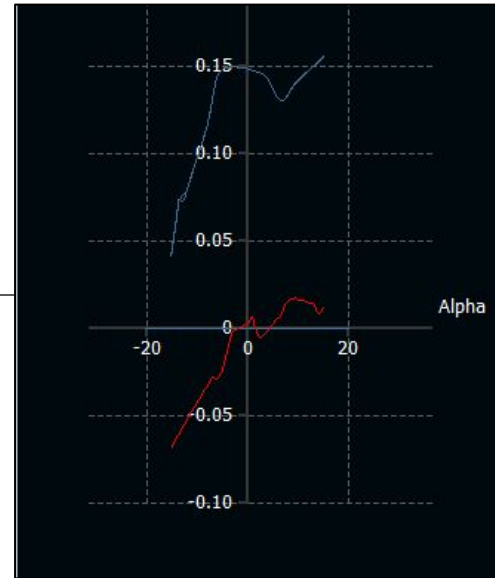
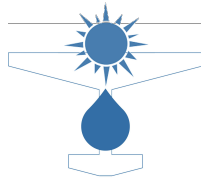


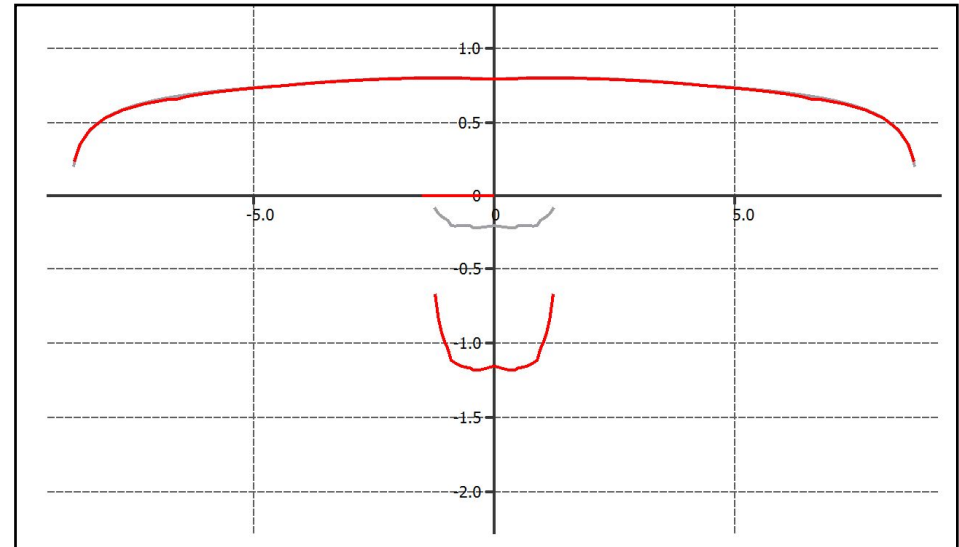
Fig: Non-dimensional moment coefficient vs AoA at 40kts



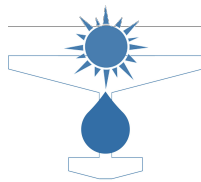
# Elevator Hinge Moment and Pulley Analysis

## Design Choice:

- Based on XFLR5 analysis, it seems appropriate to use a 0.8m lever arm with a radius  $\sim 0.04\text{m}$  for the aileron bell-crank pulleys causing a cable tension of 1780N and matching 80Nm control hingemoment at 100lbs for maximum deflection.



*Fig Jax River. Local Cl vs Span at 0 AoA. Red is at max deflection of 25°*



# Elevator Hinge Moment and Pulley Analysis

## Design Choice:

- The previous Local  $C_l$  vs Span profile can be used to deduce a lift and hence a theoretical upper bound moment, if we take the lift generated at cruise speed as acting at the  $C_g$  of the elevator and assume  $C_l$  of  $\pm 1.25$ . We are also assuming a  $C_p \sim 1$  across the surface on the partial elevator.

$$C_l = 2L/\rho u^2 S$$

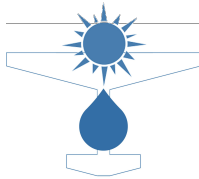
$$1.2 = 2 * L / (1.224 * 21^2 * 1.2) /$$

$$L = 389N$$

$$H_{moment, elevator} = 259N * 0.17 m$$

$$H_{moment, elevator} = 66 Nm$$

*Fig calculating hinge moment of elevator*



# Cable Routing Estimates

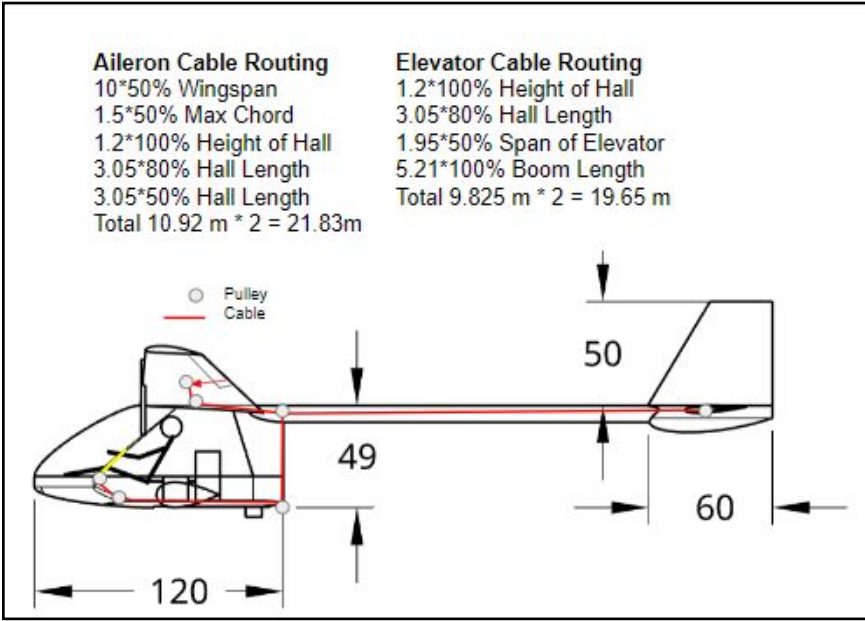
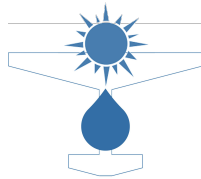


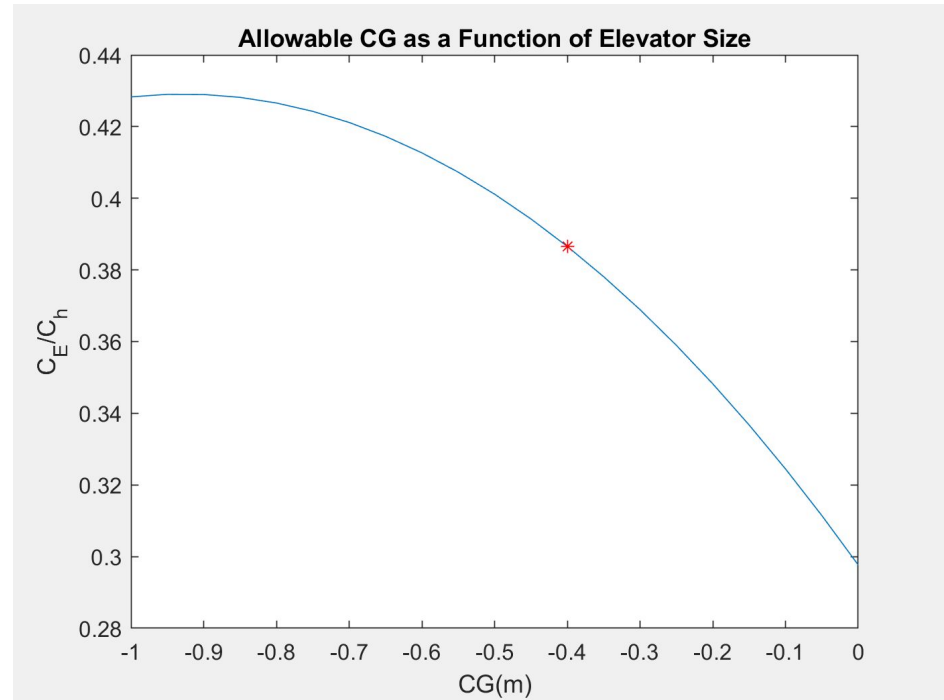
Fig Lower Bound Cable Length

# Control Surfaces

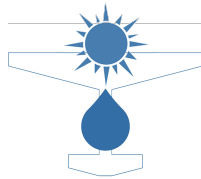


# Elevator Performance

- Chosen size gives us an additional 0.13 m in allowable aft CG Range
- This size was also chosen to account for possible underestimations in the sizing process



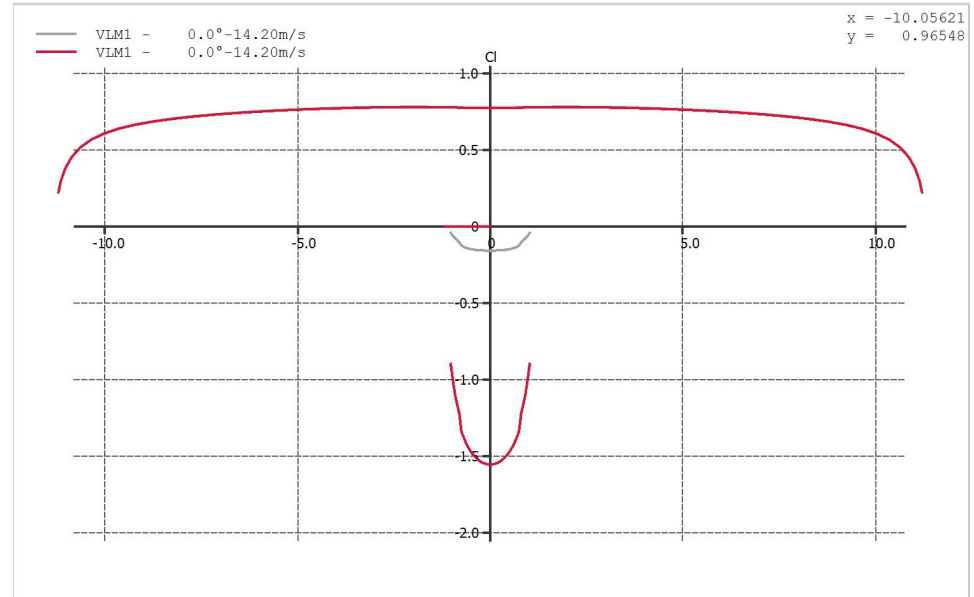
\* : current plane CG estimation



# Elevator Performance

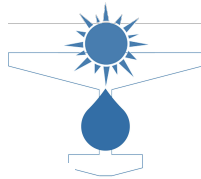
Coefficient of Lift for the Elevator: **-1.2**

Maximum Elevator Stick force



Courtesy of Jax Rivera via XFLR5





# Elevator Sizing Calculations

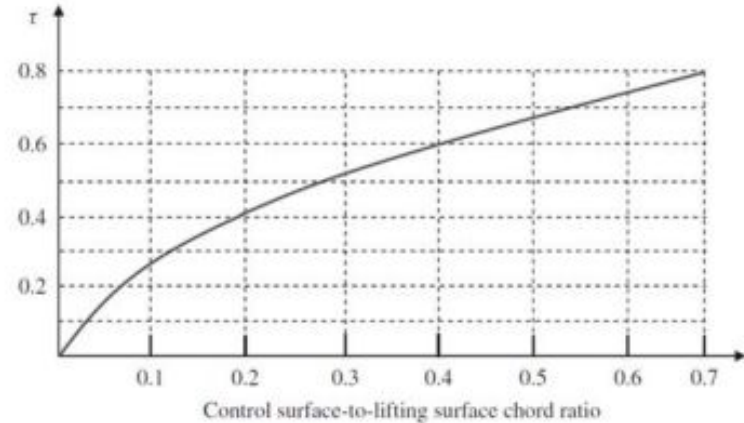
$$L_h = \frac{\left( L_{wf}(x_{mg} - x_{ac_{wf}}) + M_{ac_{wf}} + ma(z_{cg} - z_{mg}) - \right. \\ \left. -W(x_{mg} - x_{cg}) + D(z_D - z_{mg}) - T(z_T - z_{mg}) - I_{yy} \gamma_{mg} \bar{\theta} \right)}{x_{ac_h} - x_{mg}}$$

$$C_{L_h} = C_{L_{\alpha_h}} \alpha_h + C_{L_{\tau_e}} \tau_e \delta_e$$

$$\alpha_h = \alpha + i_h - \varepsilon$$

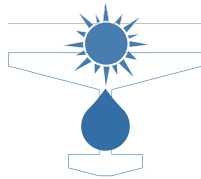
$$\varepsilon = \varepsilon_0 + \frac{\partial \varepsilon}{\partial \alpha} \alpha_w$$

$$\delta_e = \frac{\left( \frac{T * z_T}{\bar{q} * S * \bar{C}} + C_{m_0} \right) C_{L_\alpha} + (C_{L_l} - C_{L_0}) C_{m_\alpha}}{C_{L_\alpha} C_{m_{\delta_e}} - C_{m_\alpha} C_{L_{\delta_e}}}$$



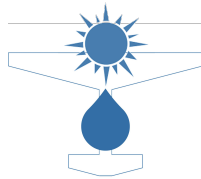
$$C_{m_{\delta_e}} = -C_{L_{\alpha_h}} \eta_h \bar{V}_h \frac{b_e}{b_h} \tau_e$$

$$C_{L_{\delta_e}} = C_{L_{\alpha_h}} \eta_h \frac{s_h}{s} \frac{b_e}{b_h} \tau_e$$



# Elevator Performance Metrics

$\tau_e$ (Elevator Effectiveness)	0.62
$C_{m\delta e}$ (Rate of change of the aircraft pitching moment with respect to elevator deflection)	-1.11 1/rad
$C_{L\delta}$ (Rate of change of the aircraft lift coefficient with respect to elevator deflection)	0.129 1/rad



# Rudder Sizing Calculations

$$N = N_{wing} + N_{w\delta_a} \delta_a + N_{fuselage} + F_v (X_{Vcl} - X_{cg}) - TY_p - DY_p - F_p (X_{cg} - X_p)$$

$$L = L_{wing} + L_{w\delta_a} \delta_a - F_v (Z_v)$$

$$\frac{N}{qS_w b} = C_N = 0 = - \frac{(T+D_{engine\ out})}{q S_w b} + C_{n\delta_r} \delta_r$$

$$C_{n\delta_r} = - C_{L\alpha_v} \eta_{VT} V_{VT} \tau$$

$$V_{VT} = (X_{VTcl} - X_{cg}) * S_{VT} / b * S_w$$

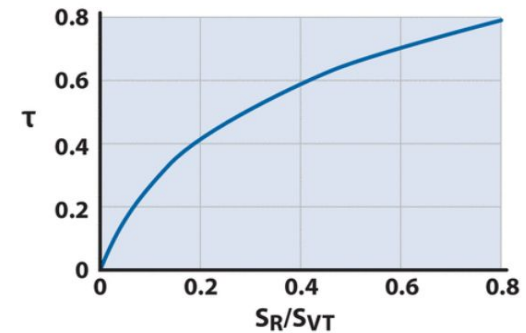
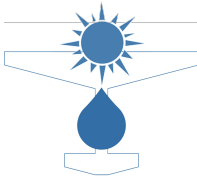
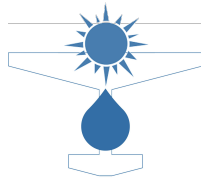


Figure 21.14 Rudder effectiveness chart (from data in Fig. 9.10).



# Rudder Sizing Assumptions

Dengine out	7.5 N	Estimated upper-bound of additional drag from dead engine
C <sub>lv</sub>	4.5 1rad	Approximation of lift curve slope for tail with similar airfoils
eta <sub>v</sub>	0.9	Assumption gathered from example calculations in textbooks
tau	0.3	Gathered from analysis of common aircraft configurations (Figure 21.14)
dh/dt	500 ft/min	Assumption based on requirements of slow aircraft
a	2734 ft/min <sup>2</sup>	Assuming takeoff thrust and distance of 1000 ft



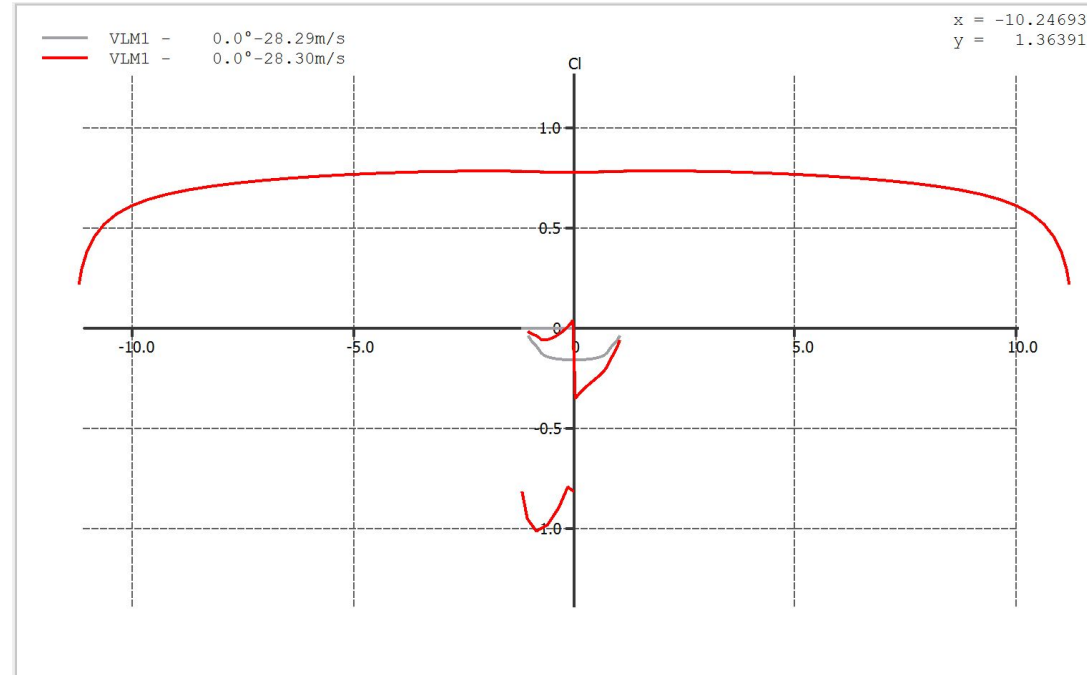
# Rudder Performance

Lift Force Generated by Rudder at Max Deflection at Max Allowable Speed:

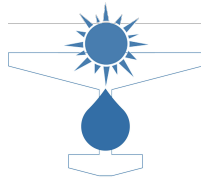
**210 N**

Resultant Pedal Force:

**~ 60 lbs**



Courtesy of Jax Rivera via XFLR5



# Sizing - Roll Rate/Lift Force Equations

Lift Equation

$$L = Cl q A \quad q = \frac{\rho(V^2)}{2}$$

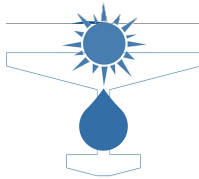
Calculations done at 55 kts

Roll Moment Coefficient relative to Aileron

$$c_{la} = \frac{L_A}{qSb} \quad L_A = 2 * L_{aileron} * y_d$$

Roll rate

$$w_x = -2 * \frac{v}{b} * \frac{c_{la}}{c_{lp}} * \frac{\delta_{Aleft} - \delta_{Aright}}{2}$$



# Water Rudder (S 38)

Chosen for additional control during taxi

Retractable rudder attached to bottom of planing hull

1 ft<sup>2</sup> total area

